

# Direct measurements of the total rate constant of the reaction $\text{NCN} + \text{H}$ and implications for the product branching ratio and the enthalpy of formation of $\text{NCN}$

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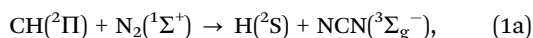
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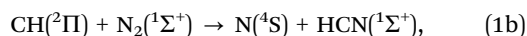
The overall rate constant of the reaction (2),  $\text{NCN} + \text{H}$ , which plays a key role in prompt-NO formation in flames, has been directly measured at temperatures  $962 \text{ K} < T < 2425 \text{ K}$  behind shock waves.  $\text{NCN}$  radicals and  $\text{H}$  atoms were generated by the thermal decomposition of  $\text{NCN}_3$  and  $\text{C}_2\text{H}_5\text{I}$ , respectively.  $\text{NCN}$  concentration-time profiles were measured by sensitive narrow-line-width laser absorption at a wavelength of  $\lambda = 329.1302 \text{ nm}$ . The obtained rate constants are best represented by the combination of two Arrhenius expressions,  $k_2/(\text{cm}^3 \text{ mol}^{-1} \text{ s}^{-1}) = 3.49 \times 10^{14} \exp(-33.3 \text{ kJ mol}^{-1}/RT) + 1.07 \times 10^{13} \exp(+10.0 \text{ kJ mol}^{-1}/RT)$ , with a small uncertainty of  $\pm 20\%$  at  $T = 1600 \text{ K}$  and  $\pm 30\%$  at the upper and lower experimental temperature limits. The two Arrhenius terms basically can be attributed to the contributions of reaction channel (2a) yielding  $\text{CH} + \text{N}_2$  and channel (2b) yielding  $\text{HCN} + \text{N}$  as the products. A more refined analysis taking into account experimental and theoretical literature data provided a consistent rate constant set for  $k_{2a}$ , its reverse reaction  $k_{1a}$  ( $\text{CH} + \text{N}_2 \rightarrow \text{NCN} + \text{H}$ ),  $k_{2b}$  as well as a value for the controversial enthalpy of formation of  $\text{NCN}$ ,  $\Delta_f H_{298\text{K}}^\circ = 450 \text{ kJ mol}^{-1}$ . The analysis verifies the expected strong temperature dependence of the branching fraction  $\phi = k_{2b}/k_2$  with reaction channel (2b) dominating at the experimental high-temperature limit. In contrast, reaction (2a) dominates at the low-temperature limit with a possible minor contribution of the  $\text{HNCN}$  forming recombination channel (2d) at  $T < 1150 \text{ K}$ .

## 1 Introduction

Nitrogen oxides,  $\text{NO}$  and  $\text{NO}_2$  ( $\text{NO}_x$ ), are major atmospheric pollutants formed by different reaction mechanisms in combustion processes. Especially under fuel rich combustion conditions, the so-called prompt-NO formation pathway becomes significant. According to Fenimore,<sup>1</sup> prompt-NO formation is initiated by the reaction of small hydrocarbon radicals with molecular nitrogen from the combustion air. Although it has been proven both theoretically<sup>2–4</sup> and experimentally<sup>5,6</sup> that the key initiation reaction  $\text{CH} + \text{N}_2$  yields the spin-allowed products  $\text{H} + \text{NCN}$ ,

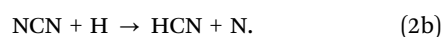
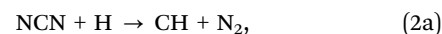


instead of the previously assumed spin-forbidden products  $\text{N} + \text{HCN}$ ,



so far  $\text{NCN}$  chemistry has only been implemented in two detailed kinetic mechanisms for combustion modeling, namely konnov0-6

and GDFkin3.0\_NCN.<sup>7,8</sup> Adopted  $\text{NCN}$  reaction rate constant parameters are largely based on the theoretical work of the M. C. Lin group who reported rate constant values for the most important bimolecular  $\text{NCN}$  consumption reactions  $\text{NCN} + \text{H}$ ,<sup>2,4</sup>  $\text{O}$ ,<sup>9</sup>  $\text{OH}$ ,<sup>10</sup> and others.<sup>11–13</sup> Experimental high-temperature data for  $\text{NCN}$  reactions are scarce. Next to the early shock tube detection of  $\text{NCN}$  and indirect rate constant measurements of the reaction  $\text{NCN} + \text{H}$  performed by Vasudevan *et al.*,<sup>6</sup> Busch and Olzmann investigated the thermal decomposition of  $\text{NCN}$  by means of C-ARAS detection behind shock waves.<sup>14,15</sup> All other direct high-temperature measurements are based on work performed in the Kiel shock tube laboratory operated by us. We use the thermal decomposition of cyanogen azide ( $\text{NCN}_3$ ) as a quantitative source of  $\text{NCN}$  radicals.<sup>16</sup> So far, we were able to report rate constant data for the bimolecular  $\text{NCN}$  reactions with  $\text{O}$ ,  $\text{NCN}$ ,  $\text{NO}$ ,  $\text{NO}_2$ , and its unimolecular decomposition  $\text{NCN} + \text{M} \rightarrow \text{C} + \text{N}_2 + \text{M}$ .<sup>17,18</sup> The purpose of this paper is to provide the first direct high-temperature measurements of the total rate constant of the reaction  $\text{NCN} + \text{H}$ . At combustion temperatures, the reaction exhibits two main reaction channels:



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Depending on the reaction conditions, two additional minor reaction channels forming  $\text{HNC} + \text{N}$  and  $\text{HCN}$  are accessible (see Discussion section). The rate of reaction (2) and its exact branching ratio turned out to be crucial factors for modelling the fate of NCN in hydrocarbon flames.<sup>7,8,19</sup> On the one hand reaction (2a) constitutes the reverse of the prompt-NO initiation reaction (1a) and can be calculated from  $k_{1a}$  via the thermochemical equilibrium constant  $K(\text{CH} + \text{N}_2 \rightleftharpoons \text{NCN} + \text{H}) = k_{1a}/k_{2a}$ . On the other hand the products of reaction (2b) are the same as the products of the formerly assumed spin-forbidden reaction (1b), which brings the new NCN chemistry back to the old Fenimore  $\text{NO}_x$  formation route.

Reported rate constant values for reaction  $\text{NCN} + \text{H}$  have been included in the Arrhenius diagram shown in Fig. 1. An early rate constant estimate of Glarborg *et al.*<sup>20</sup> assumed reaction (2b) to proceed with a temperature independent rate constant close to the collisional rate,  $k_{2b} = 1 \times 10^{14} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  (upper solid line). Shortly after, the reaction  $\text{NCN} + \text{H}$  has been theoretically analyzed by Moskaleva and Lin.<sup>2</sup> As a side note in their paper on the overall rate constant of the reaction  $\text{CH} + \text{N}_2 \rightarrow \text{NCN} + \text{H}$ , but unfortunately without giving much details on the underlying theoretical model, they reported a pressure independent rate constant expression of  $k_{2b} = 1.89 \times 10^{14} \times \exp(-35.3 \text{ kJ mol}^{-1}/RT) \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  revealing that the reaction takes place over a sizable barrier (lower dash-dotted line). Hence, with  $k_{2b} = 1.1 \times 10^{13} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  at  $T = 1500 \text{ K}$ , the reaction is one order of magnitude slower than the initial estimate. Experimentally, Vasudevan *et al.*<sup>6</sup> indirectly determined the rate constant of reaction (2b) in the temperature range of  $2378 \text{ K} < T < 2492 \text{ K}$  by measuring absorption-time profiles of NCN in ethane- $\text{N}_2$  mixtures behind shock waves (triangles with error bars).

Following fast NCN generation by reaction (1a), the observed slow decays of the NCN radical concentration profiles were found to be consistent with  $k_{2b}$  values close to the ones reported by Moskaleva and Lin.

In an indirect experimental and numerical study of the role of NCN formation in low pressure flames, Lamoureux *et al.*<sup>8</sup> reported the value  $k_{2b} = 2.5 \times 10^{13} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  (dotted line), which was also adopted for the GDFkin3.0\_NCN mechanism. Essentially, this value had been chosen to match the experimentally measured NCN and NO concentration profiles in methane and acetylene flames with peak flame temperatures of  $T = 1600\text{--}1835 \text{ K}$ . Therefore, this reported value is highly dependent on the value of the assumed absorption cross section for NCN, which is subject to ongoing discussion.<sup>21</sup> Furthermore, the assumed enthalpy of formation of NCN, here  $\Delta_f H_{298\text{K}}^\circ = 452 \text{ kJ mol}^{-1}$ , is a critical quantity as  $k_{2a}$  is calculated from  $k_{1a}$  via thermochemical equilibrium in their simulations. The crucial role of NCN thermochemistry for modelling prompt-NO formation in flames has been recently highlighted in a paper by Goos *et al.*<sup>22</sup> They nicely demonstrated that the modelled branching ratio of the overall reaction (2) heavily depends on the assumed enthalpy of formation value for NCN. For example, by switching the enthalpy of formation from the low value  $\Delta_f H_{298\text{K}}^\circ = 444.5 \text{ kJ mol}^{-1}$  (representative for theoretical estimates based on single-reference computations)<sup>16,23</sup> to the high value  $466.5 \text{ kJ mol}^{-1}$  (experimental result based on photodissociation experiments)<sup>24</sup> both the simulated NCN peak mole fraction and final NO yield varied by a factor of about 3 for a fuel rich low-pressure  $\text{CH}_4\text{--O}_2\text{--N}_2$  flame. In view of this large variation it becomes clear that also the indirect  $k_{2b}$  value of Lamoureux *et al.* is uncertain.

Very recently the M. C. Lin group<sup>4</sup> updated their theoretical prediction of the rate constants of the reactions  $\text{CH} + \text{N}_2$  and  $\text{NCN} + \text{H}$  based on (i) high-level *ab initio* calculation (CCSD(T) with complete basis set limit) of the underlying quartet and doublet potential energy surfaces and (ii) by correcting a previous coding error in a program used in their original paper<sup>2</sup> from the year 2000. Teng *et al.*<sup>4</sup> clearly showed that reaction (2b) is a spin-allowed process predominantly taking place on a quartet surface, in contrast to reaction (2a) taking place only on a doublet surface. In comparison with their previous work, they now recommend the rate expression  $k_{2b} = 4.96 \times 10^{12} \times T^{0.41} \times \exp(-22.8 \text{ kJ mol}^{-1}/RT) \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  yielding 20% to 40% higher  $k_{2b}$  values at temperatures from 1500 K to 2000 K (upper dash-dotted line in Fig. 1). Another important finding was that an alternative reaction channel yielding  $\text{HNC} + \text{N}$  is minor and that the recombination reaction yielding HNCN, which dominates at room temperature, contributes to less than 5% at combustion relevant temperatures of  $T > 1000 \text{ K}$  at 1 bar total pressure. Remarkably high total rate constant values with a shallow minimum of  $k_2 \approx 1.3 \times 10^{14} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  at  $T = 3180 \text{ K}$  have been reported in their work as well (long-dashed curve), which we consider unfeasible. As it turns out in this work, the recommendation of Teng *et al.* for reaction channel (2a) alone is already up to 6 times higher (short-dashed curve) than our experimentally determined total rate constant  $k_2$  (see also Section 4).

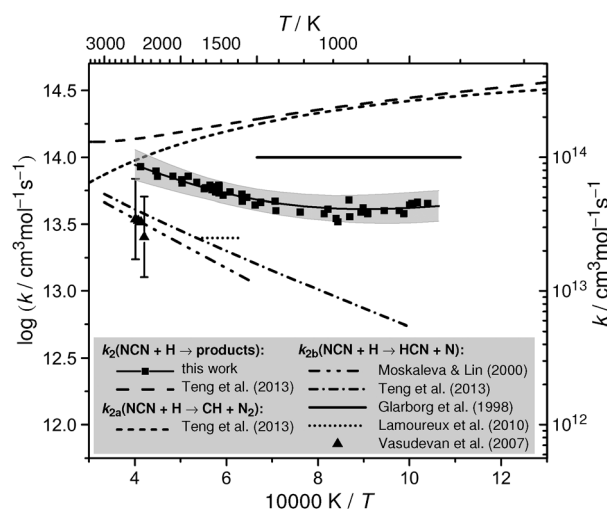


Fig. 1 Experimental and theoretical literature rate constant data for the reaction  $\text{NCN} + \text{H}$  in comparison with the results of this work. Estimate of Glarborg *et al.*,<sup>20</sup> shock tube data of Vasudevan *et al.*,<sup>6</sup> flame data of Lamoureux *et al.*,<sup>8</sup> and theoretical predictions of Teng *et al.*<sup>4</sup> and Moskaleva and Lin<sup>2</sup> are illustrated as outlined in the legend. The squares depict the experimental data of this work; the shaded area and the thick solid curve correspond to the range of uncertainty and a fit of the experimental data, respectively.



From this short overview of existing literature data we conclude that a reliable modeling of NCN chemistry in flames is not possible so far. Clearly, experimental data on the rate constant of the reaction  $\text{NCN} + \text{H}$  are needed to constrain the rate constant uncertainties and to advance current prompt-NO formation models.

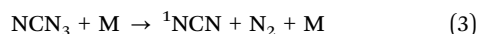
## 2 Experimental

### Shock tube apparatus

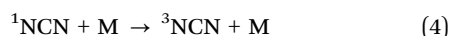
All experiments were carried out in an electropolished stainless steel shock tube with inner diameter of 81 mm. A more detailed description can be found elsewhere.<sup>25</sup> Briefly, hydrogen or mixtures of hydrogen and nitrogen were used as driver gas; diaphragms were made from 80 or 100  $\mu\text{m}$  thick aluminium foil. The experimental conditions behind the incident and reflected shock waves were calculated from pre-shock conditions and the shock wave velocity, which was measured by four fast piezoelectric sensors (PCB Piezotronics M113A21). A frozen-chemistry code was applied taking into account real gas effects and the measured shock wave damping, which was on the order of 1% per meter. Storage gas mixtures of 500–750 ppm  $\text{NCN}_3$  and 1000 ppm  $\text{C}_2\text{H}_5\text{I}$  in argon were prepared using the partial pressure method and were further diluted with argon using calibrated mass flow controllers (Aera, FC-7700CU). The low pressure section of the shock tube was flushed for about 5 min at  $p \approx 30$  mbar to reduce possible adsorption effects on the shock tube wall.

### NCN precursor

The thermal decomposition of cyanogen azide ( $\text{NCN}_3$ )



has been used as a quantitative source of NCN radicals.<sup>26,27</sup> It was shown in previous publications<sup>16,28</sup> that the thermal decomposition initially yields NCN in its first electronically excited singlet state. Under the experimental conditions applied in this work with total densities  $\rho > 2 \times 10^{-6} \text{ mol cm}^{-3}$  and temperatures  $T > 962 \text{ K}$ , the subsequent collision induced intersystem crossing (CIISC) is rate limiting for triplet NCN formation according to



The CIISC efficiency is strongly dependent on the nature of the collider, reveals a non-linear pressure dependence due to a pressure saturation effect, and increases with increasing temperature.<sup>18,28</sup> In order to accurately model the initial formation rate of  ${}^3\text{NCN}$  (denoted NCN in the following), the CIISC rate constant has been allowed to vary within the error limit reported by Dammeier *et al.*<sup>28</sup>

The highly toxic and explosive precursor molecule  $\text{NCN}_3$  has been directly synthesized using a procedure described previously.<sup>29,30</sup> Briefly, a small amount of gaseous cyanogen bromide ( $\text{BrCN}$ ,  $\sim 20$  mbar) was passed into an evacuated 1 L glass flask containing a huge excess of solid sodium azide ( $\text{NaN}_3$ ). After a 8–10 h reaction time, the gaseous products were

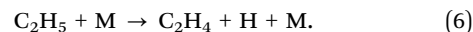
analyzed by FTIR spectroscopy. Almost no water and carbon dioxide ( $\sim 0.01\%$ ), which serves as an indicator for a potential gas leak, were present in the reaction samples and the impurities of remaining cyanogen bromide were well below 4%, in some cases  $< 0.1\%$ . A slow decomposition of about 10%  $\text{NCN}_3$  per day took place in the storage flask, therefore mixtures were used up within 3 days. Accurate initial  $\text{NCN}_3$  mole fraction in the actual reaction mixtures were determined by modeling the maximum NCN yield in the experiments and were found to be consistent with the expected  $\text{NCN}_3$  content in the storage gas mixtures in all cases.

### H precursor

Hydrogen atoms were generated by the thermal unimolecular decomposition of ethyl iodide ( $\text{C}_2\text{H}_5\text{I}$ ). Under typical experimental conditions behind shock waves, the reaction can be assumed to take place close to the high pressure limit<sup>39</sup> and exhibits two main reaction channels:



H atom formation proceeds through the fast subsequent decomposition of the ethyl radical,



Although ethyl iodide has been widely used as an H atom precursor, until recently the assumed absolute values and temperature dependences of the H atom yield were uncertain and often represented the most significant source of error in such studies. Selected values of reported branching ratios  $\phi = k_{5a}/(k_{5a} + k_{5b})$  are collected in Fig. 2. The most frequently used value of  $\phi = 0.87 \pm 0.11$  is based on direct H and I atom resonance absorption spectroscopic (ARAS) measurements performed by Kumaran *et al.*<sup>31</sup> at temperatures of  $946 \text{ K} < T < 1303 \text{ K}$ .

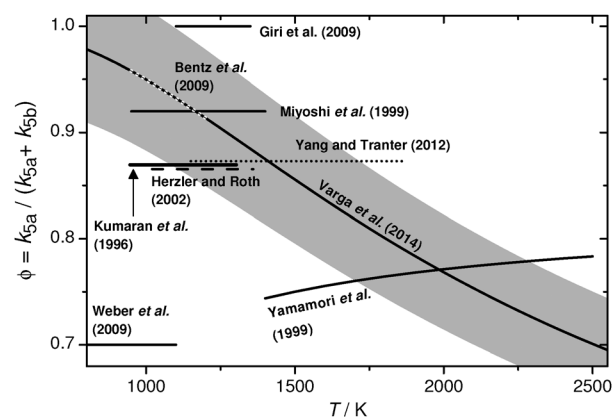


Fig. 2 Selected literature values for the branching ratio  $\phi$  of the thermal decomposition of ethyl iodide yielding  $\text{C}_2\text{H}_5 + \text{I}$  (channel (5a)) and  $\text{C}_2\text{H}_4 + \text{HI}$  (channel (5b)), respectively. H and/or I atom resonance absorption measurements: Kumaran *et al.*,<sup>31</sup> Yamamori *et al.*,<sup>32</sup> Miyoshi *et al.*,<sup>33</sup> Herzler and Roth,<sup>34</sup> Giri *et al.*,<sup>35</sup> and Bentz *et al.*,<sup>36</sup> laser schlieren technique: Yang and Tranter;<sup>37</sup> mass spectrometry: Weber *et al.*,<sup>38</sup> global optimization: Varga *et al.*<sup>39</sup> The gray area represents the assumed uncertainty range of  $\pm 7\%$ .



Also based on ARAS experiments, Herzler and Roth<sup>34</sup> reported a coinciding value, Yamamori *et al.*<sup>32</sup> used lower values of  $\phi < 0.78$  at overall higher temperatures, Miyoshi *et al.*<sup>33</sup> determined a higher value of  $\phi = (0.92 \pm 0.06)$ , and Giri *et al.*<sup>35</sup> assumed  $\phi = 1$  by considering the hydrogen forming pathway only. Recently, Weber *et al.*,<sup>38</sup> Yang and Tranter,<sup>37</sup> and Bentz *et al.*<sup>36</sup> revisited the ethyl iodide pyrolysis. Whereas Yang and Tranter found excellent agreement with their laser-schlieren densitometry shock tube measurements by assuming  $\phi = 0.87$ , Weber *et al.* report a significantly lower value of  $\phi = (0.7 \pm 0.1)$  from a mass spectrometric investigation of the flash pyrolysis of ethyl iodide. However, Bentz *et al.* could show by a combination of H- and I-ARAS measurements and statistical rate calculations that the abstraction reaction  $\text{H} + \text{C}_2\text{H}_5\text{I} \rightarrow \text{C}_2\text{H}_5 + \text{HI}$ , which had been neglected in former studies, needs to be taken into account for an accurate analysis of the branching ratio. Their experimental data, together with other available literature data, have been very recently reanalyzed by Varga *et al.*<sup>39</sup> in a follow-up publication using a new global optimization method developed by Turányi.<sup>40</sup> The simultaneous optimization of the rate constant expressions of all relevant reactions yielded a considerably temperature dependent branching ratio decreasing from  $\phi(T = 962 \text{ K}) = 0.96$  to  $\phi(T = 2450 \text{ K}) = 0.71$  over the temperature range of this study. A very low  $3\sigma$  uncertainty level of  $\pm 0.035$  has been specified by Varga *et al.* at a temperature of  $T = 1200 \text{ K}$ . As can be seen in Fig. 2 the recommended branching ratios are consistent with most of the previous literature data. We consider these results to be most reliable and therefore adopted the ethyl iodide decomposition mechanism as reported by Varga *et al.* It is included in the list of reactions in Table 1.

We have recommended the use of a different expression with opposite temperature dependence of  $\phi$  in a previous paper dating back to the year 2002.<sup>41</sup> That recommendation was based on a theoretical treatment of the unimolecular decomposition of ethyl iodide with barrier heights taken from the paper of Kumaran *et al.* Then, the energy barrier  $E_0$  of the I atom forming C–I bond fission channel (5a) was assumed to be about  $15 \text{ kJ mol}^{-1}$  higher than of the HI elimination channel (5b). However, the recent accurate CCSD(T) *ab initio* data of Bentz *et al.*<sup>36</sup> showed that both barriers are more or less energetically equal, which is more consistent with the reported decrease of  $\phi$  with increasing temperature. For a more detailed treatment of the unimolecular decomposition reactions of alkyl iodides in the framework of statistical rate theories we refer to the work of Kumaran *et al.*, Miyoshi *et al.*, and Bentz *et al.*<sup>31,33,36</sup>

### NCN detection

Triplet NCN radicals were detected by time-resolved difference amplification laser absorption spectroscopy at  $\tilde{\nu} = 30383.11 \text{ cm}^{-1}$  ( $\lambda = 329.1302 \text{ nm}$ ). The absorption feature at this wavelength mainly stems from a superposition of the  $^3\Pi_1$  sub band of the  $\tilde{A}^3\Pi_u(000) - \tilde{X}^3\Sigma_g(000)$  and the  $Q_1$  band head of the  $^3\Sigma^+(010) - ^3\Pi(010)$  transition.<sup>21</sup> About 1 mW UV laser radiation was generated by intra-cavity frequency doubling of a continuous-wave ring-dye laser (Coherent, 899) with DCM-Special as dye pumped with a solid state Nd:YVO<sub>4</sub> laser using 8 W at  $\lambda = 532 \text{ nm}$  (Coherent Verdi V10). The wavelength of the laser fundamental was measured interferometrically by a wavemeter (MetroLux) with an accuracy of  $\Delta\tilde{\nu} \approx \pm 0.015 \text{ cm}^{-1}$ . The UV laser beam was split into a detection and a reference beam by a

**Table 1** Rate constant parameters for important NCN reactions and the ethyl iodide submechanism. Rate constants are given in terms of  $k = AT^n \exp(-E_a/RT)$  in units of  $\text{cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  and  $\text{kJ}$ . The listed rate constants for NCN (representing  $^3\text{NCN}$ ) reactions have been duplicated for  $^1\text{NCN}$  to approximately take into account  $^1\text{NCN}$  secondary chemistry. In addition to the reactions listed here, the GRI-Mech 3.0 has been used as base mechanism<sup>42</sup> supplemented by iodine chemistry adopted from our previous work<sup>41</sup>

No.	Reaction	A	n	E <sub>a</sub>	Ref.
3	$\text{NCN}_3 \rightleftharpoons ^1\text{NCN} + \text{N}_2$	$4.9 \times 10^9$		71	28
4	$^1\text{NCN} \rightarrow \text{NCN}$	$2.0 \times 10^6$		31	28 <sup>c</sup>
2	$\text{NCN} + \text{H} \rightarrow \text{products}$				See text
2a	$\text{NCN} + \text{H} \rightleftharpoons \text{CH} + \text{N}_2$	$4.2 \times 10^{15}$	−0.69	2.0	This work <sup>b</sup>
2b	$\text{NCN} + \text{H} \rightleftharpoons \text{HCN} + \text{N}$	$7.9 \times 10^{12}$	0.41	22.8	This work <sup>a</sup>
7	$\text{NCN} + \text{M} \rightleftharpoons \text{C} + \text{N}_2 + \text{M}$	$8.9 \times 10^{14}$		260	17
8	$\text{NCN} + \text{NCN} \rightleftharpoons \text{CN} + \text{CN} + \text{N}_2$	$3.7 \times 10^{12}$			28
9	$\text{NCN} + \text{C} \rightleftharpoons \text{CN} + \text{CN}$	$1.0 \times 10^{14}$			28
10	$\text{NCN} + \text{N} \rightleftharpoons \text{N}_2 + \text{CN}$	$1.0 \times 10^{13}$			2
11	$\text{NCN} + \text{CN} \rightleftharpoons \text{C}_2\text{N}_2 + \text{N}$	$1.3 \times 10^{14}$		33.5	2
11	$\text{NCN} + \text{CH} \rightleftharpoons \text{HCN} + \text{CN}$	$3.2 \times 10^{13}$		−3.6	2
13	$\text{NCN} + \text{CH}_2 \rightleftharpoons \text{H}_2\text{CN} + \text{CN}$	$8.0 \times 10^{13}$		26.9	2
5a	$\text{C}_2\text{H}_5\text{I} \rightleftharpoons \text{C}_2\text{H}_5 + \text{I}$	$3.4 \times 10^{13}$		203	39
5b	$\text{C}_2\text{H}_5\text{I} \rightleftharpoons \text{C}_2\text{H}_4 + \text{HI}$	$4.7 \times 10^{13}$		226	39
6	$\text{C}_2\text{H}_5 + \text{M} \rightleftharpoons \text{C}_2\text{H}_4 + \text{H} + \text{M}$	$1.0 \times 10^{18}$		140	39
14	$\text{C}_2\text{H}_5\text{I} + \text{H} \rightleftharpoons \text{C}_2\text{H}_5 + \text{HI}$	$1.0 \times 10^{15}$		21.6	39
15	$\text{C}_2\text{H}_5\text{I} + \text{I} \rightleftharpoons \text{C}_2\text{H}_5 + \text{I}_2$	$4.0 \times 10^{13}$		69.9	43
16a	$\text{C}_2\text{H}_5 + \text{H} \rightleftharpoons \text{CH}_3 + \text{CH}_3$	$4.2 \times 10^{13}$			44
16b	$\text{C}_2\text{H}_5 + \text{H} \rightleftharpoons \text{C}_2\text{H}_4 + \text{H}_2$	$1.2 \times 10^{12}$			45
17	$\text{H} + \text{HI} \rightleftharpoons \text{H}_2 + \text{I}$	$6.6 \times 10^{13}$		4.1	39

<sup>a</sup> Rate expression of Teng *et al.*<sup>4</sup> scaled by a factor of 1.6. <sup>b</sup> Assuming  $\Delta_f H_{298\text{K}}^\circ(\text{NCN}) = 450 \text{ kJ mol}^{-1}$ ; this corresponds to  $k_{1a}(\text{CH} + \text{N}_2 \rightarrow \text{NCN} + \text{H}) = 2.3 \times 10^{10} \times T^{0.53} \times \exp(-71.2 \text{ kJ mol}^{-1}/RT)$ . <sup>c</sup>  $\rho = 3.5 \times 10^6 \text{ mol cm}^{-3}$ ; for other densities see ref. 28.





(50:50) beam splitter plate. The detection beam was passed through the shock tube and coupled into an optical fiber (Thorlabs BF H22-550) connected to a balanced photodetector and amplifier (Thorlabs PDB 150A-EC). The intensity of the reference laser beam was fine-tuned by a variable neutral density filter to match the intensity of the detection beam. The resulting difference signals were low-pass-filtered (1.4 MHz), amplified (Ortec Fast Preamp 9305, 18 dB), and stored by an analog input board (Measurement Computing, PCI-DAS4020/12, 20 MHz, 12 bit). The NCN concentration-time profiles were calculated from the detected absorption profiles based on NCN absorption cross sections  $\log(\sigma(\text{base e})/(\text{cm}^2 \text{ mol}^{-1})) = 8.9\text{--}8.3 \times 10^{-4} \times T/K$  previously measured with an accuracy of  $\pm 25\%$  using the same apparatus at similar temperatures and pressures.<sup>16</sup>

### 3 Results

The reaction of NCN radicals with hydrogen atoms has been investigated behind incident and reflected shock waves in the temperature and pressure ranges  $962 \text{ K} < T < 2425 \text{ K}$  and  $290 \text{ mbar} < p < 2130 \text{ mbar}$ , respectively, at three different total densities of  $\rho \approx 3.5 \times 10^{-6}$ ,  $7.4 \times 10^{-6}$ , and  $1.5 \times 10^{-5} \text{ mol cm}^{-3}$ . Reaction gas mixtures contained 72–363 ppm ethyl iodide and 3–31 ppm  $\text{NCN}_3$  in argon. In most cases, a large excess of ethyl iodide with  $[\text{C}_2\text{H}_5\text{I}]_0/[\text{NCN}_3]_0$  ratios up to 60 was applied, hence the hydrogen atom was used as the excess species. Experimental conditions are listed in Table 2.

Fig. 3a illustrates a typical experiment behind the incident shock wave at a temperature  $T = 1720 \text{ K}$  and a total density  $\rho = 3.43 \times 10^{-6} \text{ mol cm}^{-3}$  with initial mole fractions of  $x(\text{NCN}_3) = 21 \text{ ppm}$  and  $x(\text{C}_2\text{H}_5\text{I}) = 72 \text{ ppm}$ . After the arrival of the incident

shock wave, the NCN signal increases within  $20 \mu\text{s}$ . Obviously, both the thermal decomposition of  $\text{NCN}_3$  and the singlet-triplet relaxation of NCN are fast. The subsequent NCN decay is well resolved and is more or less complete at the end of the experimental time window set by the Schlieren signal of the reflected shock wave at  $t = 460 \mu\text{s}$ .

In order to extract rate constants for reaction (2),  $\text{NCN} + \text{H} \rightarrow$  products, the NCN profiles were numerically simulated using the CHEMKIN-II package.<sup>46</sup> The GRI-Mech 3.0 was used as a base mechanism<sup>42</sup> supplemented by an iodine submechanism adopted from our previous work<sup>41</sup> and the reactions outlined in Table 1. The mechanism for NCN secondary chemistry was assembled from literature data, in particular from our previous measurements that have been validated to reproduce NCN concentration-time profiles of pure  $\text{NCN}_3$ -argon mixtures over a wide range of experimental conditions. The ethyl iodide decomposition has been modeled by including the recently optimized submechanism reported by Varga *et al.*<sup>39</sup> (*vide supra*). In order to identify potential contributions of  $^1\text{NCN}$  secondary chemistry, all triplet NCN reactions have been duplicated for singlet NCN. Although this treatment neglects the presumably different  $^1\text{NCN}$  reactivity, it can be safely assumed that  $^1\text{NCN}$  secondary chemistry is dominated by its relaxation reaction forming triplet NCN within the first few  $\mu\text{s}$  of the experiments. Thermodynamic data were taken from Burcat's thermodynamic database<sup>47</sup> with updated NASA polynomial parameters for NCN from Goos *et al.*<sup>22</sup> Note that the assumed value for the enthalpy of formation of NCN, although of utmost importance for the discussion of the branching ratio of reaction (2) (*vide infra*), is not important for the determination of the total rate constant from the experimental profiles.

The solid curve in Fig. 3a reflects the best fit of the data using  $k_2$  as an adjustable parameter. Two additional simulations using

Table 2 Experimental conditions and results

$T/K$	$\rho \times 10^6 / \text{mol cm}^{-3}$	$x(\text{NCN}_3) \text{ ppm}$	$x(\text{C}_2\text{H}_5\text{I}) \text{ ppm}$	$k_2 \times 10^{-13} / \text{cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$	$T/K$	$\rho \times 10^6 / \text{mol cm}^{-3}$	$x(\text{NCN}_3) \text{ ppm}$	$x(\text{C}_2\text{H}_5\text{I}) \text{ ppm}$	$k_2 \times 10^{-13} / \text{cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$
1186	3.78	7.4	75	3.3	962	3.52	3.8	185	4.5
1714	3.43	19.0	72	6.1	1000	3.57	4.0	185	4.4
1720	3.43	21.0	72	5.5	1192	3.77	4.6	185	3.5
1813	3.46	21.8	72	5.8	1230	3.80	5.2	185	3.8
1870	3.46	22.8	72	6.5	1552	4.03	9.5	185	5.0
1936	4.20	9.0	76	7.2	1747	3.44	27.5	184	6.0
1991	3.51	27.8	72	6.8					
2070	3.54	23.5	72	7.2	1482	3.99	5.0	299	4.6
2227	3.57	25.0	72	7.2	1509	4.01	3.0	104	4.4
2242	3.55	26.0	72	7.9	1578	3.37	24.5	712	5.3
2425	2.89	28.0	72	8.5	1714	3.41	23.7	40	6.2
					1774	3.31	31.0	363	6.2
					1988	2.11	11.9	155	6.4
996	3.56	7.0	138	4.5					
1013	3.59	4.6	137	3.8					
1023	3.60	6.9	138	4.0	983	7.10	7.0	138	4.6
1101	3.69	3.2	137	3.8	993	7.13	6.5	138	4.5
1113	3.70	5.3	138	4.2	1059	7.25	5.8	138	4.0
1151	3.73	8.5	136	3.6	1119	7.41	6.4	138	3.9
1217	3.80	12.5	138	4.1	1153	7.48	6.5	138	4.8
1314	3.88	4.0	137	3.9	1646	7.19	4.0	185	5.5
1413	3.95	6.3	136	4.0	1760	7.43	7.4	138	5.7
1416	3.94	4.6	137	4.7	1805	7.50	3.9	137	5.9
1576	4.05	6.3	136	4.7					
1688	3.41	16.4	131	5.2	1713	14.7	5.0	138	5.4
					1735	14.8	5.0	138	5.5



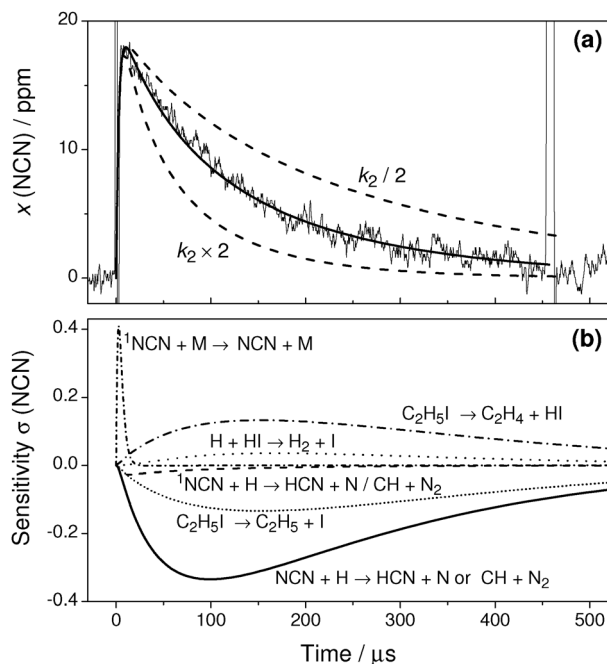


Fig. 3 (a) Experimental NCN profile in comparison with numerical simulations.  $T = 1720$  K,  $\rho = 3.43 \times 10^{-6}$  mol cm $^{-3}$ ,  $p = 490$  mbar,  $x(\text{NCN}_3) = 21$  ppm,  $x(\text{C}_2\text{H}_5\text{I}) = 72$  ppm,  $k_2 = 5.5 \times 10^{13}$  cm $^3$  mol $^{-1}$  s $^{-1}$ . (b) Sensitivity analysis.

$k_2$  varied by a factor of two (dashed curves) are shown as well. They deviate strongly from the experimental profile demonstrating the high sensitivity of reaction (2). Assuming either the products of reaction channel (2a), CH + N $_2$ , or reaction channel (2b), HCN + N, did not change the extracted  $k_2$  value within error limits. The high sensitivity of reaction (2) is further outlined in the sensitivity analysis shown in Fig. 3b. Here, the sensitivity coefficient  $\sigma(i, t)$  for reaction  $i$  at time  $t$  was normalized with respect to the maximum concentration  $[\text{NCN}]_{\text{max}}$  over the time history,  $\sigma(i, t) = 1/[\text{NCN}]_{\text{max}} \times (\partial[\text{NCN}]/\partial \ln k_i)$ . For the analysis, a branching ratio of  $\phi = k_{2b}/k_2 = 0.5$  has been assumed. Following the initial increase of the signal, which is determined by the NCN relaxation reaction (4), reaction (2) dominates the NCN decay. The relatively high sensitivity coefficients for reactions (5a) and (5b) directly reflect the influence of the branching ratio of reaction (5) and hence the assumed H atom yield from ethyl iodide pyrolysis. Presuming that this branching ratio is accurate, the sensitivity analysis reveals that the rate constant of reaction (2) could be directly measured under nearly pseudo first-order conditions.

Whereas the highest feasible experimental temperature was limited by the increasingly fast thermal decomposition of NCN, towards lower temperatures non-NCN secondary chemistry becomes significant as well. This is illustrated by the  $T = 1150$  K experiment and sensitivity analysis shown in Fig. 4. Both reaction (14),  $\text{H} + \text{C}_2\text{H}_5\text{I}$ , and the assumed products of reaction (2) become important. Assuming the products of channel (2a), HCN + N, at longer reaction times the reaction  $\text{N} + \text{NCN}$  significantly consumes NCN. Similarly, assuming the products of channel (2b), CH + N $_2$ , the reaction  $\text{C} + \text{NCN}$  gains importance. Here, C atoms are efficiently generated by the reaction  $\text{CH} + \text{H} \rightarrow \text{C} + \text{H}_2$ . Consistent with the expected

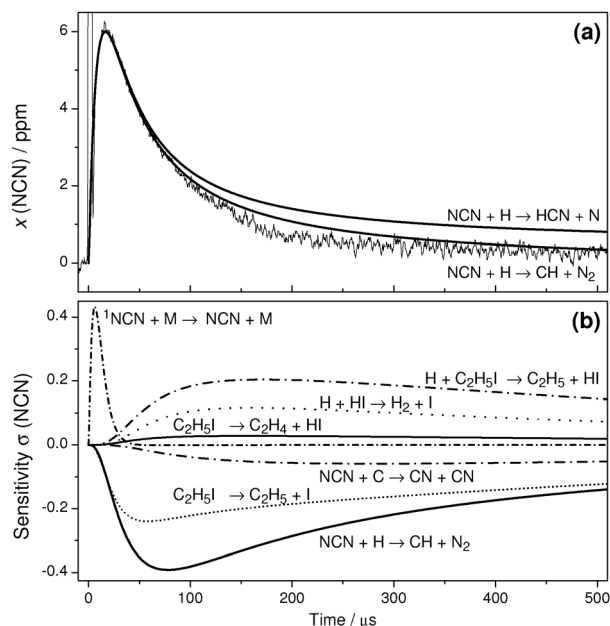


Fig. 4 (a) Experimental NCN profile in comparison with numerical simulations.  $T = 1150$  K,  $\rho = 7.48 \times 10^{-6}$  mol cm $^{-3}$ ,  $p = 720$  mbar,  $x(\text{NCN}_3) = 6.5$  ppm,  $x(\text{C}_2\text{H}_5\text{I}) = 138$  ppm,  $k_2 = 4.8 \times 10^{13}$  cm $^3$  mol $^{-1}$  s $^{-1}$ . (b) Sensitivity analysis.

diminishing role of the activation controlled channel (2b), somewhat better agreement with the experiment is obtained by assuming channel (2a). However, as the remaining differences between simulation and experiment could not be clearly attributed to a specific secondary reaction, no attempt was made to further improve the simulation at longer reaction times. Instead, the rate of reaction (2) was extracted from the NCN decay by fitting the transient at short reaction times where secondary chemistry did not yet exert a significant influence.

All measured rate constants  $k_2$  are listed in Table 2 and are shown in Arrhenius form in Fig. 5. Overall, the rate constants follow the same trend independent of total density (varied by a factor of 4) and mixture composition (varied within  $1.7 < [\text{C}_2\text{H}_5\text{I}]_0/[\text{NCN}_3]_0 < 60$ ). The data reveal a shallow minimum at temperatures around 1050–1200 K indicating that at least two reaction channels are active, presumably channels (2a) and (2b) with (2b) becoming more important towards higher temperatures. Accordingly, in the temperature range  $962 \text{ K} < T < 2425 \text{ K}$  the total rate constant can be best represented by the sum of two Arrhenius expressions,

$$k_2/(\text{cm}^3 \text{ mol}^{-1} \text{ s}^{-1}) = 3.49 \times 10^{14} \exp(-33.3 \text{ kJ mol}^{-1}/RT) + 1.07 \times 10^{13} \exp(+10.0 \text{ kJ mol}^{-1}/RT), \quad (\text{I})$$

depicted as the solid curve in Fig. 5. The two single Arrhenius terms are also shown as dashed lines and can be roughly interpreted to represent the contributions of channel (2b) (first term) and channel (2a) (second term). A more refined analysis of the overall rate constant will be presented below.

An error analysis has to take into account uncertainties resulting from the scatter of the data ( $\pm 6\%$ ), the mixture

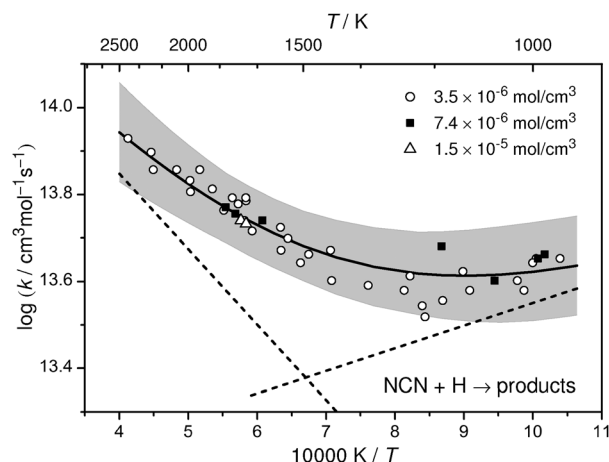


Fig. 5 Arrhenius plot for  $k_2$  measured at three different total densities. The solid curve corresponds to a fit of the data using a sum of two Arrhenius expressions (dashed lines). The gray area represents the uncertainty range based on a comprehensive error analysis.

composition (in particular the initial ethyl iodide mole fraction,  $\pm 3\%$ ), the channel branching ratio of the ethyl iodide decomposition (estimated from Fig. 2 to be  $\pm 7\%$ ), the NCN absorption cross section ( $\pm 25\%$ , resulting in a 3% uncertainty in  $k_2$ ), and the secondary chemistry. In the middle of the investigated temperature range ( $T \approx 1600$  K), a direct pseudo first-order evaluation was possible and hence errors from secondary chemistry are minor. Nevertheless, we allow for a 10% error due to a possibly large uncertainty of the rate constant of the reaction (10),  $\text{NCN} + \text{N}$ , which has not been directly measured so far. Increasing its rate constant from  $1 \times 10^{13} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  to  $1 \times 10^{14} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  would make this reaction sensitive because N atoms are formed in reaction (2b) and hence slightly too high  $k_2$  values would have been determined by our analysis. Taking into account partial error compensation, we estimate the overall uncertainty of  $k_2$  to be  $\pm 20\%$  at  $T = 1600$  K, increasing to  $\pm 30\%$  due to higher uncertainties resulting from secondary chemistry and the employed ethyl iodide branching ratio at the high and low temperature limit of the experiments. A corresponding uncertainty range is indicated by the grey shaded area in Fig. 5.

## 4 Discussion

The obtained total rate constant expression for  $k_2$  is compared with selected literature values and further analyzed in order to derive a consistent set of rate constants for the two main high-temperature reaction channels (2a) and (2b) as well as the NCN enthalpy of formation  $\Delta_f H_{298\text{K}}^\circ$  ( $\Delta H$  in the following) in Fig. 6. As it was shown by the high level *ab initio* calculations of Teng *et al.*,<sup>4</sup> from the four feasible reaction channels

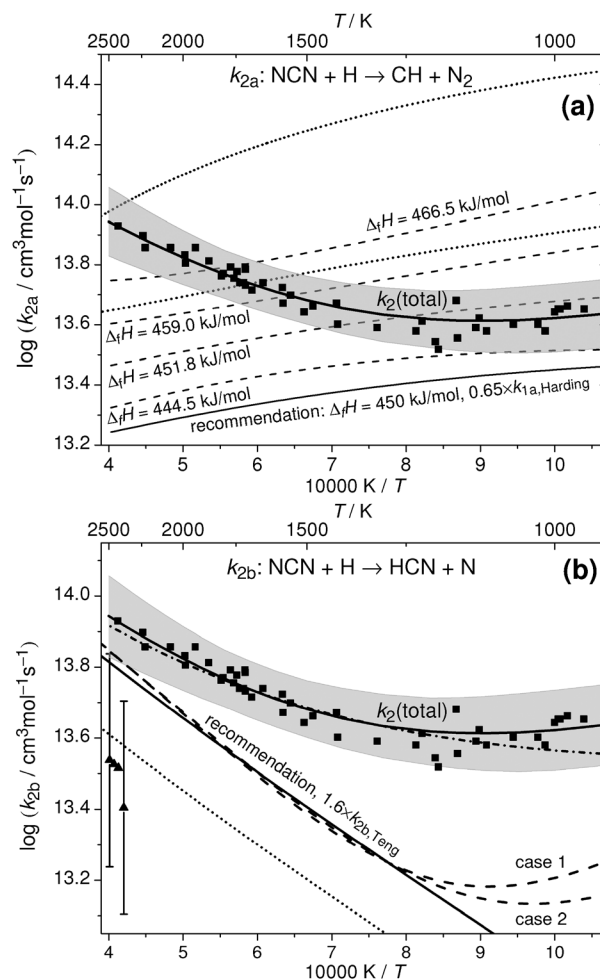
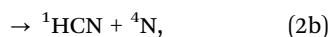
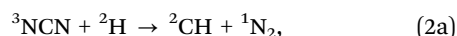


Fig. 6 Analysis of total rate constant data in terms of  $\Delta_f H_{298\text{K}}^\circ(\text{NCN})$  ( $\Delta H$  in the following). The squares, the corresponding solid curves, and the shaded areas reflect the experimental data for  $k_2$  of this work and their uncertainty limits. Upper plot a: analysis with respect to channel (2a). The upper dotted curve depicts the original expression for  $k_{2a}$  adopted from Teng *et al.*,<sup>4</sup> the lower dotted curve a re-evaluation of their data using  $\Delta H = 458 \text{ kJ mol}^{-1}$ . The dashed curves reflect  $k_{2a} = k_{1a}/K$  with  $k_{1a}$  from Harding *et al.*,<sup>3</sup> derived for different  $\Delta H$  values using eqn (II). For the lower solid curve, eqn (II) was scaled by a factor of 0.65. Lower plot b: Analysis with respect to channel (2b). Triangles with error bars and the dotted line reflect the experimental and theoretical data reported by Vasudevan *et al.*,<sup>6</sup> and Teng *et al.*,<sup>4</sup> respectively. The dashed curves depict  $k_{2b} = k_2 - k_{2a}$  expressions obtained from the  $k_2$  values of this work and  $k_{2a}$  derived from Harding *et al.*; case 1:  $k_2 \times 1.0$ ,  $k_{1a} \times 1.0$ ,  $\Delta H = 440 \text{ kJ mol}^{-1}$ ; case 2:  $k_2 \times 1.0$ ,  $k_{1a} \times 0.65$ ,  $\Delta H = 450 \text{ kJ mol}^{-1}$ . The lower solid curve reflects the recommended  $k_{2b}$  expression, which is equal to the Teng *et al.*<sup>4</sup> expression scaled by a factor of 1.6. The dash-dotted curve corresponds to  $k_2 = k_{2a} + k_{2b}$  using the two recommended rate expressions.

reaction channel (2c) yielding  $\text{HNC} + \text{N}$  exhibits high activation barriers and does not play a role. The recombination channel (2d), which dominates at room temperature and very high pressures, becomes less important with increasing temperature and can be expected to be of minor importance at combustion relevant temperatures  $T > 1000$  K as well. At a typical total pressure of  $p = 0.5$  bar used in this work, the theoretical predictions of Teng *et al.*<sup>4</sup> range channel (2d) to contribute



about 1.2% at 1000 K and 3.8% at  $T = 800$  K to the overall reaction. Due to the inconsistencies in that paper (*vide infra*) these number should be interpreted with caution, however, the order of magnitude reveals that this channel starts to play a role at the lowest experimental temperatures of this study. Nevertheless, as a good starting point, we limit our analysis of the  $k_2$  data to channels (2a) and (2b) in the following. Regarding the potential energy surface for reaction (2) from Teng *et al.*,<sup>4</sup> channel (2a) proceeds on the doublet surface over the formation of an HNCN complex and is supposed to have a slightly negative temperature dependence. In contrast, channel (2b) exhibits a small activation barrier and predominantly proceeds on a quartet surface. The kinetic calculations also reveal that both reaction channels are important at combustion temperatures.

### Analysis method a

In Fig. 6a, the upper dotted curve depicts the calculated rate expression for  $k_{2a}$  from Teng *et al.*<sup>4</sup> The very high rate constant values for  $k_{2a}$  as well as the very high total rate constants  $k_2$  (dashed curve included in Fig. 1) are unreasonable. Compared to our experimentally determined *total* rate constant values, the expression yields up to 6 times higher rate constants for channel (2a) already. Moreover, there seems to be an inconsistency in the reported rate constants for the equilibrium  $\text{CH} + \text{N}_2 \rightleftharpoons \text{NCN} + \text{H}$  in the paper of Teng *et al.* Using their values for the rate constant of the forward reaction (1a) and their preferred value for the enthalpy of formation,  $\Delta H = 458 \text{ kJ mol}^{-1}$ , we calculate reverse rate constants  $k_{2b}$ . Thermodynamic data for CH,  $\text{N}_2$ , H, and NCN were taken from Burcat's database<sup>47</sup> with updated heat capacity data for NCN from Goos *et al.*,<sup>22</sup> where 7-term NASA polynomial parameter  $a_6$  has been scaled to adjust  $\Delta H(\text{NCN})$ . Obtained  $k_{2b}$  values are 2–3 times lower than reported by Teng *et al.* (lower dotted curve in Fig. 6a). Another indication that the reported rate constants may be flawed comes from the reported total rate constant values; for example, the recommended room temperature value  $k_2 \approx 7 \times 10^{14} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$  is higher than the Lennard-Jones collision limit of  $k_{\text{LJ}} \approx (3.5\text{--}5.5) \times 10^{14} \text{ cm}^3 \text{ mol}^{-1} \text{ s}^{-1}$ , which can be estimated based on the Lennard Jones parameters reported in the literature (parameters for H:<sup>48–50</sup>  $\sigma = (2.00\text{--}3.26) \text{ \AA}$  and  $\epsilon/k_B = (2.7\text{--}145) \text{ K}$ ; parameters for NCN:<sup>48</sup>  $\sigma = 3.83 \text{ \AA}$  and  $\epsilon/k_B = 232 \text{ K}$ ).

To the best of our knowledge, no other experimental or theoretical values for  $k_{2a}$  have been reported explicitly in the literature yet. Therefore, we continue our analysis by calculating  $k_{2a}$  values from the reverse reaction  $k_{1a}$ , which has been thoroughly studied both experimentally and theoretically. For an overview of available literature data we refer to the work of Harding *et al.*<sup>3</sup> who performed high-level *ab initio* and transition state theory calculations on the reaction  $\text{CH} + \text{N}_2$  using multi-reference electronic structure methods. Using their recommended value of the enthalpy of formation,  $\Delta H = 459 \text{ kJ mol}^{-1}$ , the theoretical prediction was found to be in quantitative agreement with the most recent shock tube data of Vasudevan *et al.*<sup>6</sup> over the temperature range  $2100 \text{ K} < T < 3350 \text{ K}$ . At these high temperatures, the predicted rate constant is less dependent on the assumed value of  $\Delta H$ . Towards lower temperatures and in

the practically important temperature range of 1000–2000 K, however, an accurate enthalpy of formation is crucial. In an Arrhenius plot, Harding *et al.*<sup>3</sup> present their results of temperature dependent calculations of the rate constant of reaction (1a) assuming different values for the enthalpy of formation of NCN (Fig. 13 in their paper). For example, it was shown that changing  $\Delta H$  by  $\pm 8 \text{ kJ mol}^{-1}$  yields a factor of 1.6 higher ( $-8 \text{ kJ mol}^{-1}$ ) or 1.9 lower ( $+8 \text{ kJ mol}^{-1}$ )  $k_{1a}$  value at  $T = 1000 \text{ K}$ . In order to take this pronounced thermodynamic effect into account in our analysis and to derive rate constant estimates for  $k_{2a} = k_{1a}/K$  as function of the assumed NCN enthalpy of formation, we reparametrized the original data of Harding *et al.* and used the expression

$$k_{1a}/(\text{cm}^3 \text{ mol}^{-1} \text{ s}^{-1}) = e^{(274.5 - 0.556x)} \times (T/\text{K})^{(-31.24 + 0.0706x)} \times e^{(-71.2 \text{ kJ mol}^{-1}/RT)} \quad (\text{II})$$

with  $x = \Delta_f H_{298\text{K}}^0(\text{NCN})$  in  $\text{kJ mol}^{-1}$ . Eqn (II) provides a stable fit of the rate constant data of Harding *et al.* and yields a reasonable extrapolation to somewhat higher and lower  $\Delta_f H_{298\text{K}}^0(\text{NCN})$  values. Representative literature values of the enthalpy of formation span the range from  $444.5 \text{ kJ mol}^{-1}$  (single-reference computations)<sup>16,23</sup> to  $459 \text{ kJ mol}^{-1}$  (high-level basis set extrapolation or multi-reference computations)<sup>3,4</sup> for theoretical and from  $451.8 \text{ kJ mol}^{-1}$  (electron affinity of NCN)<sup>51</sup> to  $466.5 \text{ kJ mol}^{-1}$  (NCN photodissociation)<sup>24</sup> for experimental literature data. The resulting  $k_{2a}$  expressions are shown as dashed curves in Fig. 6a. They reveal a weak and negative temperature dependence of the reaction  $\text{NCN} + \text{H} \rightarrow \text{CH} + \text{N}_2$  with the absolute rate constant values basically offset by the assumed enthalpy of formation of NCN. Clearly, the higher enthalpies of formation yield unfeasible  $k_{2a}$  values that are up to a factor of 2.4 higher than the total rate constant measured in this work. Assuming that (i) the branching fraction  $k_{2a}/k_2 = 1$  around  $T = 1000 \text{ K}$ , (ii)  $k_{1a}$  from Harding *et al.* is correct, and (iii)  $k_2$  is at the upper limit of the uncertainty range of our experimental data ( $+30\%$ ), an upper limit of  $\Delta H < 454 \text{ kJ mol}^{-1}$  can be estimated from this analysis.

### Analysis method b

A second analysis of our data focusing on the rate constant of channel (2b) is shown in Fig. 6b. The indirect experimental data of Vasudevan *et al.*<sup>6</sup> (triangles with error bars) and the most recent theoretical estimate of Teng *et al.*<sup>4</sup> (dotted curve) are shown as well. In the light of the negative temperature dependence of channel (2a) it becomes clear that the experimentally determined positive temperature dependence of  $k_2$  towards higher temperatures arises from the increasingly dominant activation controlled channel (2b). Moreover, the high temperature activation energy  $E_a = 33 \text{ kJ mol}^{-1}$  estimated from the two channel fit of our experimental data (see Fig. 5 and eqn (I)) is in very good agreement with the theoretically predicted activation energies of  $35 \text{ kJ mol}^{-1}$  and  $28 \text{ kJ mol}^{-1}$  reported by the M. C. Lin group<sup>2,4</sup> (see Fig. 1 and 6b). Hence, we consider the activation energy of reaction channel (2b) a well-constrained quantity with a preferred value of  $E_a \approx 28 \text{ kJ mol}^{-1}$  adopted from the most recent *ab initio* study.<sup>4</sup> Having the temperature





**Table 3** Feasible values of  $\Delta_f H_{298K}^0(\text{NCN})$  for different combinations of  $k_{1a}$  and  $k_2$  values. The reported enthalpy values in  $\text{kJ mol}^{-1}$  yield activation energies  $E_{a,2a} \approx 28 \text{ kJ mol}^{-1}$  for reaction channel (2a) that are consistent with the corresponding theoretical estimate of Teng *et al.*<sup>4</sup>

$\Delta_f H_{298K}^0(\text{NCN})$	$k_2 + 30\%$	$k_2$	$k_2 - 30\%$
$k_{1a} + 35\%$	436	430	423
$k_{1a}$	445	440	432
$k_{1a} - 35\%$	456	450	443

dependence of  $k_{2b}$  fixed, it is possible to arrive at a consistent value for the enthalpy of formation. Here,  $\Delta H$  has been chosen in a way such that the rate constant expression for  $k_{2b} = k_2 - k_{2a}$ , with  $k_2$  values taken from eqn (I) of this work and  $k_{2a}$  values calculated *via* thermodynamic equilibrium from the  $k_{1a}$  expression eqn (II), yields a temperature dependence that is consistent with  $28 \text{ kJ mol}^{-1}$ . A matrix of appropriate enthalpy of formations with  $k_2$  and  $k_{1a}$  varied within their uncertainty limits is given in Table 3. Here, uncertainties of  $k_2 \pm 30\%$  as obtained in this work and  $k_{1a} \pm 35\%$  as reported for the experimental shock tube results of Vasudevan *et al.*<sup>6</sup> (which are in turn consistent with the  $k_{1a}$  expression of Harding *et al.*) have been assumed. Table 3 reveals a large range of possible enthalpy of formations,  $423 \text{ kJ mol}^{-1} < \Delta H < 456 \text{ kJ mol}^{-1}$ . Nevertheless, two conclusions can be drawn from this analysis. First, increasing  $k_{1a}$  yields unfeasible enthalpy values that are even well below the results of the single-reference computations (about  $444.5 \text{ kJ mol}^{-1}$ ), which can be regarded a reasonable lower limit for  $\Delta H$ . Even with  $k_{1a}$  unchanged, the highest value of  $445 \text{ kJ mol}^{-1}$  would be close to this limit. Secondly, the upper limit of  $456 \text{ kJ mol}^{-1}$ , corresponding to a scenario with  $k_2 + 30\%$  and  $k_{1a} - 35\%$ , is in agreement with the upper limit of  $454 \text{ kJ mol}^{-1}$  inferred from analysis method a. Therefore, the high experimental value of Bise *et al.*<sup>24</sup> ( $466.5 \pm 2.9 \text{ kJ mol}^{-1}$ ), the results of the high-level basis set extrapolation and multi-reference computations (about  $459 \text{ kJ mol}^{-1}$ ),<sup>3,4</sup> and the most recent recommendation of the Active Thermochemical Tables as cited in Goos *et al.*<sup>22</sup> ( $457.8 \pm 2$ ) are hardly compatible with this work.

Resulting  $k_{2b}$  expressions are illustrated in Fig. 6b for two selected cases. Case 1, assuming that both  $k_2$  and  $k_{1a}$  exhibit values as given by eqn (I) and (II), yields  $\Delta H = 440 \text{ kJ mol}^{-1}$ . Case 2, assuming  $k_2$  from eqn (I) and  $k_{1a}$  from eqn (II) scaled by a factor of 0.65, yields  $\Delta H = 450 \text{ kJ mol}^{-1}$ . For all other cases outlined in Table 3, similar  $k_{2b}$  curves have been obtained, of course somewhat offset for different assumed  $k_{1a}$  values (not shown). It is obvious from Fig. 6b that the calculated  $k_{2b}$  expressions deviate from linearity at temperatures below 1250 K. With decreasing temperatures and hence a decreasing contribution of  $k_{2b}$ , the analysis procedure gets less reliable, hence, part of this deviation may be attributed to inaccuracies of the analysis method itself. However, it may also indicate the onset of the low temperature reaction channel (2d), which has been neglected in the analysis. In this sense, the increase of  $k_{2b}$  at low temperatures would simply arise from the neglected contributions of this channel.

Overall, relying on the direct  $k_2$  determination of this work, an enthalpy value of  $450 \text{ kJ mol}^{-1}$  is most consistent with both

the enthalpy limits set by the single-reference computations and our analysis,  $444.5 \text{ kJ mol}^{-1} < \Delta_f H_{298K}^0(\text{NCN}) < 454 \text{ kJ mol}^{-1}$ , the experimental and theoretical values for  $k_{1a}$  from Vasudevan *et al.*<sup>6</sup> and Harding *et al.*,<sup>3</sup> the activation energy of reaction channel (2b) reported by Teng *et al.*,<sup>4</sup> and the indirect shock tube measurements for  $k_{2b}$  from Vasudevan *et al.*<sup>6</sup> This enthalpy value is also in very good agreement with the experimental electron affinity measurements of Clifford *et al.*<sup>51</sup> ( $451.8 \pm 16.7 \text{ kJ mol}^{-1}$ ) that has been, for example, used in the GDFkin3.0\_NCN flame modelling mechanism as well.<sup>8</sup>

Using  $\Delta H = 450 \text{ kJ mol}^{-1}$ , the recommended rate constant expressions for  $k_{1a}$ ,  $k_{2a}$ , and  $k_{2b}$  are as follows: compatible with the lower experimental uncertainty limit of Vasudevan *et al.*,  $k_{1a}$  is set to 0.65 times the values of Harding *et al.* (eqn (II)):

$$k_{1a}/(\text{cm}^3 \text{ mol}^{-1} \text{ s}^{-1}) = 2.3 \times 10^{10} \times (T/\text{K})^{0.53} \times \exp(-71.2 \text{ kJ mol}^{-1}/RT)$$

Using the updated NASA polynomial parameters for NCN from Goos *et al.*<sup>22</sup> (scaled to  $\Delta H = 450 \text{ kJ mol}^{-1}$ ), this corresponds to a reverse reaction rate constant  $k_{2a}$  of

$$k_{2a}/(\text{cm}^3 \text{ mol}^{-1} \text{ s}^{-1}) = 4.2 \times 10^{15} \times (T/\text{K})^{-0.69} \times \exp(-2.0 \text{ kJ mol}^{-1}/RT)$$

Adopting the temperature dependence of Teng *et al.*, their rate expression is recommended for  $k_{2b}$  adjusted by a factor of 1.6 to fit the case 2 data in Fig. 6b:

$$k_{2b}/(\text{cm}^3 \text{ mol}^{-1} \text{ s}^{-1}) = 7.94 \times 10^{12} \times (T/\text{K})^{0.41} \times \exp(-22.8 \text{ kJ mol}^{-1}/RT)$$

This expression is also compatible with the upper limit of the indirect shock tube measurements of Vasudevan *et al.*<sup>6</sup>

Finally, the sum of  $k_{2a}$  and  $k_{2b}$  is shown in Fig. 6b as dash-dotted curve. It is in close agreement with the  $k_2$  rate expression given by eqn (I), except at the lowest temperatures where channel  $k_{2d}$  presumably starts to play a role. The recommended rate expression for  $k_{2b}$  corresponds to a branching ratio  $\phi = k_{2b}/k_2$  that increases from  $\phi = 0.21$  at  $T = 1000 \text{ K}$  to  $\phi = 0.74$  at  $T = 2500 \text{ K}$ . Hence, in the temperature range relevant for flame modelling, channel switching between channel (2a) dominating at low temperatures and channel (2b) dominating at high temperatures takes place.

## 5 Concluding remarks

The overall rate constant of the reaction  $\text{NCN} + \text{H}$  has been directly measured at temperatures between 962 K and 2425 K behind shock waves using the thermal decomposition of  $\text{NCN}_3$  and  $\text{C}_2\text{H}_5\text{I}$  as suitable precursors for NCN radicals and H atoms, respectively. A conservative error analysis revealed that comparatively narrow error limits of  $\pm 20\%$  at  $T = 1600 \text{ K}$ , increasing to  $\pm 30\%$  at the upper and lower temperature limits of the measurements, could be achieved. A main error arises from the possibly large uncertainty of the potentially important secondary reaction (10),  $\text{NCN} + \text{N}$ , which has not been measured yet.



If the theoretical estimate of Moskaleva and Lin<sup>2</sup> turns out to be right, the influence of reaction (10) would be very small and the error estimate could be further reduced. The second most important uncertainty is related to the assumed overall H atom yield from C<sub>2</sub>H<sub>5</sub>I decomposition. However, relying on the very recently published global analysis data on the ethyl iodide composition by Varga *et al.*,<sup>39</sup> this error contribution could be safely assumed to be not more than 7% (an error estimate of 3.5% at  $T = 1200$  K has been stated in the original paper).

The high reliability of the rate constant data enabled us to analyze the  $k_2$  data in terms of branching ratio and the crucial value of the enthalpy of formation of NCN. Taking into account experimental and theoretical literature data for the rate constant of reaction (1a) and the temperature dependence of reaction channel (2b),  $\Delta_f H_{298K}^0 = 450$  kJ mol<sup>-1</sup> was found to be most consistent. With a robust upper limit of  $\Delta_f H_{298K}^0 < 456$  kJ mol<sup>-1</sup> derived from the  $k_2$  values of this work, significantly higher literature values – about 459 kJ mol<sup>-1</sup> from high-level *ab initio* calculations<sup>3,4</sup> and 466.5 kJ mol<sup>-1</sup> from NCN photodissociation experiments<sup>24</sup> – are at odds with our analysis. Clearly, more work is needed to further constrain the uncertainty of the enthalpy of formation of NCN.

Modelling of NO<sub>x</sub> formation in flames critically depends on the branching ratio of the reaction NCN + H. Whereas channel (2a) constitutes the reverse reaction of the main prompt-NO formation reaction (1a), CH + N<sub>2</sub>, it is in particular reaction channel (2b) with the products HCN + N that brings the overall reaction forward on the prompt-NO pathway. The results of this study with branching fractions  $\phi = k_{2b}/k_2$  increasing from  $\phi(T = 1000 \text{ K}) = 0.21$  to  $\phi(T = 2500 \text{ K}) = 0.74$  verifies the expected strong temperature dependence of this quantity. However, again the actual value of the derived branching ratio strongly depends on the assumed value of the enthalpy of formation of NCN. In fact, accurate measurements of the branching ratio would be very useful to constrain the enthalpy of formation of NCN. Moreover, in conjunction with the already compiled theoretical and experimental rate constant data, accurate branching fractions would help to draw final conclusions on this reaction system including the contributions of the recombination channel (2d), which may play a role even at temperatures as high as 1000 K.

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