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# Bonding and spectroscopic properties of complexes of SO<sub>2</sub>–O<sub>2</sub> and SO<sub>2</sub>–N<sub>2</sub> and its atmospheric consequences

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van der Waals complexes of sulfur dioxide (SO<sub>2</sub>) with oxygen (O<sub>2</sub>) and nitrogen (N<sub>2</sub>) have been investigated by using MP2 and aug-cc-pVXZ (X = D, T) basis set. Two minimum structures with symmetry C<sub>1</sub> and C<sub>s</sub> have been located at the intermolecular potential energy surface (IPES) of the complex of SO<sub>2</sub>–O<sub>2</sub>. Stacked C<sub>s</sub> structure of SO<sub>2</sub>–O<sub>2</sub> is found to have greater stability than C<sub>1</sub> structure. In the case of SO<sub>2</sub>–N<sub>2</sub>, one minimum structure with C<sub>s</sub> symmetry has been characterized. In this study, CCSD(T)/aug-cc-pVTZ//MP2/aug-cc-pVTZ and interaction energy calculation at complete basis set (CBS) limit has been employed for better energetic description. The natural bond orbital (NBO) calculation demonstrates the bonding in terms of charge transfer from X-atom lone pair of X<sub>2</sub> (X = O or N) to the antibonding SO orbital of SO<sub>2</sub>. The strength of various intra and inter bonds in the complexes were calculated in terms of electron density at bond critical points (BCP) using quantum theory of atoms in molecules (QTAIM). Frequency calculations for these complexes show a number of interactions induced by low frequency modes in the far IR region. Symmetry adapted calculation were also computed for the complexes and is established that the ratio of dispersion to induction effect is large for the most stable conformers. The atmospheric implications are also discussed for these complexes.

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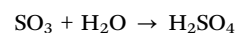
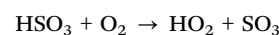
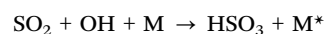
## 1. Introduction

In atmosphere sulphur dioxide (SO<sub>2</sub>) is known to form a wide range of weakly bound van der Waals (vdW) complexes which have been categorized and discussed according to the role of SO<sub>2</sub> in complex formation.<sup>1</sup> Studies regarding weak complexes of SO<sub>2</sub> are the topic of several theoretical and experimental investigations.<sup>1–6</sup> The explication of the structure, stability and bonding in these complexes has been a challenge for both theoretical and experimental chemists.<sup>2</sup>

One of the important steps in any chemical reaction is molecular recognition and weak interacting forces. The characterization of binding forces, equilibrium structures and stabilities at the intermolecular levels are necessary to have a complete knowledge of the intermolecular potential energy surface (IPES).<sup>7–9</sup> Detailed theoretical analysis of IPES of the weakly bound vdW complexes is important and helpful in elucidating the bulk properties of molecules at different phase.<sup>10</sup> Studies regarding the stabilizing forces present in these intermolecular complexes are essential from all chemistry, physics and biological point of view. Extracting useful information from vdW complexes having large-amplitude and highly coupled

motions at the intermolecular states are complicated. Indeed, theoretical descriptions are necessary for obtaining a complete picture regarding the binding forces in these complexes. Electronic structures determined by theoretical methods aid experimentalists in assigning their spectra.

Sulfur containing compounds play an important role in the atmospheric chemistry.<sup>11</sup> These compounds are of interest due to their role in atmospheric aerosol formation. One of the major atmospheric pollutants is SO<sub>2</sub>. Due to its reactive nature, it takes part in the formation of various organic, inorganic compounds and aerosol particles.<sup>12</sup> SO<sub>2</sub> is found to be the major contributor to acid rain.<sup>6,13</sup> The atmospheric oxidation of SO<sub>2</sub> proceeds in presence of the carrier gas M like O<sub>2</sub>, N<sub>2</sub> or H<sub>2</sub>O<sup>14,15</sup> to form HSO<sub>3</sub> which in turn forms the aerosol particles of sulfuric acid (H<sub>2</sub>SO<sub>4</sub>) via the formation of sulfur trioxide (SO<sub>3</sub>) by the following mechanism.<sup>16,17</sup>



Another important pathway of formation of SO<sub>3</sub> is the reaction of photoexcited SO<sub>2</sub> with O<sub>2</sub>.<sup>18</sup> In presence of O<sub>2</sub>, oxidation of SH radical in atmosphere leads to the formation of SO<sub>2</sub>.<sup>19</sup>

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The most abundant gas molecule in atmosphere is nitrogen,  $N_2$ , and indeed, there is a possibility of complex formation between  $N_2$  and  $SO_2$ , which may affect the reactivity of  $SO_2$ . In the atmosphere, molecular oxygen ( $O_2$ ) is recognized as the primary absorber in the UV-range.<sup>20</sup> There are a number of studies on the complex formation of  $O_2$  which significantly contribute to the solar absorption.<sup>21–24</sup>  $SO_2$  is a strong solar radiation absorber in the UV-range which leads to the average heating rate of 1 K per day.<sup>25,26</sup> So, the complexes of  $SO_2$  with  $O_2$  and  $N_2$  are expected to alter the radiative balance and hence are important. Indeed, a thorough knowledge of the theoretical study of the  $SO_2$ - $O_2$  and  $SO_2$ - $N_2$  complex formation is essential.

In this study, *ab initio* methods have been employed to predict the equilibrium geometries and IPES of the ground state of  $SO_2$ - $O_2$  and  $SO_2$ - $N_2$  complexes. The total energy contributions in these complexes may be sub-divided into electrostatic, exchange, induction and dispersion energies. Symmetry adapted calculations were performed to analyze these individual energy components and thus, the nature of interaction may be identified. To the best of our knowledge, no theoretical or experimental studies on  $SO_2$ - $O_2$  complex are known. The equilibrium structure of  $SO_2$ - $N_2$  complex has been established using molecular beam electric resonance spectroscopy<sup>27</sup> and by microwave technique,<sup>28</sup> these results are compared and discussed with our theoretical findings.

## 2. Computational methods

The IPES of the complexes has been explored using perturbation theory. The supermolecular interaction energies were calculated with complete basis set (CBS) limit. Symmetry adapted calculation is performed to define the various physical forces responsible in formation of these complexes.

### 2.1. Geometry optimization and supermolecular interaction energy calculation

All geometry optimization of the monomers and 1 : 1 weak vdW complexes of  $SO_2$ - $O_2$ ,  $SO_2$ - $N_2$  were performed using second-order Møller-Plesset (MP2) perturbation theory and Dunning's augmented correlation-consistent polarized valence double and triple zeta (aug-cc-pVXZ, X = D, T) basis sets. In our systems, correlation energies are likely to play an important role in interaction, so to include the correlation energies, augmented basis sets with diffuse functions have been implemented.<sup>29,30</sup> This level of theory has been shown to produce reliable structural parameters in cases of weakly bound complexes.<sup>30–33</sup> The same level of theory was used for harmonic frequency calculations to ensure if the optimized structures are true minimum. For better energetic description, single point energy calculation at coupled cluster method with single and double excitations and perturbative triples (CCSD(T)) and aug-cc-pVTZ basis set on MP2/aug-cc-pVTZ optimized structures were performed. CCSD(T) has been examined to provide reliable energy for weak vdW complex which are comparable with experimental results.<sup>34,35</sup>

The supermolecular interaction energies of the weak vdW complexes in this study are assumed to be small and the basis set superposition error (BSSE)<sup>36</sup> associated with these complexes are important. Therefore, in this study BSSE is considered and is corrected with the full counterpoise correction (CP) procedure of Boys and Bernardi.<sup>37</sup> All zero point corrected binding energies ( $D_0$ ) and BSSE-corrected binding energies ( $D_e$ ) of the complexes are given in Table 3.

### 2.2. Complete basis set (CBS) extrapolation energies

The CBS extrapolation technique is used to estimate the energies of the  $SO_2$ - $O_2$ ,  $SO_2$ - $N_2$  complexes, the monomers and predict the equilibrium structure of these complexes. CBS method is less expensive and is found to be efficient in yielding accurate interaction energies.<sup>33</sup> The different extrapolation models for calculating CBS energies show no significant difference amongst them.<sup>30,33</sup> In this work, CBS extrapolation is performed using the model proposed by Helgaker<sup>38,39</sup> with a series of correlation-consistent basis sets. This formula is found to have numerous applications and the generalized form is given by,

$$E(X) = E_{\text{CBS}} + A(X - B)^{-\alpha} \quad (1)$$

Here  $E(X)$  is the interaction energy,  $E_{\text{CBS}}$  is CBS energy limit,  $X$  is an integer with values 2, 3, 4, and 5 for aug-cc-pVXZ basis sets and  $A$ ,  $B$ ,  $\alpha$  are fitting parameters. Jeziorska *et al.*<sup>40</sup> showed the most appropriate CBS interaction calculation is when  $B = 0$  and  $\alpha = 3$ . In the above relation to obtain CBS energy limit,  $B = 0$  and  $\alpha = 3$  is used. The CBS calculations were performed with MP2 method and aug-cc-pVXZ (X = D, T, Q, and 5) basis sets on the MP2/aug-cc-pVTZ optimized geometries. CBS extrapolation using eqn (1) with a series of correlation-consistent polarized valence basis set has been successfully used for binding energy calculation of weak vdWs complexes.<sup>41,42</sup> In ref. 41 and 42, the authors have found that the interaction energy calculated with CBS method is comparable with the higher computationally reliable methods. All MP2 single point energy calculations are BSSE corrected. The CBS binding energies of the complexes is compared with other supermolecular interaction energies.

All the above calculations were performed with Gaussian09 software.<sup>43</sup> GaussView 5.0.9 software<sup>44</sup> was used for the visualization of molecular structures and vibrational motions.

### 2.3. Symmetry-adapted perturbation theory (SAPT) calculation

SAPT provides the interaction energy calculation for weakly bound intermolecular complexes. This approach partitions the total interaction energy into physically definable components and is free from basis set superposition error. In SAPT calculation, the total interaction energy is decomposed into electrostatic ( $E_{\text{elst}}$ ), exchange ( $E_{\text{exch}}$ ), dispersion ( $E_{\text{disp}}$ ) and induction ( $E_{\text{ind}}$ ) energies. The SAPT interaction energy,  $E_{\text{int}}^{\text{SAPT}}$  as perturbative series is given by

$$E_{\text{int}}^{\text{SAPT}} = \sum_{n=1}^{\infty} \sum_{j=0}^{\infty} \left( E_{\text{pol}}^{(nj)} + E_{\text{exch}}^{(nj)} \right) \quad (2)$$



where,  $n$  is the order of intermolecular interaction operator and  $j$  denotes the order of Møller–Plesset fluctuation operator. Polarization energy  $E_{\text{pol}}^{nj}$  is obtained from Rayleigh–Schrodinger perturbation theory and exchange energy  $E_{\text{exch}}^{nj}$  results from the anti-symmetrization that is the symmetric adaptation of the dimer wave function.

In this study, three different levels of SAPT interaction energies SAPT0, SAPT2 and SAPT have been calculated, which are defined as

$$E_{\text{int}}^{\text{SAPT0}} = E_{\text{elst}}^{(10)} + E_{\text{exch}}^{(10)} + E_{\text{ind,resp}}^{(20)} + E_{\text{exch-ind,resp}}^{(20)} + E_{\text{disp}}^{(20)} + E_{\text{exch-disp}}^{(20)} + \delta E_{\text{int,resp}}^{(\text{HF})} \quad (3)$$

$$E_{\text{int}}^{\text{SAPT2}} = E_{\text{int}}^{\text{SAPT0}} + E_{\text{elst,resp}}^{(12)} + E_{\text{exch}}^{(11)} + E_{\text{exch}}^{(12)} + E_{\text{ind}}^{(22)} + E_{\text{exch-ind}}^{(22)} \quad (4)$$

$$E_{\text{int}}^{\text{SAPT}} = E_{\text{int}}^{\text{SAPT2}} + E_{\text{elst,resp}}^{(13)} + e_{\text{exch}}^{(1)}(\text{CCSD}) - (E_{\text{exch}}^{(11)} + E_{\text{exch}}^{(12)}) + E_{\text{disp}}^{(21)} + E_{\text{disp}}^{(22)} \quad (5)$$

where,  $E_{\text{int}}^{(\text{HF})} = E_{\text{elst}}^{(10)} + E_{\text{exch}}^{(10)} + E_{\text{ind,resp}}^{(20)} + E_{\text{exch-ind,resp}}^{(20)} + \delta E_{\text{int,resp}}^{(\text{HF})}$  is supermolecular HF interaction energy and the rest are the correlation interaction energies.

In above equations  $E_{\text{elst}}^{(ij)}$  represents the classical electrostatic energy.  $E_{\text{exch}}$ ,  $E_{\text{disp}}$ ,  $E_{\text{ind}}$  are repulsive-exchange, dispersion and induction energies respectively of different order. The induction energy is caused by the interaction of permanent multipole moment of one monomer and induced moment of other monomer whereas dispersion energy results from the correlation of the electron motion in the two monomers. The  $E_{\text{ind}}^{(22)}$  is part of  $E_{\text{ind}}^{(22)}$  not included in  $E_{\text{ind,resp}}^{(20)}$ . The  $E_{\text{exch-ind}}^{(22)}$  term is the estimated exchange counterpart of  $E_{\text{ind}}^{(22)}$ .  $\delta E_{\text{int,resp}}^{(\text{HF})}$  term accounts for the third and higher order induction and exchange-induction energy contribution. 'resp' subscript implies the inclusion of the coupled perturbed HF response. SAPT0 lacks the intramolecular correlation effect and the interaction energy SAPT2 includes intramolecular correlation.

All the SAPT calculations were performed using SAPT2012.2 program<sup>45</sup> and for the integral calculation, GAMESS<sup>46</sup> has been used. The basis sets used for SAPT calculation are cc-pVDZ, aug-cc-pVDZ and aug-cc-pVTZ and are denoted by VDZ, AVDZ and AVTZ respectively. It is expected that in the weakly bound systems of our studies, the interaction energies mainly arise from the induction and dispersion effect. For better description of the different interaction energy terms, the total SAPT energy is decomposed into four main terms as follows:

$$E_{\text{elst}} = E_{\text{elst}}^{(10)} + E_{\text{elst,resp}}^{(12)} + E_{\text{elst,resp}}^{(13)} \quad (6)$$

$$E_{\text{exch}} = E_{\text{exch}}^{(10)} + E_{\text{exch-ind,resp}}^{(20)} + E_{\text{exch-disp}}^{(20)} + e_{\text{exch}}^{(1)}(\text{CCSD}) \quad (7)$$

$$E_{\text{ind}} = E_{\text{ind,resp}}^{(20)} + E_{\text{ind}}^{(22)} \quad (8)$$

$$E_{\text{disp}} = E_{\text{disp}}^{(20)} + E_{\text{disp}}^{(21)} + E_{\text{disp}}^{(22)} \quad (9)$$

Thus

$$E_{\text{int}}^{\text{SAPT}} = E_{\text{elst}} + E_{\text{exch}} + E_{\text{ind}} + E_{\text{disp}} + \delta E_{\text{int,resp}}^{(\text{HF})} \quad (10)$$

Atom-pair wise additive density functional dispersion correction (DFT-D3)<sup>47</sup> is found to have chemical accuracy in

evaluating the dispersion interaction present in weak vdW complexes with the inclusion of standard Becke and Johnson (BJ) damping function.<sup>48</sup> It is due to the inability of standard DFT calculations to correctly cover the long-range London dispersion interactions. The general expression of the corrected dispersion energy,  $E_{\text{disp}}$  is given by

$$E_{\text{disp}} = -\frac{1}{2} \sum_{A \neq B} \sum_{n=6,8,\dots} s_n \frac{C_n^{\text{AB}}}{R_{\text{AB}}^n} f_{\text{damp}}(R_{\text{AB}}) \quad (11)$$

Here,  $C_n^{\text{AB}}$  is the averaged  $n$ th-order dispersion coefficient for atom pair AB,  $R_{\text{AB}}$  is the internuclear distance between A and B,  $s_n$  is a functional-dependent scaling factor and  $f_{\text{damp}}$  is the BJ-damping function.

In this study, dispersion energy correction,  $E_{\text{disp}}$  with BJ-damping function has been performed with Grimme's code<sup>49</sup> of DFT-D3 Ver. 3.0 Rev 0 for B3LYP,<sup>50,51</sup> TPSS<sup>52</sup> and PBE<sup>53</sup> functionals. The corresponding standard DFT calculations,  $E_{\text{DFT}}$  with aug-cc-pVTZ basis set were performed as implemented in Gaussian09 software. The contribution of dispersion correction,  $E_{\text{disp}}$  which is missing from  $E_{\text{DFT}}$  is added to  $E_{\text{DFT}}$  to have the total DFT-D3 energies,  $E_{\text{DFT-D3}}$ . These single point energy calculations of  $E_{\text{disp}}$  and  $E_{\text{DFT}}$  have been performed on the MP2/aug-cc-pVTZ optimized structures to obtain the DFT-D3 energies,  $E_{\text{DFT-D3}}$ . The dispersion corrected interaction energies,  $E_{\text{int}}(\text{DFT-D3})$  of the complexes are given in Table 4. All these energies are CP-corrected.

## 2.4. Natural bond orbital (NBO) and atoms in molecules (AIM) analysis

The structural and bonding features of the 1:1 intermolecular complexes,  $\text{SO}_2\text{-O}_2$  and  $\text{SO}_2\text{-N}_2$  have been investigated by using the NBO<sup>54–58</sup> theory. The calculations of the NBO analysis have been performed with the use of MP2/aug-cc-pVTZ on the optimized geometries at the same level of theory. The atoms in molecules (AIM) approach has been applied to analyze the topological properties of the electronic charge density at MP2/aug-cc-pVTZ using the AIMALL suite of program.<sup>59</sup> The input wave functions for AIM calculations were created from the Gaussian software.

## 3. Results and discussions

### 3.1. Optimized geometries

The monomers and complex structures optimized at MP2 method and aug-cc-pVXZ (X = D, T) basis sets are shown in Fig. 1. The representative geometric parameters are given in Table 1. In the case of  $\text{SO}_2\text{-O}_2$  complex, two minimum structures have been found. One of the minima is the stacked  $C_1$  (**1a**) and the other minima is **1b**, which belongs to  $C_s$  point group. A nearly T-shaped equilibrium structure for  $\text{SO}_2\text{-N}_2$  (minima **2a**) corresponding to  $C_s$  symmetry has been found at all level of theories. In the three vdW complexes of  $\text{SO}_2$  (**1a**, **1b**, **2a**),  $\text{SO}_2$  is oriented in such a way that its oxygen atoms are straddling the  $\text{O}_2$  or  $\text{N}_2$  monomer. Structure **1a** and **1b** differ in the orientation of the O3–O4 unit.  $\text{O}_2$  monomer is parallel to the molecular



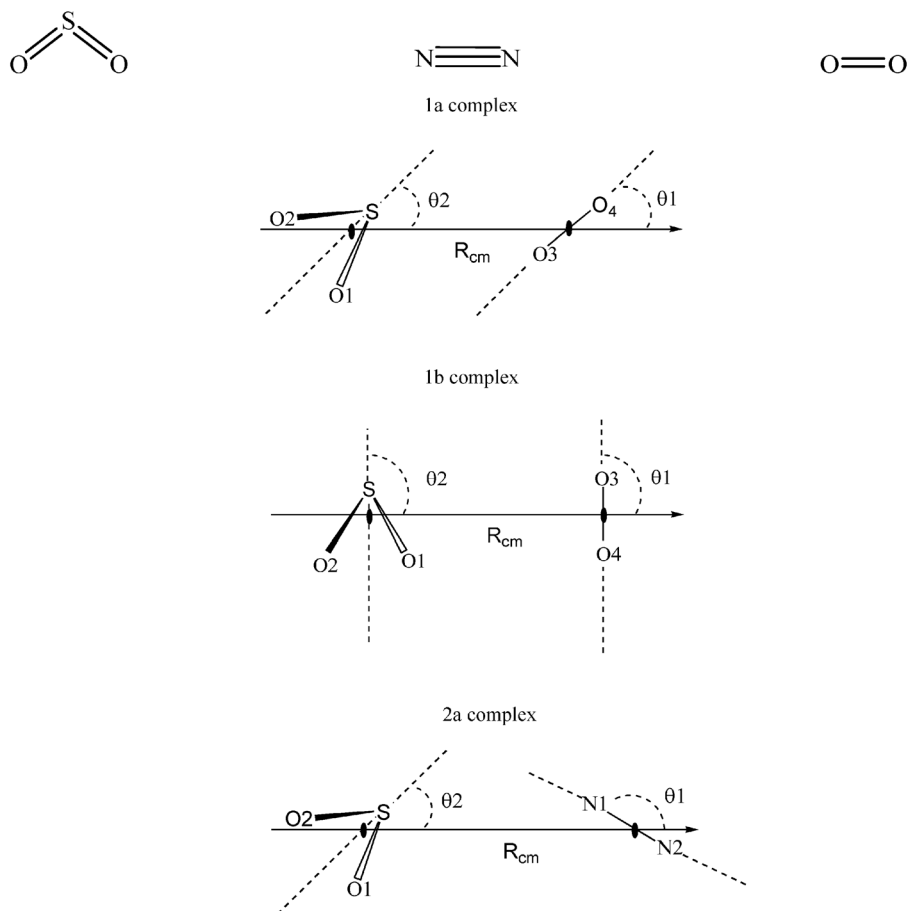


Fig. 1 Structures of SO<sub>2</sub>, O<sub>2</sub>, N<sub>2</sub> and vdW complexes **1a**, **1b** and **2a** computed at MP2 level with aug-cc-pVXZ (X = D, T). Structural parameters  $\theta_1$ ,  $\theta_2$  and  $R_{cm}$  are given in Table 1.

Table 1 MP2 optimized geometrical parameters of the monomers and minimized structures of the SO<sub>2</sub>–O<sub>2</sub>, SO<sub>2</sub>–N<sub>2</sub> at aug-cc-pVTZ and available experimental results. aug-cc-pVDZ values are given in the bracket<sup>a</sup>

Parameters	MP2/aug-cc-pVTZ(MP2/aug-cc-pVDZ)				Experiment	
	Monomer	1a	1b	2a	Monomer	2a
N–N	1.12(1.13)	—	—	1.12(1.13)	1.10 <sup>b</sup>	—
O–O	1.25(1.26)	1.25(1.26)	1.25(1.26)	—	1.21 <sup>b</sup>	—
S–O	1.46(1.51)	1.46(1.51)	1.46(1.51)	1.46(1.51)	1.43 <sup>c</sup>	—
$\angle$ OSO	118.8(118.1)	118.6(117.9)	118.6(118.0)	118.7(118.0)	119.5 <sup>c</sup>	—
$R_{cm}$	—	3.44(3.49)	3.07(3.17)	3.74(3.83)	—	3.89 <sup>d</sup>
$\theta_1$	—	70.6(72.3)	88.3(86.5)	147.6(148.0)	—	155.5 <sup>d</sup>
$\theta_2$	—	68.8(68.5)	91.5(88.0)	94.3(93.4)	—	94.8 <sup>d</sup>

<sup>a</sup> Bond lengths are in angstrom (Å) and angles are in degrees. <sup>b</sup> Experimental data are taken from ref. 70. <sup>c</sup> Experimental data are taken from ref. 71. <sup>d</sup> Experimental data taken from ref. 27.

symmetry plane of SO<sub>2</sub>, where one of O-atom of O<sub>2</sub> molecule sits above the S-atom of SO<sub>2</sub> monomer and other O-atom of O<sub>2</sub> monomer is away of SO<sub>2</sub> bond angle in **1a** and towards the bond angle in **1b**. The arrangement of the atoms of the constituent monomers in *C<sub>s</sub>* structure of **2a** is similar to structure **1b**. In the case of SO<sub>2</sub>–N<sub>2</sub> complex, molecular *C<sub>x</sub>*-axis of N<sub>2</sub> monomer is tilted by an angle from 90° making almost T-shaped structure. The rotational constants, dipole moment and nitrogen quadrupole coupling constants of the

monomers and complexes computed with MP2/aug-cc-pVXZ (X = D, T) are given in Table 2.

The calculations for the monomers have also been performed to assess reliability of the computational methods adopted in this study. A comparison of ground state experimental values with theoretical results for the monomers is summarized in Table 1. It can be observed that the error associated with the bond length is within 0.04 Å and angle is 0.9° at MP2/aug-cc-pVTZ level. It indicates that the theoretical method used in this



**Table 2** The rotational constants (MHz) and dipole moment (in Debye) of the complexes of  $\text{SO}_2\text{-O}_2$  and  $\text{SO}_2\text{-N}_2$  and monomers at MP2/aug-cc-pVXZ (X = D, T) and nuclear quadrupole moment,  $eQq_{\text{cc}}$  (MHz) of  $\text{SO}_2\text{-N}_2$  complex at MP2/aug-cc-pVTZ

Species	Basis set	Rotational constants (MHz)			Dipole moment (D)	$eQq_{\text{cc}}$ (MHz)
		A	B	C		
$\text{N}_2$	aug-cc-pVDZ	—	56 353	—	—	
	aug-cc-pVTZ	—	58 155(59 906) <sup>a</sup>	—	—	
$\text{O}_2$	aug-cc-pVDZ	—	39 816	—	—	
	aug-cc-pVTZ	—	40 469(43 100) <sup>a</sup>	—	—	
$\text{SO}_2$	aug-cc-pVDZ	52 743	9476	8033	1.737	
	aug-cc-pVTZ	56 928(60 778) <sup>b</sup>	9956(10 318) <sup>b</sup>	8474(8799) <sup>b</sup>	1.630(1.630) <sup>b</sup>	
<b>1a</b>	aug-cc-pVDZ	7426	1896	1674	1.689	
	aug-cc-pVTZ	7870	1956	1727	1.692	
<b>1b</b>	aug-cc-pVDZ	6697	2121	1877	1.692	
	aug-cc-pVTZ	7040	2232	1975	1.577	1.27( <sup>14</sup> N <sub>1</sub> ) 1.30( <sup>14</sup> N <sub>2</sub> )
<b>2a</b>	aug-cc-pVDZ	7853	1629	1434	1.704	(1.30) <sup>c</sup>
	aug-cc-pVTZ	8278(8832) <sup>c</sup>	1703(1617) <sup>c</sup>	1499(1432) <sup>c</sup>	1.593(1.59) <sup>c</sup>	

<sup>a</sup> Experimental data from the ref. 70. <sup>b</sup> Experimental data from the ref. 71. <sup>c</sup> Experimental data from the ref. 27.

study is reliable in providing the geometrical parameters of the complexes. The structures of the complexes are described in terms of the separation ( $R_{\text{cm}}$ ) of the center of masses of the monomers and the angles made by the molecular axes of both the monomers with  $R_{\text{cm}}$ . In Fig. 1,  $\theta_1$  and  $\theta_2$  are the angles between the molecular  $C_x$ -axis of  $\text{O}_2$  or  $\text{N}_2$  and  $C_2$ -axis of  $\text{SO}_2$  respectively with  $R_{\text{cm}}$ . From Table 1, it can be observed that the  $R_{\text{cm}}$  value is the shortest (3.07 Å) in **1b** when compared to the unsymmetrical **1a** (3.44 Å) and in the symmetrical **2a** complex, it has the largest value of 3.74 Å.  $\text{SO}_2$  has a permanent dipole moment while  $\text{O}_2$  and  $\text{N}_2$  have no dipole moment. There is only slight structural perturbation that has occurred after complexation of  $\text{O}_2$  or  $\text{N}_2$  with  $\text{SO}_2$ . The experimentally obtained  $R_{\text{cm}}$  value of 3.89 Å is comparable with the theoretically determined value of 3.74 Å for  $\text{SO}_2\text{-N}_2$  complex. The theoretical calculation by Connelly *et al.* to obtain minimum  $R_{\text{cm}}$  value along with their experimental study was done by rigid relaxation of the complex.<sup>28</sup> The experimentally determined value of  $\theta_1$  and  $\theta_2$  for the complex **2a** are similar to the theoretical values of the present study.  $\theta_1$  is 147.6° in our calculation with MP2/aug-cc-pVTZ and 155.5° from experiment.  $\theta_2$  is calculated to be 94.3° in this work with MP2/aug-cc-pVTZ and is 94.8° from experimental studies. The distance between the S-atom and nearest N-atom of  $\text{N}_2$  monomer in the equilibrium structure of **2a** is found to be 3.36 Å, which is similar to the Juang *et al.*, determined value of 3.45 Å. A comparison between values of  $R_{\text{cm}}$ ,  $\theta_2$  between the theoretical and experimental analysis of structure **2a** are comparable and there is a slight deviation in the angle  $\theta_1$ , this difference is indicative of the large amplitude motion of  $\text{N}_2$  about the corresponding axis of the complex. Experimental evaluation of the  $\text{N}_2$ -containing vdW complexes shows that  $\text{N}_2$  undergoes tunneling rotation within the complex.<sup>28,60</sup> It is also established that if the other partner of the complex is non-linear then there is a possibility of multiple internal rotation.<sup>61</sup>

*Ab initio* calculations at MP2/aug-cc-pVTZ with additional keyword Prop = EFG yields theoretical electric field gradients of nitrogen,  $q_{\text{aa}}$ ,  $q_{\text{bb}}$ , and  $q_{\text{cc}}$  in standard orientation of the complex, and these values were rotated to the center of mass of the complex. Using the obtained values in center of mass, the theoretical <sup>14</sup>N quadrupole coupling strength,  $eQq_{\text{aa}}$  and  $eQq_{\text{cc}}$ , for the complex can be determined. The <sup>14</sup>N nuclear quadrupole moment value obtained by Bailey<sup>62</sup> gives  $eQ/h$  as 4.5617(43) MHz per a.u., and this value can be multiplied by the calculated  $q_{\text{xx}}$  (a.u.) to give the theoretical <sup>14</sup>N quadrupole coupling strength in MHz for the complex. The calculated nuclear quadrupole moment for <sup>14</sup>N1 and <sup>14</sup>N2 in **2a** complex is −4.23 MHz and −4.35 MHz respectively for  $eQq_{\text{aa}}$  value, 1.26 MHz and 1.30 MHz, for  $eQq_{\text{cc}}$  value. The experimental values<sup>27</sup> of −3.63 MHz and 1.30 MHz are similar to the calculated values.

### 3.2. Supermolecular interaction energies

The supermolecular interaction energies of the studied complexes of  $\text{SO}_2$  with different basis sets are given in Table 3. This table contains the BSSE corrected, BSSE uncorrected and ZPE corrected energies of the complexes. The BSSE contribution to the interaction energies vary from 50% to 7% for  $\text{SO}_2\text{-O}_2$  complexes and from 58% to 6% for  $\text{SO}_2\text{-N}_2$  complex. It shows that the BSSE correction is important, which should be taken into account while calculating the interaction energies of these systems. The values of the interaction energies of the complexes are small (see Table 3). The MP2/aug-cc-pVXZ (X = D, T), BSSE corrected binding energy,  $D_e$  is 6.59 kJ mol<sup>−1</sup> with aug-cc-pVDZ and 7.51 kJ mol<sup>−1</sup> with aug-cc-pVTZ for minima **1b**, which are higher than the corresponding value of 6.29 kJ mol<sup>−1</sup> and 6.68 kJ mol<sup>−1</sup> for the minima **1a**. This implies that **1b** structure of the  $\text{SO}_2\text{-O}_2$  vdW complex is more stable than the **1a** structure. It is also confirmed from the calculation at CBS limit and the correlation energy calculation with CCSD(T)/aug-cc-pVTZ. All the structural parameters in the complexes are CP-corrected. The CBS BSSE corrected interaction energy is 7.88 kJ mol<sup>−1</sup> for **1b** and 6.99 kJ mol<sup>−1</sup> for **1a**



**Table 3** The BSSE-corrected ( $D_e$ ) and ZPE corrected ( $D_0$ ) binding energies at MP2 and CBS methods of the CP-corrected complexes  $\text{SO}_2\text{-O}_2$  and  $\text{SO}_2\text{-N}_2$ . CCSD(T)/aug-cc-pVTZ//MP2/aug-cc-pVTZ are also given. All energies are in  $\text{kJ mol}^{-1}$ 

Binding energies									
Basis set	<b>1a</b>			<b>1b</b>			<b>2a</b>		
	$D_e$	$D_e^a$	$D_0$	$D_e$	$D_e^a$	$D_0$	$D_e$	$D_e^a$	$D_0$
MP2/aug-cc-pVDZ	-6.29	-9.33	-5.00	-6.59	-9.89	-4.89	-4.37	-6.89	-3.07
MP2/aug-cc-pVTZ	-6.68	-8.40	-5.22	-7.31	-9.30	-5.38	-4.85	-6.20	-3.42
CBS	-6.99	-7.43	—	-7.88	-8.35	—	-5.15	-5.46	—
CCSD(T)/aug-cc-pVTZ	-5.45	-7.29	—	-6.23	-8.35	—	-4.12	-5.50	—

<sup>a</sup> Binding energies are BSSE uncorrected.

whereas CCSD(T) interaction energy is  $6.23 \text{ kJ mol}^{-1}$  for **1b** and  $5.45 \text{ kJ mol}^{-1}$  for **1a**. The distance  $R_{\text{cm}}$  is longer in **1a** than in **1b** and **1a** shows lower binding energies at all levels of theories when compared to the structure **1b**. The  $D_e$  value for the  $\text{SO}_2\text{-N}_2$  complex is  $4.37 \text{ kJ mol}^{-1}$  at MP2/aug-cc-pVDZ and is 4.85 at MP2/aug-cc-pVTZ whereas CBS extrapolation gives  $5.15 \text{ kJ mol}^{-1}$ . The  $R_{\text{cm}}$  value of  $3.74 \text{ \AA}$  in **2a** is higher than both the complexes of  $\text{SO}_2\text{-O}_2$  and has lesser binding energy than **1a** and **1b**.

### 3.3. SAPT interaction energies

A physical interpretation of the interaction energy can be obtained by partitioning it into various components by using

perturbative methods. SAPT approach splits the total interaction energy into physically meaningful components. In this article, SAPT calculations have been performed as single point energy calculation for each of the three complex **1a**, **1b** and **2a** of  $\text{SO}_2$  with the basis set of cc-pVDZ (VDZ), aug-cc-pVDZ (AVDZ) and aug-cc-pVTZ (AVTZ). The geometries used for SAPT calculations are MP2/aug-cc-pVTZ optimized and CP-corrected. The basis set AVDZ and AVTZ are large enough for providing reliable energy components. Calculation with VDZ basis set was carried out to evaluate the effect of diffusion functions in energy calculations. The total SAPT interaction energy ( $E_{\text{int}}^{\text{SAPT}}$ ) is partitioned into the major energy terms of electrostatic ( $E_{\text{elst}}$ ), exchange ( $E_{\text{exch}}$ ),

**Table 4** Calculated SAPT interaction energies and its components for the three vdW complexes of  $\text{SO}_2$  in  $\text{kJ mol}^{-1}$  with VDZ, AVDZ and AVTZ basis sets

Energy components	VDZ			AVDZ			AVTZ		
	$\text{SO}_2\text{:O}_2$		$\text{SO}_2\text{:N}_2$	$\text{SO}_2\text{:O}_2$		$\text{SO}_2\text{:N}_2$	$\text{SO}_2\text{:O}_2$		$\text{SO}_2\text{:N}_2$
	<b>1a</b>	<b>1b</b>	<b>2a</b>	<b>1a</b>	<b>1b</b>	<b>2a</b>	<b>1a</b>	<b>1b</b>	<b>2a</b>
$E_{\text{elst}}^{(10)}$	0.74	0.49	-5.30	-6.86	1.16	-4.29	-6.09	1.03	-4.27
$E_{\text{elst,resp}}^{(12)}$	-1.16	0.19	-0.43	-1.86	0.64	-0.71	-1.74	0.60	-0.52
$E_{\text{elst,resp}}^{(13)}$	0.73	0.24	0.10	1.02	-0.04	0.30	1.17	-0.09	0.34
$E_{\text{exch}}^{(10)}$	9.75	12.36	5.15	8.39	12.59	5.39	8.34	12.49	5.36
$E_{\text{exch}}^{(11)}$	0.14	0.13	-0.05	-0.19	0.26	-0.005	-0.08	0.41	0.07
$E_{\text{exch}}^{(12)}$	-0.34	-0.11	0.90	2.61	0.48	1.11	2.13	-0.18	0.80
$E_{\text{ex-ind}}^{(22)}$	-0.08	-0.74	0.05	0.13	-0.45	0.09	0.12	-0.67	0.03
$E_{\text{ex-ind,resp}}^{(20)}$	3.45	4.80	1.38	3.12	4.80	1.38	3.23	4.94	1.42
$E_{\text{exch-disp}}^{(20)}$	0.49	0.62	0.28	0.67	0.91	0.40	0.78	1.05	0.45
$E_{\text{ind,resp}}^{(20)}$	-5.52	-6.07	-2.04	-23.68	-6.44	-2.14	-21.80	-6.59	-2.19
$E_{\text{ind}}^{(22)}$	0.36	0.93	-0.07	-1.00	0.61	-0.14	-0.79	0.89	-0.04
$E_{\text{disp}}^{(20)}$	-4.14	-5.24	-3.62	-7.57	-9.77	-5.84	-8.67	-11.14	-6.42
$E_{\text{disp}}^{(21)}$	1.34	1.82	1.38	1.80	2.85	1.86	1.85	3.00	1.93
$E_{\text{disp}}^{(22)}$	-0.88	-1.28	-1.23	-2.24	-2.47	-1.98	-2.42	-2.59	-2.08
$E_{\text{exch}}^{(1)}(\text{CCSD})$	-0.26	0.003	1.23	3.16	0.73	1.53	2.48	0.05	1.12
$E_{\text{int,resp}}^{(\text{HF})}$	1.58	-11.58	0.81	19.03	-12.12	-0.34	16.32	-11.86	-0.33
$E_{\text{int}}^{\text{SAPT0}}$	-3.65	-4.62	-3.34	-6.90	-8.86	-5.44	-7.89	-10.08	-5.97
$E_{\text{int}}^{\text{SAPT2}}$	-4.73	-4.22	-2.94	-7.20	-7.33	-5.08	-8.24	-9.02	-5.63
$E_{\text{int}}^{\text{SAPT}}$	-3.60	-3.45	-2.32	-5.88	-6.99	-4.48	-7.21	-8.88	-5.19
$E_{\text{elst}}$	0.32	0.92	-5.63	-7.69	1.77	-4.70	-6.65	1.54	-4.44
$E_{\text{exch}}$	13.34	17.05	8.08	15.48	18.58	8.79	14.95	17.86	8.39
$E_{\text{ind}}$	-15.16	-5.14	-2.10	-24.68	-5.83	-2.28	-22.59	-5.70	-2.23
$E_{\text{disp}}$	-3.68	-4.69	-3.47	-8.01	-9.39	-5.95	-9.24	-10.72	-6.57
$E_{\text{int}}^{(\text{B3LYP-D3})}$							-5.79	-7.66	-4.75
$E_{\text{int}}^{(\text{TPSS-D3})}$							-5.36	-8.20	-4.34
$E_{\text{int}}^{(\text{PBE-D3})}$							-11.92	-15.58	-4.82
$E_{\text{int}}^{(\text{MP2})}$							-6.68	-7.31	-4.85
$D_0$							-5.22	-5.38	-3.42
CCSD							-5.45	-6.23	-4.12
CBS	-6.99	-7.88	-5.15	-6.99	-7.88	-5.15	-6.99	-7.88	-5.15



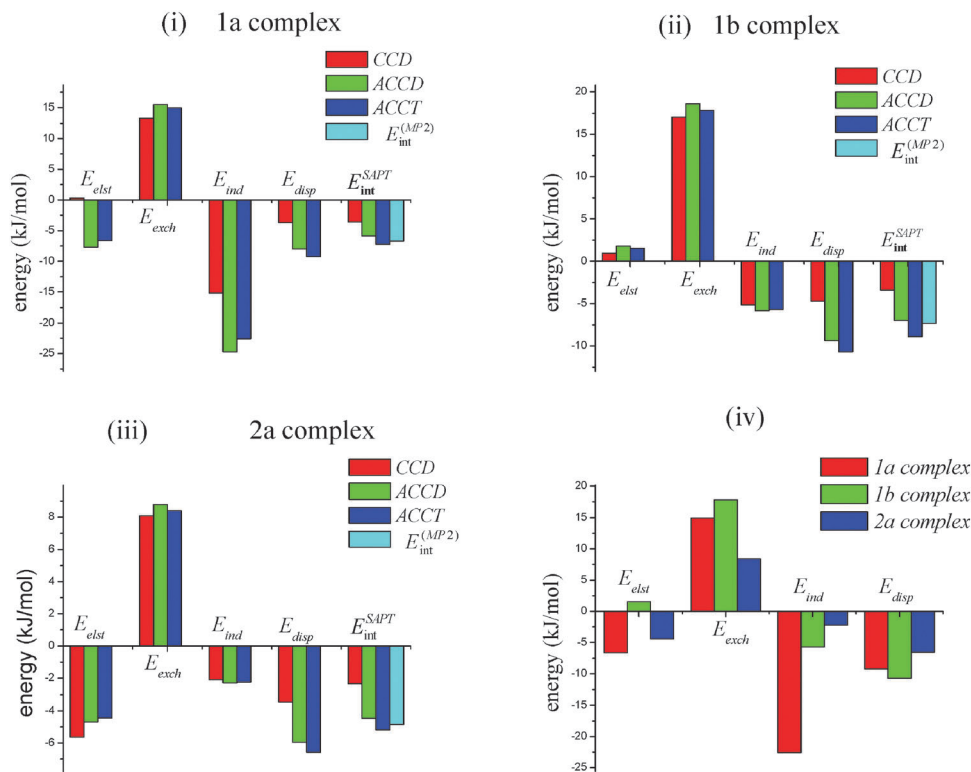


Fig. 2 Bar diagram (i), (ii), (iii) represents the SAPT interaction energy components with VDZ, AVDZ and AVTZ basis sets. (iv) is the comparison of SAPT interaction energies with AVTZ basis set amongst the complexes **1a**, **1b**, **2a** optimized at MP2/aug-cc-pVTZ.

induction ( $E_{\text{ind}}$ ) and dispersion ( $E_{\text{disp}}$ ) energies. Table 4 contains the corresponding SAPT results of different energy terms and the plots are shown in Fig. 2.

It is observed from Table 4 that VDZ basis set without the diffuse function leads to an underestimation of  $E_{\text{int}}^{\text{SAPT}}$  compared with the supermolecular interaction energy calculation. VDZ basis set underestimates each energy term when compared with AVDZ basis set as shown in Fig. 2(i)–(iii). AVDZ with the diffuse functions gives the comparable result for the total SAPT interaction energies. There is no significant change in the SAPT energy than the respective supermolecular energy calculated at MP2/aug-cc-pVTZ, CCSD(T)/aug-cc-pVTZ and CBS limit. There is a significant increase in stabilization energies of the complexes with AVDZ basis set when compared to the VDZ basis set. Therefore, for these complexes use of diffuse function is a necessity. The discrepancy between the VDZ calculated SAPT energy and MP2 calculation could also be seen from the Fig. 2(i)–(iii). The  $C_s$  complex shows greater stability than  $C_1$  complex of  $\text{SO}_2\text{-O}_2$  and is in agreement with the supermolecular calculation as discussed above. The total SAPT energy and each major SAPT energy components show negligible difference between AVDZ and AVTZ basis sets. There is a small change in the energy terms for the three complexes of  $\text{SO}_2$  by going to larger basis set. It can be concluded that for these systems in this work, use of AVDZ basis set is adequate for the SAPT calculation compared to the AVTZ basis set which is associated with significant computational effort.

The individual energy components of SAPT interaction energies of the complexes **1a**, **1b** and **2a** with the AVTZ basis

set have been interpreted. It can be noticed from Table 4 and Fig. 2(iv), that there is a significant difference in the corresponding individual energy terms amongst the structures **1a**, **1b** and **2a**. From the inspection of the energy components as given in Table 4, it can be concluded that the major contribution to the total interaction energy is from the induction energy ( $E_{\text{ind}}$ ) and dispersion energy ( $E_{\text{disp}}$ ). In case of structure **1a**, the attractive first order electrostatic energy term  $E_{\text{elst}}^{(10)}$  is compensated by the first order exchange repulsive  $E_{\text{exch}}^{(10)}$  term and is same for the structure of **2a** of  $\text{SO}_2$  and  $\text{N}_2$ . The  $E_{\text{elst}}^{(10)}$  is negligible in **1b** structure while  $E_{\text{exch}}^{(10)}$  is repulsive. The major contribution to the interaction energy of these complexes comes from the attractive second-order induction energy,  $E_{\text{ind,resp}}^{(20)}$  and second-order dispersion energy,  $E_{\text{disp}}^{(20)}$  terms. These two terms are the dominant and attractive. They are the main contributors for the binding energy of the complexes in this study. The  $E_{\text{ind,resp}}^{(20)}$  is the electric polarization caused by the electric and nuclear charge. The ratio of  $E_{\text{ind}}$  to the SAPT energy,  $E_{\text{int}}^{\text{SAPT}}$  are 3.13, 0.64 and 0.43 for **1a**, **1b** and **2a** respectively. This shows that the induction energy term form a part of the total interaction energy and thus plays an important role in binding these systems. The dispersive effect ratio ( $E_{\text{disp}}/E_{\text{int}}^{\text{SAPT}}$ ) is equal to 1.28 for **1a**, 1.21 for **1b** and 1.27 for **2a**. This indicates that the dispersive effect is similar in all complexes. The energy term,  $\delta_{\text{int,resp}}^{\text{HF}}$  contains the contribution from the higher order induction and exchange-induction effect to the stabilization of the complexes. In this study, this energy term is also an important and non-negligible to characterize the effects. The energy,  $\delta_{\text{int,resp}}^{\text{HF}}$  is repulsive in **1a**



and more attractive in structure **1b**. This shows that  $\delta_{\text{int,resp}}^{(\text{HF})}$  is important parameter, which contributes towards the extra stability of the complex **1b** compared to **1a**.

The interplay between the dispersion and induction effect in these intermolecular complexes can be understood by analyzing the ratio of dispersion energy to induction energy ( $E_{\text{disp}}/E_{\text{ind}}$ ). The ratio,  $E_{\text{disp}}/E_{\text{ind}}$  is 0.41 in **1a**, 1.88 in **1b** and 2.95 in the **2a** structure. From this ratio, it is predicted that the structure **1a** formation is favored by the induction effect whereas structure **1b** and **2a** formation are favored by dispersion effect. This can also be explained in terms of the simple molecular properties of dipole moment. The dipole moment of  $\text{SO}_2$  at MP2/aug-cc-pVTZ is comparable with the experimental value (see Table 2). Since induction energy is due to the interaction of permanent multipole moment of the monomers, the structure **1a** having the higher dipole moment than the structure **1b** and **2a** and even more than monomer  $\text{SO}_2$  at MP2/aug-cc-pVTZ is also reflected from the SAPT calculation where induction effect is dominant in structure **1a**.

The dispersion corrected interaction energies,  $E_{\text{int}}^{(\text{DFT-D3})}$  of the weak vdW complexes is also predicted by implementing the

DFT-D3 method with B3LYP, TPSS and PBE functional and aug-cc-pVTZ basis set on the MP2/aug-cc-pVTZ optimized structures as shown in Table 4. From Table 4, it is noticed that with B3LYP and TPSS methods are showing similar interaction energies for all three structures.

### 3.4. Vibrational data analysis

The calculated vibrational frequencies and corresponding intensities of the monomers  $\text{SO}_2$ ,  $\text{O}_2$ ,  $\text{N}_2$  and the complexes **1a**, **1b** and **2a** are presented in the Table 5 along with the literature values. Table 5 summarizes the data derived from MP2 method with aug-cc-pVDZ and aug-cc-pVTZ basis set. There is no experimental vibrational data available in the literature for the complexes. From Table 5, it is observed that the frequency data computed with aug-cc-pVTZ are much closer to the available data for the monomers. The geometries used for the vibrational analysis are CP-corrected.

There is a smaller shift in frequencies and intensities in the complexes from the individual monomers for different modes of vibrations. The vibrational frequencies related to

**Table 5** The calculated unscaled frequencies (in  $\text{cm}^{-1}$ ) and absolute intensities ( $\text{km mol}^{-1}$ ) of the monomers and the complexes of  $\text{SO}_2\text{-O}_2$  and  $\text{SO}_2\text{-N}_2$  at MP2/aug-cc-pVXZ (X = D, T). Bracket values are respective frequency and intensity shift from individual monomers

Species	Mode no.	Mode description	Frequency		Intensity	
			aug-cc-pVDZ	aug-cc-pVTZ	aug-cc-pVDZ	aug-cc-pVTZ
$\text{N}_2$	1	N-N str	2157	2187(2359) <sup>a</sup>	—	—
$\text{O}_2$	1	O-O str	1226	1262(1580) <sup>b</sup>	—	—
$\text{SO}_2$	1	S-O symstr	1022	1099(1151) <sup>c</sup>	11.6	16.0(25) <sup>c</sup>
	2	S-O asymstr	1207	1306(1362) <sup>c</sup>	108.2	138.7(189) <sup>c</sup>
	3	O-S-O bend	463	493(518) <sup>c</sup>	22.1	23.9(25.2) <sup>c</sup>
<b>1a</b>	1	O-O str	1214(−12)	1251(−11)	0.4	0.1
	2	S-O symstr	1024(+2)	1101(+2)	11.5(−0.4)	15.8(−1)
	3	S-O asymstr	1207(+0.2)	1304(−2)	112.3(+4)	141.7(+2)
	4	O-S-O bend	464(+1)	495(+2)	21.3(−4)	22.9(−5)
	5	S-O3str	71	76	2.5	2.1
	6	S-O4str	56	59	4.1	6.3
	7	O1-O4	41	49	9.3	6.9
	8	$\text{SO}_2\text{,O}_2\text{librat.}$	31	40	0.3	0.9
	9	$\text{SO}_2\text{,O}_2\text{librat.}$	26	30	1.46	1.2
<b>1b</b>	1	O-O str	1218(−8)	1255(−7)	0.4	0.4
	2	S-O symstr	1025(+3)	1102(+3)	12.0(+4)	16.1(0.7)
	3	S-O asymstr	1207(+0.4)	1304(−2)	115.0(+6)	144.0(+4)
	4	O-S-O bend	464(+1)	494(+1)	20.5(−7)	22.0(−8)
	5	S-O3str	89	96	12.1	10.8
	6	S-O4str	71	81	2.6	6.0
	7	$\text{SO}_2\text{,O}_2\text{librat.}$	52	60	3.5	1.8
	8	$\text{SO}_2\text{,O}_2\text{librat.}$	42	49	0.5	0.6
	9	$\text{SO}_2\text{,O}_2\text{librat.}$	32	42	0.1	0.0
<b>2a</b>	1	N-N str	2156(−1)	2185(−2)	0.1	0.1
	2	S-O symstr	1024(+2)	1101(+2)	11.8(+2)	16.0(+0.1)
	3	S-O asymstr	1208(+1)	1306(+0.4)	105.3(−3)	133.9(−4)
	4	O-S-O bend	464(+1)	495(+2)	21.1(−5)	22.8(−5)
	5	S-N1str	56	61	9.5	10.3
	6	$\text{SO}_2\text{,N}_2\text{librat.}$	63	66	0.1	0.02
	7	$\text{SO}_2\text{,N}_2\text{librat.}$	60	68	0.02	0.3
	8	$\text{SO}_2\text{,N}_2\text{librat.}$	18	24	7.4	5.9
	9	$\text{SO}_2\text{,N}_2\text{librat.}$	18	20	0.1	0.2

<sup>a</sup> Experimental data from the ref. 72. <sup>b</sup> Experimental data from the ref. 70. <sup>c</sup> Experimental data from the ref. 73.



the intermolecular stretching correspond to the large amplitude motion and are of lower frequencies. The changes occurring in the vibrational frequencies are due to the dipole quadrupole interaction between the monomers. There is a red shift of  $1\text{ cm}^{-1}$  at MP2/aug-cc-pVDZ and of  $2\text{ cm}^{-1}$  at MP2/aug-cc-pVTZ for  $\text{N}_2$  stretching mode in complex **2a** from the monomer. The  $\text{N}_2$  harmonic stretching frequency is equal to  $2187\text{ cm}^{-1}$  in the monomer and it decrease to  $2185\text{ cm}^{-1}$  in the complex **2a** at MP2/aug-cc-pVTZ level. The  $\text{O}_2$  stretching mode is also red shifted by  $12\text{ cm}^{-1}$  at aug-cc-pVDZ and  $11\text{ cm}^{-1}$  at aug-cc-pVTZ in complex **1a** whereas the red shift is of  $8\text{ cm}^{-1}$  at aug-cc-pVDZ and  $7\text{ cm}^{-1}$  at aug-cc-pVTZ in complex **1b**. The harmonic stretching frequency associated with the S–O bond stretching (symmetric and asymmetric) and the bending O–S–O modes of  $\text{SO}_2$  unit are increased in the complex **2a** when compared with the respective values in the monomer. The S–O symmetric stretching is blue shifted by  $2\text{ cm}^{-1}$  both in complex **1a** and **2a** at aug-cc-pVDZ and aug-cc-pVTZ and it is also blue shifted  $3\text{ cm}^{-1}$  in case of the complex **1b**. From the Table 5 it is observed that the shifting in stretching frequency of  $\text{O}_2$  and  $\text{N}_2$  upon complex formation is small and it indicates that these are weak complexes and thus the interaction of the induced dipole in  $\text{O}_2$  and  $\text{N}_2$  with  $\text{SO}_2$  molecule affects little the stretching vibrations. The different vibrational modes associated with intermolecular motions are calculated and are given in the Table 5. From this table, it is clear that the intermolecular vibrations are of quite low frequency and low intensity. Calculation of these low frequencies can play an important role for experimentalist in characterizing the molecular vibrations in the complexes.

### 3.5. Orbital interaction analysis

The bonding features in terms of interorbital interaction present in the complexes,  $\text{SO}_2\text{--O}_2$  and  $\text{SO}_2\text{--N}_2$  have been studied by performing NBO analysis, which is computed at MP2/aug-cc-pVTZ level of theory. The secondary perturbation energies ( $E_i$ ) and related donor–acceptor orbitals of the monomers are summarized in the Table 6. In this study, the bondings in the vdW complexes are found to be caused by the charge transfer from lone pairs of X-atom of  $\text{X}_2$  ( $\text{X} = \text{O}, \text{N}$ ) unit to the antibonding orbitals of SO of  $\text{SO}_2$  unit. In complex **1a**, the charge transfer occurred from the O-atom lone pairs of  $\text{O}_2$  to each of  $\sigma^*$  and  $\pi^*$  antibonding SO orbital giving interaction energy of amount  $0.46\text{ kJ mol}^{-1}$  and  $0.75\text{ kJ mol}^{-1}$  respectively. In complex **1b**, the main contribution comes from the charge transfer from O-atom lone pair of  $\text{O}_2$  to  $\pi^*$  antibonding SO orbital, which amounts to  $3.06\text{ kJ mol}^{-1}$  followed by another charge transfer from O-atom lone pair of  $\text{O}_2$  to  $\sigma^*$  antibonding SO orbital amounting  $0.34\text{ kJ mol}^{-1}$ . The higher stabilization energy for the charge transfer from O-lone pair of  $\text{O}_2$  to SO antibonding orbital suggests that structure **1b** is more stable than structure **1a**. In the **2a** complex, the interaction energy for the charge transfer from the N-atom lone pair to the  $\sigma^*$  antibonding SO orbital is  $0.25\text{ kJ mol}^{-1}$  and this is lower than the non-Lewis type  $\text{S}_{\text{lp}} \rightarrow \text{Ryd}^*(\text{N})$  amounting  $0.34\text{ kJ mol}^{-1}$ . The lowest stability of complex **2a**, having the lowest orbital interaction energy among the three complexes is found to be

**Table 6** The secondary perturbation NBO energies ( $E_i$ , in  $\text{kJ mol}^{-1}$ ) of the  $\text{SO}_2\text{--O}_2$  and  $\text{SO}_2\text{--N}_2$  complexes computed at the level of MP2/aug-cc-pVTZ

Species	Donor/acceptor	Interaction orbital	$E_i$
<b>1a</b>	$\text{O}_2/\text{SO}_2$	$\text{O}_{\text{lp}} \rightarrow \sigma^*(\text{SO})$	0.46
	$\text{O}_2/\text{SO}_2$	$\text{O}_{\text{lp}} \rightarrow \pi^*(\text{SO})$	0.75
<b>1b</b>	$\text{O}_2/\text{SO}_2$	$\text{O}_{\text{lp}} \rightarrow \sigma^*(\text{SO})$	0.34
	$\text{O}_2/\text{SO}_2$	$\text{O}_{\text{lp}} \rightarrow \pi^*(\text{SO})$	3.06
<b>2a</b>	$\text{N}_2/\text{SO}_2$	$\text{N}_{\text{lp}} \rightarrow \sigma^*(\text{SO})$	0.29

consistent with the results of the other interaction energy calculations. The pictorial diagrams of electron density surface of the three vdW complexes investigated in this study are shown in Fig. 3.

The quantum theory of atoms in molecules (QTAIM)<sup>63,64</sup> has become an important tool which reveals the chemical bonding present in molecules in terms of electron density,  $\rho$  at bond critical points (BCP).<sup>65</sup> The topological parameter of  $\rho$ , at the BCP in the complexes of  $\text{SO}_2$  are summarized in Table 7. From the data in Table 7, it can be observed that the  $\rho$  value for the S–O3 interaction in the  $\text{SO}_2\text{--O}_2$  complexes is in the range of  $0.008\text{--}0.009\text{ a.u.}$  while it is of  $0.006\text{ a.u.}$  in  $\text{SO}_2\text{--N}_2$  complex for the bond between S and N1. The low value of  $\rho$  shows that these are weak intermolecular vdW bonds. This is indicated by minor structural changes in geometric parameters of the monomers in complexes and also smaller perturbation in harmonic stretching frequencies.

## 4. Atmospheric consequences

The complexes of  $\text{SO}_2$  with  $\text{O}_2$  and  $\text{N}_2$  exhibit several low frequency intermolecular vibrational modes. Due to the presence of these vibrational modes, the complexes can absorb the IR radiation. The average concentration of  $\text{SO}_2$  in atmosphere<sup>66</sup> is approximately  $1 \times 10^3\text{ ppt}$  (parts per trillion), and its concentration rises to  $1 \times 10^6\text{ ppt}$  after a volcanic eruption. The higher  $\text{SO}_2$  concentration is known to linger for several days before it gets oxidized to form aerosol particles.<sup>21</sup> The estimation of the atmospheric concentration of the studied complexes at  $298.15\text{ K}$  and  $1\text{ atmosphere}$  can be calculated by applying the following expression

$$\Delta G = -RT \ln \frac{P[\text{SO}_2\text{--Y}_2]}{P[\text{SO}_2]P[\text{Y}_2]} \quad (12)$$

where  $P$  represents the partial pressure and  $\Delta G$  is Gibb's free energy change,  $\text{Y} = [\text{O}_2]$  or  $[\text{N}_2]$  for the respective complexes. Second-order vibrational perturbation theory as implemented in Gaussian09 has been used to perform the anharmonic frequency calculation at MP2/aug-cc-pVTZ to obtain the anharmonic corrected thermochemical parameters of enthalpy and entropy. These corrected data are then used to predict the atmospheric concentration of the complexes. The thermochemical data of change in enthalpy ( $\Delta H$ ), change in entropy ( $\Delta S$ ) and Gibb's free energy change ( $\Delta G$ ) of the  $\text{SO}_2\text{--O}_2$  and



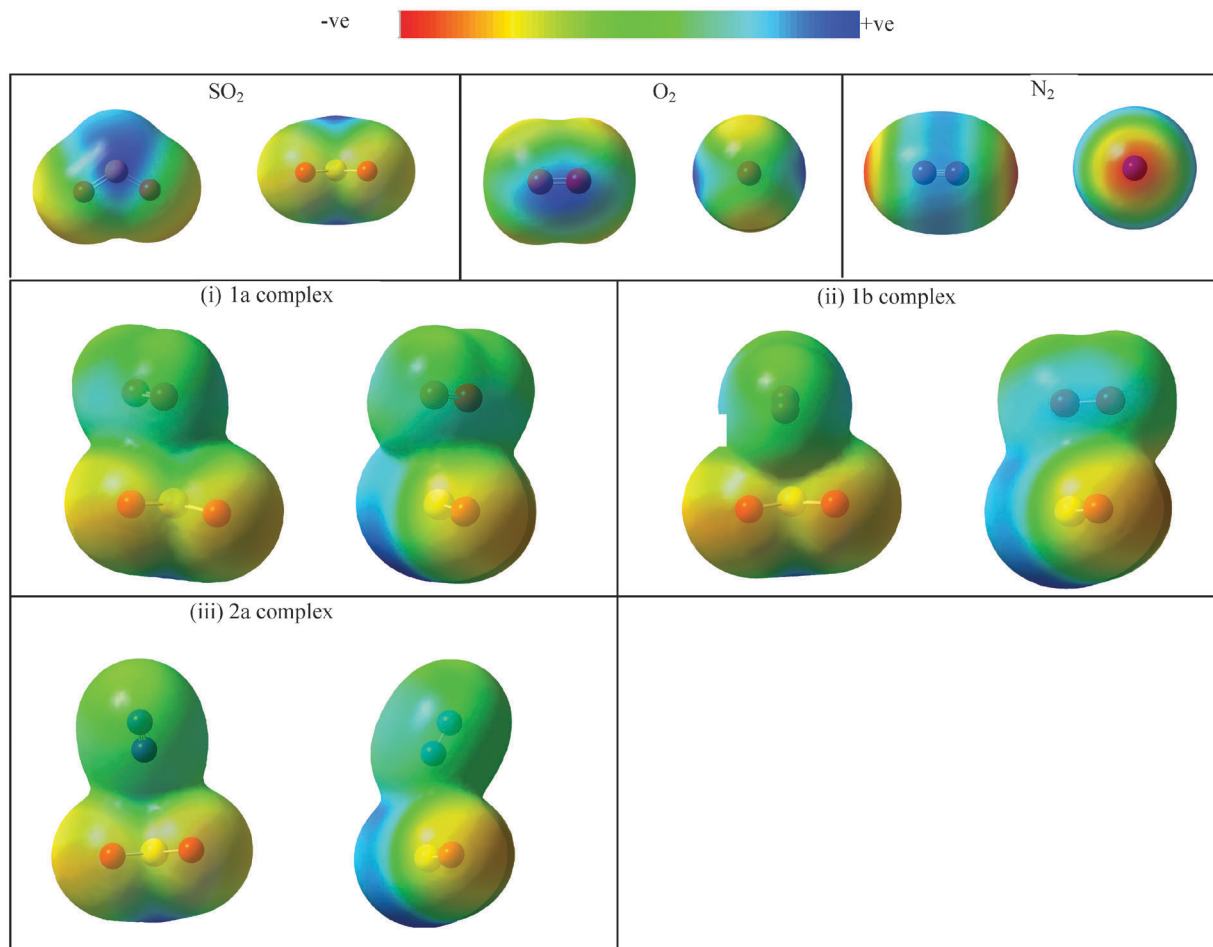


Fig. 3 The plot of electron density surface of the monomers and the complexes  $\text{SO}_2\text{-O}_2$  and  $\text{SO}_2\text{-N}_2$  at isosurface value of  $\pm 0.0004$  a.u. at MP2/aug-cc-pVTZ level. Blue, green, yellow and red colors define the region from more positive values to the region of negative values. Two different views with respect to molecular/complex plane and normal plane are shown for the monomers and complexes.

Table 7 The AIM calculated electron density ( $\rho$ , in a.u.) of bond critical points (BCP) of the monomers and  $\text{SO}_2\text{-O}_2$  and  $\text{SO}_2\text{-N}_2$  complexes computed at the level of MP2/aug-cc-pVTZ

Monomers	$\rho$	Complexes	$\rho$
$\text{SO}_2$		<b>1a</b>	
S–O1	0.281	S–O1	0.281
S–O2	0.281	S–O2	0.281
		O3–O4	0.468
		S–O3	0.008
$\text{O}_2$		<b>1b</b>	
O3–O4	0.470	S–O1	0.281
		S–O2	0.281
		O3–O4	0.470
		S–O3	0.009
$\text{N}_2$		<b>2a</b>	
N1–N2	0.681	S–O1	0.281
		S–O2	0.281
		N1–N2	0.680
		S–N1	0.006

$\text{SO}_2\text{-N}_2$  complex formation at 298.15 K and 1 atmosphere are given in Table 8. The atmospheric concentration of  $\text{N}_2$  and  $\text{O}_2$  are  $7.8 \times 10^{11}$  ppt and  $2.1 \times 10^{11}$  ppt respectively. Substituting these

Table 8 Thermochemical parameters of change in enthalpy ( $\Delta H$ , in  $\text{kJ mol}^{-1}$ ), change in entropy ( $\Delta S$ , in  $\text{J mol}^{-1} \text{K}$ ) and Gibbs's free energy change ( $\Delta G$ , in  $\text{kJ mol}^{-1}$ ,  $\Delta G = \Delta H - T\Delta S$ ) of the  $\text{SO}_2\text{-O}_2$  (**1a**, **1b**) and  $\text{SO}_2\text{-N}_2$  (**2a**) complex formation calculated at MP2/aug-cc-pVTZ. Thermochemical parameters of enthalpy and entropy are anharmonic corrected

Parameters	<b>1a</b>	<b>1b</b>	<b>2a</b>
$\Delta H$	−6.62	−1.00	3.80
$\Delta S$	−118.99	−74.88	−35.72
$\Delta G$	28.86	21.32	14.44

concentration values in eqn (12), the equilibrium concentration of the complex **1a**, **1b** and **2a** in atmosphere can be calculated. Using expression (12), the concentration of **1a**, **1b** and **2a** are calculated to be 0.002 ppt, 0.04 ppt and 2.30 ppt respectively in atmosphere and are 2 ppt, 39 ppt and 2300 ppt respectively after volcanic eruption under the ambient atmospheric condition. After a volcano eruption, the concentration of  $\text{N}_2$  molecules increases<sup>67</sup> and concentration of  $\text{O}_2$  decreases due to oxidation process for few days. Hence, calculated value of 2300 ppt is a lower limit for nitrogen complex and 2 ppt, 39 ppt is the upper limit for both the oxygen complex. The relative concentration



of **1a**, **1b** and **2a** complexes to SO<sub>2</sub> concentration are  $1.8 \times 10^{-4}$ ,  $3.9 \times 10^{-3}$  and  $2.3 \times 10^{-1}\%$  respectively. Though these relative concentrations are low in number but they can have role in atmospheric chemistry like chlorofluorocarbon (CFC), hydrochlorofluorocarbon (HCFC), hydrofluorocarbon (HFC) which have the concentration range of 3–550 ppt in atmosphere and are considered to have the greater potential to increase the green house effect than CO<sub>2</sub>.<sup>68,69</sup> The complexes of SO<sub>2</sub> with O<sub>2</sub> and N<sub>2</sub> with such a concentration might also play an important role in atmospheric chemistry.

## 5. Conclusion

The complexes studied in this work are important from the atmospheric point of view. The ground state bonding features, energies and spectroscopic properties of 1 : 1 vdW complexes of SO<sub>2</sub>-O<sub>2</sub> and SO<sub>2</sub>-N<sub>2</sub> have been investigated using high level *ab initio* methods and basis sets. Two minimum structures for SO<sub>2</sub> with O<sub>2</sub> and one with N<sub>2</sub> have been determined and characterized. In both the cases, the most stable equilibrium configurations of the complexes are found to have the C<sub>s</sub> symmetry where one atom of O<sub>2</sub> or N<sub>2</sub> is facing the S atom of SO<sub>2</sub> (see Fig. 1). The complex **1b** of SO<sub>2</sub>-O<sub>2</sub> is determined to have higher binding energy at all levels of theory than SO<sub>2</sub>-N<sub>2</sub> complex. From the SAPT calculation, it can be concluded that the stable two configurations (**1b** and **2a**) are dispersive effect dominated. The ratio of dispersion to the induction energies for **1b** is 1.88 and for **2a** it is 2.95. The binding energy calculations show that these complexes contain weak intermolecular vdW forces, which is reinforced by frequency, NBO and AIM analysis. The calculated IR absorption spectrums of the complexes are also discussed and it has been found that the studied complexes of SO<sub>2</sub> show several low intermolecular vibrational frequencies in the far IR region.

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