Short-range correlations in d–f cyanido-bridged assemblies with XY and XY-Heisenberg anisotropy

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Two new d–f cyanido-bridged 1D assemblies [RE(pzam),(H2O)Mo(CN)8]·H2O (RE = Sm(III), Er(III)) were synthesized and their magmeto-structural properties have been studied by field-dependent magnetization and specific heat measurements at low temperatures (T ≥ 0.3 K). Below T = 10 K the ground state of both the Sm(III) and Er(III) ions is found to be a Kramers doublet with effective spin S = 1/2. From analyses of the low-temperature magnetic specific heat and magnetization the exchange coupling between these RE(III) effective spins and the Mo(V) spins S = 1/2 along the structural chains has been determined. It is found to be antiferromagnetic, with J /k_B = -2.6 K and Ising-Heisenberg symmetry of the interaction (J /J_z = 0.3) for RE = Sm(III), whereas the compound with RE = Er(III) behaves as a pure XY chain, with J /k_B = -1.0 K. For the compound [Sm(pzam),(H2O)Mo(CN)8]·H2O a small λ-type anomaly in the specific heat is observed at about 0.6 K, which is ascribed to a transition to long-range magnetic ordering induced by weak interchain interactions of dipolar origin. No evidence for 3D interchain magnetic ordering is found in the Er(III) analogue.

Introduction

Heterobimetallic d–f metal complexes provide a rich source for the study of the magnetic interactions between d and f metal ions.1–7 It has been predicted theoretically that the magnetic exchange interactions of f-type ions with other paramagnetic species will be ferromagnetic for n > 7 and antiferromagnetic for n < 7.8 However, the studies reported so far do not fully corroborate this prediction. The magnetic exchange interactions involving the f electrons are weak, and often masked by the crystal field effects on the magnetic susceptibility. Therefore, the analysis of the experimental data often proves to be difficult. To ascertain the nature of the magnetic exchange interaction between rare-earth(III) ions and transition metal ions in cyanido-bridged assemblies derived from hexacyanidometallate building-blocks, an experimental methodology has been developed in which the intrinsic rare-earth(III) ion magnetic properties are determined separately by comparing the χ,T vs. T curves for two isostructural analogues (i.e. RE-M and RE-M′) where RE is a rare-earth ion M and M′ represent a paramagnetic and a diamagnetic transition metal ion).9–12 However, in several cases, this approach has likewise failed in correctly determining the strength and/or type of the d–f exchange interaction. Consequently, a more precise estimate of the d–f exchange interaction should preferably include measurements of other thermodynamic properties besides the magnetic susceptibility, in order to more reliably separate the effects of the ligand field splittings from the contributions arising from the (anisotropic) exchange coupling. In this respect, the experimental study of the low-temperature magnetic specific heat of heterobimetallic d–f assemblies has proven to be a useful tool since it provides a direct determination of the magnetic ground state of the f metal ion9 resulting from the ligand field splittings, as well as a valuable estimate of the strength and type of the d–f exchange interaction.

As a part of a detailed study of cyanido-bridged complexes with low-dimensional magnetic networks, we have previously shown that a combination of magnetic and low-temperature specific heat measurements advantageously allows a rigorous determination of the exchange interactions between neighbouring metal ions and their correlation to the structure.13–25 In this paper, we extend these studies to two new RE members of this series, namely [RE(pzam),(H2O)Mo(CN)8]·H2O (RE(III) = Sm, Er).

Structural and experimental details

The synthesis and complete crystallographic studies of the complexes of general formula [RE(pzam),(H2O)Mo(CN)8]·H2O have been reported earlier.21–25 They crystallize in the space group Pna21 and their crystal structure is formed by chains of cyanido-bridged alternating arrays of [Mo(CN)8]2– and [RE(pzam),(H2O)]4–.
fragments running along the b crystallographic axis. Each chain is surrounded by six other equivalent chains through hydrogen bonding interactions, giving rise to a three-dimensional network.

Temperature dependent magnetic susceptibility and magnetization measurements were performed with a Quantum Design MPMS-5 ST SQUID magnetometer in the temperature range 1.8–300 K and up to 5 T. Data were corrected for the magnetization of the sample holder and for diamagnetic contributions as estimated from the Pascal constants. The presence of next-nearest neighbour magnetic interactions, i.e. RE(III)–RE(III) or Mo(V)–Mo(V) within the chains has been verified by studying the magnetic properties of the lanthanum diamagnetic derivative.24 In that case, we have found no evidence for a magnetic interaction between the 4d Mo(v) ions via the La(III) ion. It may then also be safely assumed that the magnetic interaction between the 4f RE(III) ions mediated through the Mo(v) ion can be neglected.24

Heat capacity measurements in different magnetic fields were carried out in the range 0.3 K to 25 K with a commercial 3He setup (PPMS), using the relaxation method. The investigated samples were in the form of polycrystalline powders. The measured specific heat of both complexes has been analyzed in terms of two additive contributions, namely the lattice (phonon) contribution (C_l) and the magnetic contribution (C_m). The phonon contribution can be deduced from the zero-field measurements, in combination with the field-independent part of the high-temperature in-field data (the data for T > 10 K). As explained previously,25 C_l is given by a polynomial function above 8 K of which the lowest order (T^α) can be interpreted in terms of the Debye model, yielding an estimate of the Debye temperature. By numerical integration of the magnetic heat capacity the magnetic entropy can be obtained, giving a direct determination of the number of spin states involved in the magnetic ordering process and thus the magnetic ground states of the RE(III) ion involved.

Results and discussion

Temperature and field dependent magnetizations above 1.8 K

As alluded to in the above, it is often not straightforward to determine the nature of the interaction between a RE(III) ion with a first-order orbital momentum and a paramagnetic transition metal ion without ambiguity. This is because the free-ion states of the RE(III) ions having the same J but arising from different \( ^{2S+1} \Gamma _{J} \) terms may mix through spin–orbit coupling. In addition, the resulting states are split further and mixed by the ligand field, such that the spectrum of the low-lying states that determine the magnetic properties at low temperature may become rather complicated. The presence of excited states further up in energy above the ground state may also add a significant temperature-independent contribution to the magnetic susceptibility. However, for small magnetic interactions a first analysis of the magnetic data can be done using an approximate approach26 where the RE(III) ions are considered as non-interacting, as discussed below.

The 4f⁰ electronic configuration of Sm(III) gives \(^{4}H_{{1/2}}\) as the ground term, which splits into six J-multiplets under the spin–orbit interaction and yields the multiplet with \( J = 5/2 \) as the ground state. Crystal fields lift the degeneracy of the J-manifolds, giving rise to Kramers doublets, and within the process also states belonging to different J-multiplets become mixed (the so-called crystal field J–J mixing). Since for Sm(III) the J-multiplets are closely spaced (10⁴ cm⁻¹) as compared to other rare-earth(III) ions, the crystal field J–J mixing is quite appreciable and thus its effect on the magnetic properties can be profound. As seen in Fig. 1a, the \( \chi _{M}T \) value of I measured at 300 K is 1.04 cm⁻¹K mol⁻¹, considerably higher than the theoretical value of 0.46 cm⁻¹K mol⁻¹ calculated on the basis of the free ion approximation taking only the \(^{4}H_{{3/2}}\) ground state into consideration (\( J = 5/2, \ g_{J} = 2/7 \) for Sm(III) and \( S = 1/2 \) and \( g = 2 \) for Mo(v)). It seems likely that the admixtures from the \(^{4}H_{{5/2}}\) excited multiplet within the \(^{4}H_{{3/2}}\) ground state multiplet are responsible for the observed difference. In fact, spin-relaxation studies performed on several Sm(III) compounds have shown that even small admixtures from the \(^{4}H_{{5/2}}\) level produce large effects, i.e. increases in the \( g_{\text{mag}} \) factors.27,28 When lowering the temperature, the \( \chi _{M}T \) value is seen to decrease smoothly, reaching a minimum value of 0.76 cm⁻¹K mol⁻¹ at ca. 20 K followed by a sharp increase to a value of 1.31 cm⁻¹K mol⁻¹ at 1.8 K. On the basis of literature data, one may expect the \( J = 5/2 \) multiplet to be split into three Kramers doublets, the distance of the two excited doublets being of the order of 100 K above the ground doublet. Lowering of the temperature

![Fig. 1](image-url)
will therefore produce a progressive depopulation of the excited levels and thus a temperature dependence of the $\chi_M T$ product. Based on the specific heat data presented below, we find indeed that at temperatures below ca. 20 K only the lowest Kramers doublet remains thermally populated. In addition, the already mentioned presence of the excited states arising from the $J = 7/2$ multiplet will entail a temperature-independent contribution to the magnetic susceptibility, i.e., an upward shift of the $\chi_M T$ vs. $T$ curve. The need for including such an additional contribution can be seen when comparing the experimental $\chi_M T$ vs. $T$ curve with the theoretical one based on the expression of $\chi_{\text{obs}}$ as a function of $\lambda$ reported previously, assuming a spin–orbit coupling parameter $\lambda = 210$ cm$^{-1}$, as typical for Sm(III), and the expected $\chi_M T$ value of 0.38 cm$^3$ K mol$^{-1}$ for Mo(V) (Fig. 1a). Finally, the abrupt increase in the $\chi_M T$ vs. $T$ curve at low temperature can be attributed to the magnetic exchange interaction between Sm(III) and Mo(V), as will be further discussed below.

Temperature-dependent magnetic susceptibility data of 2 are shown in Fig. 1b, likewise as plots of $\chi_M T$ vs. $T$ and $\chi_M$ vs. $T$. The $\chi_M T$ product measured at 300 K is 11.7 cm$^3$ K mol$^{-1}$, equal within errors to the expected value of 11.8 cm$^3$ K mol$^{-1}$ based on the non-interacting free-ion approximations ($J = 15/2$, $g_J = 1/5$ for Er(III) and $S = 1/2$ and $g = 2$ for Mo(V)). When the temperature is lowered, the $\chi_M T$ product gradually decreases and reaches the value of 6.55 cm$^3$ K mol$^{-1}$ at 1.8 K. The Er(III) ion with its electron configuration 4f$^{13}$ has the $^4$I$_{15/2}$ ground multiplet. The first excited state $^4$I$_{13/2}$ is located at about 6470 cm$^{-1}$ above the ground state and therefore its contribution to the magnetic susceptibility is only about 1% at room temperature and can be neglected. In crystal fields of low symmetry, the 16-fold degeneracy of the free ion is removed by the splitting of the ground multiplet in eight Kramers doublets over an energy range of the order of 500 K. Consequently, the gradual depopulation of the excited doublets can be held responsible for the observed variation in the $\chi_M T$ product with temperature. When fitting the $\chi_M$ data in the paramagnetic region ($T > 50$ K) to the Curie–Weiss law, the Curie constant and Curie–Weiss temperature are obtained as 12.2 cm$^3$ K mol$^{-1}$ and $-13.7$ K, respectively. The large Curie–Weiss temperature is clearly a result of the strong crystal field effects and should not be attributed to exchange interactions.

To get more insight in the type of magnetic interactions in 1 and 2, the field dependence of the magnetization was recorded at different temperatures in the range 1.8–8 K, as shown in Fig. 2 and 3. For 1, the measured curves are compared to the Brillouin function calculated for the non-interacting ions, with the expected spin $S = 1/2$ for Mo(V) and an effective spin of $S = 1/2$ for Sm(III) in view of the specific heat data to be discussed below. In agreement with the field-dependence observed for the magnetic specific heat, we have adopted a powder $g_{\text{Sm}}$ value of 0.6, which is in the range observed for Sm(III) in sites of low-symmetry. The ground multiplet of Sm(III), $^4$H$_{5/2}$, is split by a cubic crystal field into a doublet $\Gamma_7$ and a quartet $\Gamma_8$. In crystal fields of lower symmetry, the quartet $\Gamma_8$ splits into two Kramer doublets $\Gamma_5$ and $\Gamma_6$. Experimental determinations of the $g$-values for Sm(III) compounds have shown that the $\Gamma_6$ doublet is the ground state for the axial symmetry whilst for lower symmetry, i.e. monoclinic, the ground state is the $\Gamma_5$ doublet. In most cases, the average $g$-value is close to 0.6. As seen in the Fig. 2, the non-interacting limit describes the data at 8 K rather well. The data at 2 and 4 K show deviations attributable to weak magnetic interactions, to be further discussed below.
In the case of complex 2, from the magnetization curve taken at 1.8 K it appears that a field of ca. 3 T is sufficient to reach saturation of the magnetic moment of the Er(III) ground state, since the subsequent slow and nearly linear increase of the magnetization can be attributed to the contributions from the excited levels (Fig. 3a). Indeed, the slope of this high-field part gives $\chi = 0.28$ cm$^3$ mol$^{-1}$, about equal to the value measured in low fields at $T = 30$ K. By extrapolating the magnetization $M(B)$ measured at the higher fields ($B > 4$ T) to $B = 0$ we obtain the intercept $M^\text{total} = 4.4$ N$\beta$ (Fig. 3b). Since $M^\text{total} = M^I + M^M$ and $M^M = 1$ N$\beta$ we obtain an effective powder $g$ value of $g_{\text{eff}} = 6.8$ for the Er(III) ion when assuming only a lowest Kramers doublet with an effective spin $S = 1/2$ to be populated at 2 K for Er(III) ion (see the specific heat data below). This value agrees well with the presence of Er(III) in sites of low symmetry.$^{34,35}$

In Fig. 3b, we show the calculated Brillouin function for non-interacting Er(III) and Mo(V) ions at 1.8 K. The origin of the small deviations observed for the magnetization data measured at 1.8 K (with the high-field contribution of the excited levels subtracted) can likewise be ascribed to weak exchange effects, in this case between Er(III) and Mo(V) ions.

**Specific heat at very low temperatures**

Fig. 4a and 5a show the measured temperature dependence of the specific heat of 1 and 2 in the temperature range 0.3–25 K in zero field and in various applied magnetic fields. From the (field-independent) data above about 10 K and the zero-field curve down to about 7 K, the lattice contribution $C_l$ could be estimated and fitted to the simple Debye model, yielding a Debye temperature, $\theta_D$, of $51 \pm 2$ K for 1 and $49 \pm 2$ K for 2, respectively. Fig. 4b and 5b display the magnetic specific heat curves obtained by subtracting $C_l$ from the total specific heat. By integrating the $C_m$ data, we have calculated the magnetic entropies of 1 and 2, which are plotted as insets in Fig. 4b and 5b. As can be seen, the magnetic entropy, $\Delta S/R$, reaches the value of 1.36 J mol$^{-1}$ K$^{-1}$ for both. This value is equal, within the errors, to the theoretical value of $\Delta S/R = 2ln2 = 1.38$ J mol$^{-1}$ K$^{-1}$ expected for two spins $S = 1/2$, implying that the ground state of both Sm(III) and Er(III) ions is a doublet with effective spin $S = 1/2$.

As can be seen from the temperature range of the zero-field $C_m$ data in Fig. 4b and 5b, the magnetic exchange interactions ($J$) between Sm(III) or Er(III) with Mo(IV) are rather weak, in particular for Er(III). Nevertheless, they are clearly discernable in the specific heat, leading to broad anomalies with maxima at 1.4 K and 0.7 K for 1 and 2, respectively. In view of the chain-like crystal packing, these broad anomalies can be ascribed to short-range magnetic correlations along the chains, as typically observed for 1D magnetic systems. In addition, compound 1 is found to display a $\lambda$-type peak at $T_c = 0.60$ K under zero-field, which can be attributed to a cooperative transition to a 3D ordered magnetic arrangement resulting from weak interchain interactions. Since no direct superexchange paths connecting magnetic ions in neighbouring chains can be discerned in the crystal structure, such interchain interactions are most likely of dipolar origin and thus quite weak.

The specific type of magnetic exchange interaction ($J / k_B$) along the 1D chains in 1 and 2 is governed by the intrinsic anisotropic properties of the Sm(III) and Er(III) magnetic ground states.

**Specific heat at very low temperatures**

![Figure 4](image-url) (a) Molar heat capacity of 1 as measured in zero field and in constant magnetic fields up to 7 T. Solid curve shows the estimated (field-independent) lattice contribution. (b) Magnetic heat capacity of 1 as obtained by subtracting the lattice contribution (Inset: magnetic entropy curves obtained by integration of the magnetic heat capacity).

Since the shape and the height of the specific heat maximum ($C_m^\text{max}$) are sensitive to the type of anisotropy, a determination of the type of 1D chain can be done by comparison of the magnetic specific heat anomalies as measured in zero field with theoretical predictions for the various model Hamiltonians (Ising, XY, Heisenberg and intermediate symmetries).$^{36}$ The observed heights of the specific heat maxima for 1 and 2 are equal to 0.80 $R$ and 0.64 $R$, respectively, occurring at $T_m = 1.33$ K and 0.65 K, respectively. When comparing with the calculations of Blöte$^{37}$ for magnetic chain models with different symmetry of interaction, it appears that the antiferromagnetic chain model with $S = 1/2$ and intermediate Ising–Heisenberg symmetry of the interaction provides the best description of the observed anomaly of compound 1 (Fig. 6a). The appropriate spin-Hamiltonian reads:

$$H = - 2 \sum \{ J_{\parallel} \{ S_n S_n + S_{n+1} S_{n+1} \} + J_{\perp} S_n S_{n+1} \}$$

The ratio of the exchange constants $J_{\parallel}$ and $J_{\perp}$ found from the fit is $J_{\parallel} / J_{\perp} = 0.3$. From this comparison we estimate a value of the antiferromagnetic exchange interaction of $J_{\parallel} / k_B = -2.6$ K. On the other hand, as shown in Fig. 6b, the magnetic specific heat of 2 can be fitted quite well to the theoretical prediction$^{38}$ for the (pure) XY linear chain model ($J_{\parallel} \neq 0, J_{\perp} = 0$), leading to $| J_{\parallel} | / k_B = 1.0$ K. This
planar anisotropy agrees with the symmetry of the $g$-tensor often observed for Er(III). For instance, EPR studies on different Er(III) compounds have shown that the $g$-values are highly anisotropic with mostly $g_\parallel < g_\perp$ and an average $g$-value equal to $7.37-40$. Since the symmetry of the interaction can be roughly related to that of the $g$-tensor by the expression:

$$J_{\parallel}/k_B \propto (g_{\parallel}/g_\perp)^2$$

the strong XY symmetry demonstrated by the specific heat anomaly would be well explained. We remind that for the pure XY model the specific heat is the same for ferro- or antiferromagnetic $J_\parallel^-$ so that the sign of $J_\parallel^-$ remains to be determined.

With regards to the in-field data, a detailed quantitative analysis in terms of these theoretical models is not possible since in the experiment we are not dealing with equal magnetic moments ($gS$) at all chain sites but with ferrimagnetic chains due to the non-equivalent RE(III) and Mo(V) $g$-values. In addition, only powder data are available, so that the experimental field-dependent properties are averages over non-equivalent crystallographic directions. Nevertheless, a rough qualitative analysis can be done for the case of the Er(III)–Mo(V) (compound 2), for which the Zeeman energies corresponding to the applied fields of 3 T and 5 T are (relatively) large compared to the exchange interaction. As described previously,\textsuperscript{25} we can then try to analyze the in-field specific heat data in terms of a mean-field model, in which the total splitting $\Delta_{\text{tot}}$ of each doublet is the addition of the Zeeman splitting, $D_Z = g_b B_{\text{appl}}$ due to the applied field $B_{\text{appl}}$, and the exchange splitting $D_{\text{ex}} = 2S|J|/g_b$ due to the exchange interaction $J/k_B$ interpreted in terms of an exchange field:

$$B_{\text{ex}} = 2S|J_\perp|/g_b = \Delta_{\text{tot}}/g_b$$

(2)

Since for all ions involved $S = 1/2$, the number of magnetic neighbours along the chain is $z = 2$ and $\beta/k_B = 2/3 \times K/T$, these formulae reduce to

$$\Delta_\perp/k_B = 2|J_\perp|/\beta$$

(3)

and

$$\Delta_{\text{tot}}/k_B = 2|J_\perp|/\beta$$

(4)

Each split doublet will contribute a two-level Schottky anomaly to the specific heat, with different splitting factors $g_{\text{RE}}$ and $g_{\text{Mo}}$ for the $\Delta_\parallel/k_B$ of RE(III) and Mo(V), whereas $\Delta_{\text{tot}}/k_B \approx 2 K$ for $|J_\parallel|/k_B \approx 1 K$, independent of the $g$-value. We show in Fig. 7 the fit for compound 2 for the data collected at 5 T obtained by subtracting an exchange field $B_{\text{ex}} = -\Delta_{\text{tot}}/g_b$ from the applied field values, corresponding to $-3/7 T$ for Er(III) taking $g_{\text{Er}} = 7,
studied RE(III)–Mo(V) chains, it is of dipolar origin, corresponding to an interaction of strength \( J_\parallel \). A similar analysis for the Sm(III)–Mo(v) (compound 1) is not useful since the condition \( \Delta_2 \ll \Delta_m \) needed for applying the model is not reached even in highest field due to the larger value of \( J/k_B \).

Finally, in order to estimate the effects of the weak interchain coupling (\( J' \)), we will assume that, similar as for the previously studied RE(III)–Mo(v) chains, it is of dipolar origin, corresponding to an interaction of strength \( J'/k_B = 0.02 \) K. To estimate the 3D ordering temperature \( T_c \), resulting from such an interaction, we adopt the well known mean-field formula:

\[
k_B T_c = \xi_{\parallel}(T_c) J' S^2
\]

where \( \xi_{\parallel}(T) \) is the magnetic correlation length along the individual magnetic chains. The argument basically equates the thermal energy at the transition temperature with the interaction energy at \( T = T_c \) of a reference spin with a correlated spin segment in the adjacent chain. In the case of compound 1, with its Ising-like character, we take for the intrachain correlation length the Ising prediction:

\[
\xi_{\parallel}(T) = (1/k_B T) \exp(J/k_B T)
\]

Taking \( J/k_B = 2.6 \) K and \( S = 1/2 \) one obtains \( T_c = 0.6 \) K, just equal to the experimental value. For the XY chain compound 2, we use instead the prediction for the pure XY chain: \( \xi_{\parallel}(T) = J/k_B T \) (again for \( S = 1/2 \)), leading with \( J/k_B = 1 \) K to the estimate \( T_c = 0.07 \) K, i.e. far below the lowest temperature reached in our specific heat measurements. The fact that the \( T_c \) is so much higher for compound 1 can thus be clearly attributed to the exponential temperature dependence of \( \xi_{\parallel}(T) \) characteristic for an Ising-type chain. This simple argument clearly explains why the presence of 3D ordering was only observed in the case of compound 1, in spite of the close similarities between the two materials in other respects.

Conclusions

We have synthesized two new 1D cyanido-bridged coordination polymers based on \([\text{Re}((pmzam)_3(H_2O)]^{2+} (\text{RE} = \text{Sm(III)}, \text{Er(III)}) and \([\text{Mo(CN)}_6]^{2-}\) fragments and studied their magnetic properties in detail. The field-dependent magnetization and specific heat measurements at low temperatures reveal the presence of antiferromagnetic superexchange interactions between the RE(III) and Mo(v) ions, of magnitude \( J/k_B = -2.6 \) K and Ising–Heisenberg symmetry of the interaction \( (J//J_\perp = 0.3) \) for RE = Sm and \( J/k_B = -1.0 \) K and a strong XY-type (planar) anisotropy for RE = Er(III).

Further work on the investigation of the magnetic properties of isostuctural compounds in this series containing W(v) is currently in progress.

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Notes and references
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