Rhombic Coulomb diamonds in a single-electron transistor based on an Au nanoparticle chemically anchored at both ends

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Rhombic Coulomb diamonds are clearly observed in a chemically anchored Au nanoparticle single-electron transistor. The stability diagrams show stable Coulomb blockade phenomena and agree with the theoretical curve calculated using the orthodox model. The resistances and capacitances of the double-barrier tunneling junctions between the source electrode and the Au core (R1 and C1, respectively), and those between the Au core and the drain electrode (R2 and C2, respectively), are evaluated as 4.5 MΩ, 1.4 aF, 4.8 MΩ, and 1.3 aF, respectively. This is determined by fitting the theoretical curve against the experimental Coulomb staircases. Two-methylene-group short octanethiols (C8S2) in a C8S2/hexanethiol (C6S) mixed self-assembled monolayer is concluded to chemically anchor the core of the Au nanoparticle at both ends between the electroless-Au-plated nanogap electrodes even when the Au nanoparticle is protected by decanethiol (C10S). This is because the R1 value is identical to that of R2 and corresponds to the tunneling resistances of the octanethiol chemically bonded with the Au core and the Au electrodes. The dependence of the Coulomb diamond shapes on the tunneling resistance ratio (R1/R2) is also discussed, especially in the case of the rhombic Coulomb diamonds. Rhombic Coulomb diamonds result from chemical anchoring of the core of the Au nanoparticle at both ends between the electroless-Au-plated nanogap electrodes.

1. Introduction

Formation of a functional structure of a desired texture on the subnanometer scale is a primary concern in the design of nanodevices such as single-electron and molecular devices.1–4 A molecule-based chemical assembly technique is one of the candidate methods for realizing subnanometer-scale formation, as molecules have unique structures and can be used as building blocks.4,5 Despite their simple structures, alkane-thiols and alkanedithiols consisting of alkyl chains and thiols groups have been extensively studied in both electronics and photonics fields.6–8 It is well known that the thiol groups in these molecules can be chemically bonded onto the surfaces of metal electrodes. Further, their tunneling resistance depends on the chain lengths of the alkyl units; therefore, they are strong candidates for use as building blocks in nanodevices.4,9–11

Single-electron transistors (SETs) have been studied extensively as prospective nanodevices because of their potential for low power consumption and high charge sensitivity.12–18 In SETs, a quantum dot is electrically connected to the two reservoirs of the source (S) and drain (D) electrodes as a Coulomb island, to form double-barrier tunneling junctions (DBTJs). The gate electrode is located near the Coulomb island to control the offset charge of the quantum dot using the gate voltage VG. The drain current (ID) flows between the S and D electrodes by way of the Coulomb island. The drain current–drain voltage (ID–VD) characteristics of the SETs involve the Coulomb blockade region, where the current flow is restricted even under the application of VD, and exhibit a Coulomb staircase profile. These characteristics are described by the orthodox model, that is governed by tunneling rates and master equations for DBTJs.10,14,19 The I0–VD characteristics can be calculated by considering the following five parameters: the capacitance between the source and the Coulomb island (C1) and that between the Coulomb island and the drain (C2), the tunneling resistance between the S electrode and the Coulomb island (R1), and that between the Coulomb island and the D electrode (R2), and the offset charge (Q0).10,19–21 These five parameters can be evaluated by fitting the theoretical curves...
obtained from the orthodox model to the experimental $I_D-V_D$ characteristics.\textsuperscript{10,19} Over the past two decades, many SET structures have been realized, based on top-down silicon techniques and two-dimensional electron gases of GaAs-based materials, for example.\textsuperscript{22–29} SETs have also been fabricated by combining top-down and bottom-up technologies.\textsuperscript{30–39}

Recently, we have demonstrated the fabrication processes for chemically assembled SETs consisting of electroless-Au-plated nanogap electrodes\textsuperscript{40–42} covered by alkanethiol- and alkanedithiol-mixed self-assembled monolayers (SAMs),\textsuperscript{8,10,43,44} with chemically anchored Au nanoparticles\textsuperscript{20,45–47} positioned between the nanogap electrodes. Chemically assembled SETs exhibit ideal and reproducible Coulomb diamonds,\textsuperscript{48–50} uniform and controllable charging energy $E_C$,\textsuperscript{48,51–53} discrete Au nanoparticle energy levels,\textsuperscript{54} adoption of SiNx passivation,\textsuperscript{55} and all the two-input logic operations.\textsuperscript{56} The robustness of the chemically assembled SETs is extremely high, for instance, the gate voltage of $\pm 12$ V is available.\textsuperscript{48} The structures of these SETs have been discussed in terms of the values of the five parameters determined from the experimental Coulomb diamonds. In particular, $C_1$ and $C_2$ have been found to be dependent on the diameter of the Coulomb island and to agree with a concentric sphere model.\textsuperscript{51}

On the other hand, $R_1$ and $R_2$ have been analyzed in a step-by-step manner as follows: in the case of a physisorbed Au nanoparticle on an Au electrode surface, the tunneling resistance between the Au core and the Au electrodes was found to be identical to that of a chemically bonded alkanethiol protecting molecule on an Au core surface using scanning tunneling spectroscopy (STS) measurements. These tunneling resistances were evaluated as 460 M$\Omega$ and 7.6 G$\Omega$ on hexanethiol (C6S) and octanethiol (C8S), respectively. This indicates an increase of one order of magnitude in the tunneling resistance with increasing alkyl chain length in a two-methylene group.\textsuperscript{4,8,10,20,57,58} In the case of our SETs consisting of a decanethiol (C10S)-protected Au nanoparticle and electroless-Au-plated nanogap electrodes, the C10S-protected Au nanoparticles were chemisorbed by the use of the decanedithiol (C10S2) anchor molecule in a C10S2/S8S mixed SAM on the surfaces of electroless-Au-plated nanogap electrodes. In the case of an Au nanoparticle single-side chemisorbed by a C10S2 anchor molecule, the typical resistance of the chemisorbed nanoparticles between the Au core and the Au(111) substrate was measured at 1.2 G$\Omega$.\textsuperscript{48} As reduction in the tunneling resistance is key to improving the SET signal-to-noise, it is important to attempt to shorten the chain length of the anchor molecule.

In this study, we demonstrate rhombic Coulomb diamonds on a chemically assembled SET consisting of a C10S-protected Au nanoparticle anchored by octanedithiol (C8S2) between the electroless-Au-plated nanogap electrodes. The adsorption of the Au nanoparticle is discussed in terms of the values of resistances and capacitances of the DBTJs between the Au core and the S/D electrodes. The tunneling resistance ratio ($R_1/R_2$) dependence of the Coulomb diamond shapes is also discussed.

2. Results and discussion

Fig. 1(a) shows the equivalent circuit of a fabricated SET with two side-gate (G1 and G2) electrodes, while Fig. 1(b) is a scanning electron microscopy (SEM) image of the SET. A single
bright spot can be confirmed between the S and D electrodes in the SEM image. Fig. 1(c) shows the candidate schematic diagram of the SET with the top view perspective. Chemical anchoring of the core of the Au nanoparticle between the electroless-Au-plated nanogap electrodes is discussed as follows. Fig. 2(a) shows the experimental $I_D$-$V_D$ characteristics under the application of $G_1$ voltage ($V_{G1}$) = 0 and 3.2 V, which correspond to the on and off states ($Q_0$ = 0.5 e and 0) of the SET, respectively. The experimental $I_D$-$V_D$ characteristics were fitted against theoretical curves, and agree with the theoretical curve obtained for the parameters $R_1$ = 4.5 MΩ, $R_2$ = 4.8 MΩ, $C_1$ = 1.4 aF, and $C_2$ = 1.3 aF. Note that $R_1$ and $R_2$, and $C_1$ and $C_2$, were almost equivalent.

Fig. 2(b) shows the experimental $I_D$-$V_{G1}$ characteristics under the application of $V_{D}$ = 14, 28, 42 and 50 mV. Clear and stable Coulomb oscillations were observed. Theoretical curves were calculated using the same $R_1$, $R_2$, $C_1$, and $C_2$ parameters as above, with the $G_1$ capacitance ($C_{G1}$) being 0.025 aF. The theoretical curves in Fig. 2(a) (dashed lines) also agree with the experimental results. In Fig. 2(b), the experimental $I_D$-$V_{G1}$ characteristics were symmetric at the axis of $V_{G1}$ = 0. These symmetric Coulomb oscillations originated from the same $R_1$ and $R_2$.24

![Figure 2](image)

**Fig. 2** (a) Experimental $I_D$-$V_D$ characteristics under applied $V_{G1}$ = 0 and 3.2 V at $T$ = 9 K. Theoretical $I_D$-$V_D$ characteristics (dashed lines) are also shown. Here, $Q_0$ = 0.5 e for $V_{G1}$ = 0 and $Q_0$ = 0 for $V_{G1}$ = 3.2 V. (b) Experimental $I_D$-$V_{G1}$ characteristics under applied $V_D$ = 14, 28, 42, and 50 mV. The theoretical characteristics calculated for $Q_0$ = 0.5 e are also shown. In (a) and (b), the common parameters for the theoretical calculation are: $R_1$ = 4.5 MΩ, $R_2$ = 4.8 MΩ, $C_1$ = 1.4 aF, $C_2$ = 1.3 aF, and $T$ = 9 K.

Next, we consider the Coulomb oscillation dependence on $R_1/R_2$. Fig. 3(a) shows the $R_1/R_2$ ratio dependence of the theoretical $I_D$-$V_{G1}$ curves under the application of $V_D$ = 28 mV, which was almost half the Coulomb-diamond peak voltage. The value of $R_2$ was adjusted to yield $R_1/R_2$ ratios within the 0.001–1000 range, with $R_1$ = 4.5 MΩ, $C_1$ = 1.4 aF, $C_2$ = 1.3 aF, and $C_{G1}$ = 0.025 aF. $I_D$ was normalized by the maximum current $I_{peak}$. At $R_1/R_2$ = 1, the symmetric Coulomb oscillation at the $V_{G1}$ = 0 axis was observed. In contrast, the $I_D/I_{peak}$ Peak voltages negatively and positively shifted under $R_1 < R_2$ and $R_1 > R_2$ conditions, respectively, however, the current rising and falling $V_{G1}$ voltages did not change, as the Coulomb blockade break voltages are defined by $C_1$ and $C_2$.10,19 Fig. 3(b) shows the $V_{G1}$ peak shift ($\Delta V_{G1}$, illustrated in Fig. 3(a)) dependence on the $R_1/R_2$ ratio under various $V_D$. From this calculation, the large difference between $R_1$ and $R_2$ as well as the large $V_D$ resulted in large $\Delta V_{G1}$. The difference between $R_1$ and $R_2$ means that the adsorption condition of the Au nanoparticle between the S and D electrodes was asymmetric. Therefore, chemical anchoring of Au nanoparticles onto both the S and D electrodes resulted in symmetric $I_D$-$V_{G1}$ characteristics.

![Figure 3](image)

**Fig. 3** (a) $I_D$-$V_{G1}$ calculated for varying $R_1/R_2$ ratios under applied $V_D$ = 28 mV. Here, $I_D$ is normalized by $I_{peak}$, and $V_{G1}$ is normalized by the Coulomb oscillation period ($\Delta$). The following parameters are used: $C_1$ = 1.4 aF, $C_2$ = 1.3 aF, $C_{G1}$ = 0.025 aF, $R_1$ = 4.5 MΩ, and $T$ = 9 K. (b) $\Delta V_{G1}$ dependence on the $R_1/R_2$ ratio under various $V_D$.
can be evaluated from the shape of the Coulomb diamonds.\(^\text{12}\) From the boundary slopes of the diamonds and the gate voltage difference between neighboring diamonds, \(C_1\), \(C_2\), \(C_{G1}\), and \(C_{G2}\) were evaluated as 1.4, 1.3, 0.025 and 0.015 aF, respectively. The \(C_1\) and \(C_2\) values obtained from Fig. 4(a) and (b) agree with the values obtained from the theoretical fitting shown in Fig. 2(a). Note that the Coulomb diamond shapes are primarily determined by \(C_1\), \(C_2\), \(C_{G1}\), and \(C_{G2}\), as reported in a previous study.\(^\text{12}\) For the majority of the experimentally reported Coulomb diamonds, including those in our previous reports, the diamonds were parallelograms rather than rhombuses, because of differences between \(C_1\) and \(C_2\).\(^\text{48,49,54–56}\) In contrast, comparable \(C_1\) and \(C_2\) result in the almost rhombic diamond shapes apparent in Fig. 4(a) and (b).

Compared with the diamond shapes, the external regions of the Coulomb diamonds are also noteworthy. In our previous reports, the conductance peak lines along the edges of the Coulomb diamonds were extrapolated outside the diamonds.\(^\text{48,51,54,56}\) In contrast, the experimental Coulomb diamonds in Fig. 4(a) and (b) did not exhibit such extrapolated conductance peak lines. Besides the conductance peak lines, higher conduction regions were observed near the Coulomb diamond vertexes, such as \(V_D = 0.07\) V and \(V_{G1} = 3.2\) V in Fig. 4(a). This difference cannot be explained by consideration of the capacitance values.

Previously, we have measured the Coulomb staircases in DBTJs consisting of a scanning-probe/vacuum-gap/alkanethiol-protected Au nanoparticle/Au(111) electrode as a function of the set point current using scanning tunneling spectroscopy,\(^\text{10}\) demonstrating that the Coulomb staircase profiles depend on \(R_1/R_2\). This result indicates that not only the Coulomb staircase profiles, but also those of the stability diagrams depend on the \(R_1/R_2\) ratio. Fig. 5(a) shows the stability diagrams (\(dI_D/dV_D\) plots) calculated for \(R_1 = 4.5\) M\(\Omega\), \(R_2 = 4.8\) M\(\Omega\), \(C_1 = 1.4\) aF, \(C_2 = 1.3\) aF, \(C_{G1} = 0.025\) aF, and \(Q_0 = 0.5e\) at a temperature \((T)\) of 9 K. The theoretical stability diagram agrees with the experimental stability diagram shown in Fig. 4(a). Fig. 5(b) shows the

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**Fig. 4** Experimental stability diagrams obtained by plotting color maps of \(dI_D/dV_D\) for the fabricated SET as functions of (a) \(V_D\) and \(V_{G1}\) and (b) \(V_D\) and \(V_{G2}\). Both measurements are carried out at \(T = 9\) K.

**Fig. 5** Theoretical stability diagrams calculated under different \(R_2\) of: (a) 4.8 M\(\Omega\) \((R_2 = R_1)\), (b) 22.5 M\(\Omega\) \((R_2 = 5R_1)\), and (c) 0.90 M\(\Omega\) \((R_2 = \frac{1}{5}R_1)\). The other parameters: \(R_1 = 4.5\) M\(\Omega\), \(C_1 = 1.4\) aF, \(C_2 = 1.3\) aF, \(C_{G} = 0.025\) aF, \(Q_0 = 0.5e\) and \(T = 9\) K, are identical for (a)–(c).
stability diagram calculated using the same parameters in Fig. 5(a), except \( R_2 = 5R_1 (= 22.5 \text{ M} \Omega) \). Under this condition, higher conduction regions were not observed near the Coulomb diamond vertexes, but downward conductance peak lines were extrapolated along the Coulomb diamond edges. Fig. 5(c) shows the theoretical stability diagram calculated for the same parameters of Fig. 5(a), except \( R_2 = 0.2R_1 (= 0.90 \text{ M} \Omega) \). Under this condition, conductance peak lines extrapolated upward along the Coulomb diamond edges were observed. Consequently, the shapes of the SET stability diagrams are strongly dependent on \( R_1/R_2 \).

In general, the tunneling resistances of \( R_1 \) and \( R_2 \) are exponentially proportional to the tunneling distance between the Au core and the S/D electrodes, in contrast, the capacitances \( C_1 \) and \( C_2 \) are approximately inversely proportional to the distance between the Au core and the S/D electrodes. When \( R_1 \) becomes comparable to \( R_2 \) as shown in Fig. 5(a), the distance between the Au core and the surface of the source electrode is equal to that between the Au core and the surface of the drain electrode. Due to these two different dependences against the distance, the comparable \( R_1 \) and \( R_2 \) results in comparable \( C_1 \) and \( C_2 \), since the shape of the Au nanoparticle is spherical. It is also noted that the comparable \( C_1 \) and \( C_2 \) does not always result in the comparable \( R_1 \) and \( R_2 \). Consequently, rhombic Coulomb diamonds result from chemical anchoring of the Au core by octanediolthiols at both the ends between the electroless-Au-plated nanogap electrodes.

In our previous chemically assembled SETs, a C10S2/C8S mixed SAM was used to anchor a C10S-protected Au nanoparticle and different \( R_1 \) and \( R_2 \) pair values were observed. In contrast, here we used a C8S2/C6S mixed SAM to anchor a C10S-protected Au nanoparticle to reduce the tunneling resistances. As a result, equal and smaller \( R_1 \) and \( R_2 \) of 4.5 and 4.8 M\( \Omega \), respectively were obtained. Fig. 6 shows the SEM images of C10S-protected Au nanoparticles on a C8S2/C6S mixed SAM/Au substrate. The C8S2/C6S mixed SAM/Au substrate fabrication method and the Au nanoparticle solution immersion time were identical to those of the SETs. In this case, the Au nanoparticle density was 88 per 100 \( \times \) 100 nm\(^2\). We have previously reported the anchoring of a C10S-protected Au nanoparticle by a C10S2 molecule within C10S2/C8S SAMs using STM and STS measurements, with a density of 22 per 100 \( \times \) 100 nm\(^2\).\(^6\) It should be noted that the density of the C8S2-anchored C10S-protected Au nanoparticles is of the same order of magnitude as the C10S2-anchored C10-protected Au nanoparticles, even if the alkyl chain length of the anchor molecule is shorter than that of the protecting molecule. The values of the tunneling resistances (4.5 M\( \Omega \)) are comparable to that of the resistance of C8S2 on Au electrodes, as measured using an Au-coated atomic force microscopy tip.\(^8\) Due to the two thiol groups in C8S2, the molecular length of C8S2 as the anchor molecule becomes almost the same as that of C10S as the protecting group of the Au nanoparticle. Consequently, as shown in the top view schematic diagram of Fig. 1(c), two-methylene-group short C8S2 in a C8S2/C6S mixed self-assembled monolayer is concluded to chemically anchor the core of the Au nanoparticle at both ends between the electroless-Au-plated nanogap electrodes even when the Au nanoparticle is protected by C10S. Moreover, the tunneling resistance decreased through use of the C8S2 anchor molecule, with the value being more than one order of magnitude less than in the case involving C10S2 anchoring. Because of this improved fabrication process, rhombic Coulomb diamonds were demonstrated. The availability of the two-methylene-group shorter anchoring molecule is significant for the applications of chemically assembled SETs, as lower and more stable tunneling resistance can be obtained.

3. Experimental

We used electron beam lithography and a lift-off process to fabricate the initial Ti (2 nm)/Au (10 nm) electrode patterns, comprising S, D, G1 and G2 electrodes on a SiO\(_2\) (50 nm)/Si substrate. Prior to the electroless Au plating, the initial Au electrodes were cleaned using O\(_2\) plasma treatment. Probing electrodes of 150 \( \times \) 150 \( \mu \text{m}^2 \) area were then added via photolithography, and electroless plating in an Au iodine solution reduced the nanogap sizes via a self-termination reaction.\(^{10-42}\) The nanogap electrodes were immersed in a 1 mM hexanethiol [\( \text{CH}_3(\text{CH}_2)_5\text{SH}, \text{C6S} \)] solution in ethanol for 12 h to allow the formation of the C6S self-assembled monolayers (SAMs); the electrodes were then rinsed with ethanol twice. Subsequently, the sample was immersed in a 1 mM octanediolthiol [\( \text{HS}(\text{CH}_2)_8\text{SH}, \text{C8S2} \)] solution in ethanol for 12 h to yield C8S2/C6S mixed SAMs. It was then rinsed with ethanol twice.\(^8\) After the substitution, the sample was immersed in a solution of decanethiol [\( \text{CH}_3(\text{CH}_2)_10\text{SH}, \text{C10S} \)]-protected Au nanoparticles with a core diameter of 6.2 \( \pm \) 0.8 nm in toluene for 12 h. It was then rinsed with toluene twice. The electrical measurements were conducted using a semiconductor parameter analyzer (Agilent B1500, USA) in a vacuum (\( \sim 10^{-5} \text{ Pa} \)) at 9 K (in a helium refrigerator, Nagase GRAIL10-LOGOS01S, Japan). The experimental differential conductances \( dI/dV_\text{g} \) were numerically calculated based on the experimental \( I_\text{T}-V_\text{D} \) characteristics.
4. Conclusions

We have demonstrated rhombic Coulomb diamonds in a chemically anchored Au-nanoparticle SET consisting of a C10S-protected Au nanoparticle anchored by C8S2 molecules at both ends of an electroless-Au-plated nanogap. The $I_D-V_D$ characteristics showed Coulomb blockade phenomena and agree with the theoretical fitting curve calculated using the orthodox model. The evaluated $R_1$ and $R_2$ were almost identical, at 4.5 and 4.8 MΩ, respectively, and are attributed to the tunneling resistance of the chemisorbed octanethiol at both ends. The experimental stability diagram agreed with the theoretical calculation with $R_1$, $R_2$, $C_1$, and $C_2$ being evaluated from the $I_D-V_D$ characteristics. The changes in the stability diagrams for $R_1 \approx R_2$ (double-anchored Au nanoparticle), $R_1 > R_2$, and $R_1 > R_2$ (single-anchored Au nanoparticle) were discussed. In the stability diagrams, identical $R_1$ and $R_2$ did not yield extrapolated conductance peak lines. In contrast, different $R_1$ and $R_2$ corresponded to asymmetric adsorption, as indicated by the extrapolated conductance peak lines. The realization of a symmetric chemically anchored Au nanoparticle between S and D electrodes is significant, as it yields rhombic Coulomb diamonds.

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References

1 M. Ratner, Nat. Nanotechnol., 2013, 8, 378–381.


