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# Celebrating Soft Matter's 10th Anniversary: Simplicity in complexity – towards a soft matter physics of caramel†

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Caramel is a mixture of sugars, milk proteins, fat and water cooked at high temperatures to initiate Maillard reactions. We study caramels as 'active emulsion-filled protein gels', in which fat droplets are chemically-bonded to a background gel matrix of cross-linked proteins in a concentrated aqueous sugar solution. We delimit a 'caramel region' in composition space. Oscillatory rheology within this region reveals that we can superpose the mechanical spectra of our caramels into a single pair of $G'(\omega), G''(\omega)$ master curves using time-composition superposition (tCS) over 12 decades of frequency, so that these caramels are instances of an underlying 'universal material'. This insight constrains the molecular mechanisms for structure formation, and implies that measuring a couple of parameters suffices to predict the rheology of our caramels over 12 orders of magnitude in frequency.

## 1 Introduction

Long before this journal was founded, a major review drew attention to food as soft matter.[1] When this journal was five, it published an internet theme issue on food. One of the two reviews in this issue[2] says that '[a]n increasing number of food physicists now recognize the potential of soft condensed matter physics to understand ... food structure.' Viewing food 'as soft matter with some universality at the level of its structure' is sometimes known as 'molecular gastronomy'.[2]

'Foods ... possess an enormous amount of complexity.'[3] so that most soft matter studies focus on one or two ingredients. Thus, the 2008-09 theme issue dealt with $\beta$-lactoglobulin aggregation[4] and protein-polysaccharide interactions in emulsions.[5] One article only treated an entire food product: the effect of fat crystals on chocolate microstructure.[6]

Caramel is a widely-used confectionary product, second only perhaps to chocolate, but in terms of scientific scrutiny, it is the Cinderella material. Searching for 'chocolate' in the Web of Science returned well over 34,000 records, while 'caramel' returned barely 5,000, probably because chocolate is, in essence, a simpler material. Molten chocolate is basically a suspension of sucrose grains in oil.[7] By contrast, caramel[8] is irreducibly a mixture of sugars, proteins, fat and water structured at high temperatures (ca. 120 °C).

Given these complexities, it may be thought that a coarse-grained 'soft matter approach' may have little to contribute. However, in this work, we offer a case study of how judiciously-designed experiments coupled with the right questions asked of the data may nevertheless enable progress to be made.[3] We start from a recipe for a 'standard model caramel', and first enquire how much the composition could be varied for the material to still remain caramel-like. Performing rheology on the set of caramels so obtained then leads to the emergence of a surprisingly simple, coarse-grained picture, which sets constraints on possible molecular mechanisms.

## 2 Caramel: a soft-matter hypothesis

Caramel is made by cooking different proportions[8] of sugars, milk proteins, vegetable fat and water at $T \sim 120\,^{\circ}$C. Most of the sugar is from glucose (or 'corn') syrup, which is a mixture of glucose and its oligomers. The milk proteins[9] are mostly caseins or whey. Native casein occurs as micelles,[10] while $\beta$-lactoglobulin (BLG) is the main component of whey. The fat is typically solid at room temperature. There are few, if any, scientific reports on the bulk structure of caramel (although caramel surfaces have been imaged[11]); but very general considerations of the ingredients and their interactions suffice for formulating a starting hypothesis.

It is known that at $T \gtrsim 60\,^{\circ}$C, milk proteins start to denature and aggregate via exposed hydrophobic groups and/or thiol/disulphide exchange reactions,[12] although processes at $T \gtrsim 120\,^{\circ}$C are less studied.[13] Sugars typically stabilise proteins against heat denaturation,[14] though some claim the opposite.[15] At $T \sim 120\,^{\circ}$C, Maillard reactions[16] give rise to sugar-mediated protein cross-linking. Separately, milk proteins are known to stabilise oil (= molten fat) droplets.[17]

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This information, though incomplete, suggests that caramel is a dispersion of protein-stabilised fat droplets in a protein gel whose solvent is a concentrated aqueous sugar solution. Two distinct types of such 'emulsion-filled protein gels' [18] exist, depending on whether the 'filler' droplets or particles are chemically bonded to the gel network ('active') or not ('inactive'). An active filler strengthens the gel, while a passive one weakens it. [19] Whey proteins, which presumably are the main emulsifier of the fat, [17] can cross-link with caseins, which is the major protein in our work. Thus, we hypothesise that *caramel is an active emulsion-filled protein gel*.

## 3 Materials and methods

To synthesise our 'standard model caramel' (SMC), we began by preparing 200 g of a 'premix' consisting of 39.4% of glucose syrup (dry weight, available from Tate & Lyle), 0.5% table salt, 13.9% palm derivative (available from Archer Daniels Midland Company), 22.7% water, 2.96% micellar casein (courtesy of Prof György Babella, Hungarian Dairy Research Institute), 0.74% whey protein isolate (WPI, BioPro), and 19.7% sucrose (Silverspoon)*. First the sucrose, milk proteins and water were combined to form a sweetened condensed skim milk (SCSM) then the remaining ingredients were added and emulsified.

This 'premix' was heated to and held at 90 °C for 10 min, and then to and held at 120 °C until 23 g of water had been boiled off. Finally, the caramel was poured onto greaseproof paper, cooled for ≈ 10 min and then stored in a sealed petri dish in a humidity chamber. This protocol produced a caramel with 15.7% oil and 84.3% continuous phase; the latter is made up of 80% sugar, 5% protein and 15% water. We explored composition space by varying the proportions of these ingredients and the boiling off time.

Constant scraping and stirring was needed during cooking to prevent sticking and ensure homogenisation. We constructed bespoke equipment to do this reproducibly, Fig. 1. A 500 ml cylindrical cooking vessel (height 14.5 cm) is tightly fitted within an aluminium jacket with embedded heating resistors. Heating is controlled by a programmable three-term (proportional-integral-differential, PID) controller via a thermocouple in the jacket. A second thermocouple in the cooking vessel monitors the caramel. An overhead mixer actuates a blade shaped to scrape the edges of the cooking vessel (gap ≈ 3 mm) and notched to fit the second thermocouple. The drop in viscosity at 90 °C allows us to increase the initial stirring rate of 50 rpm to 250 rpm for the final stage of the boil off, which is monitored by placing the apparatus on a balance.

Rheology was performed in a TA-DHR-2 hybrid rheometer. A smooth, truncated cone-plate geometry (40 mm radius, 1°) was used to study syrup-sucrose solutions, while 40 mm radius hatched plates (1 mm gap) were used for caramels to reduce slip. Temperature was held at 20 °C using a Peltier element and equilibrated for 10 min before measurements. For each experiment, ≈ 2 g of caramel was squeezed between the plates and the excess trimmed from the edge before fitting a solvent trap to minimised evaporation. We measured the storage and loss moduli, $G'(\omega)$ and $G''(\omega)$, of caramel using small-amplitude oscillatory shear (SAOS) rheology in the frequency range $f = \omega/2\pi = 0.01$ to 100 Hz. Strain sweeps indicated that linearity fails at between 1-8% strain amplitude, depending on sugar : water ratio; our frequency sweeps were all performed at strain amplitude 0.1%.

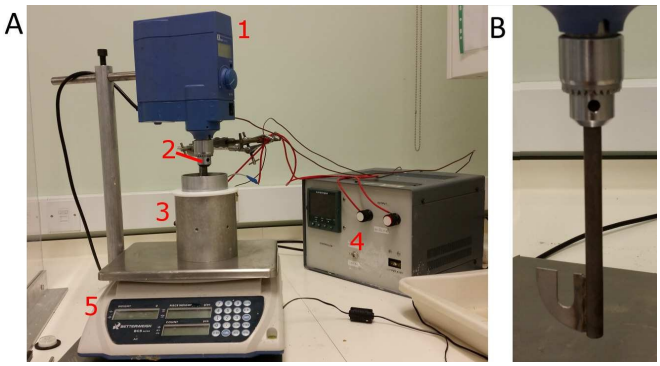


**Fig. 1** A. Our caramel apparatus. Contents are stirred by an IKA mixer (1) rotating a blade (2). An aluminium cylinder is heated by a jacket with embedded resistors (3). The temperature is controlled via a PID controller (4), The whole vessel is on a balance (5) to monitor water boil off. B. Detailed view of the mixing blade with gap for thermocouple.

## 4 Roaming composition space

Four classes of ingredients make up caramel: sugars, water, oil† and proteins. In our recipe, the composition is further tuneable by varying the syrup to sucrose and the WPI to casein ratios. Different compositions in this 6-dimensional 'space' suit different applications. [8] The interesting question arises: is there a well defined 'caramel region' in this space?

### 4.1 Delimiting the 'caramel region'

Exploring the full 6-dimensional (6D) space is impractical. We therefore keep the (syrup:sucrose) and (WPI:casein) ratios constant at the values in SMC to give a 4D composition space, where each composition is representable as a point inside a tetrahedron, Fig. 2. We further restrict ourselves al-

∗ All percentages are weight percents unless otherwise stated.

† We use 'oil' interchangeably with 'fat' unless distinguishing between solid and liquid phases is important. There is ≈ 0.1% NaCl in the continuous phase, which we do not explicitly discuss.

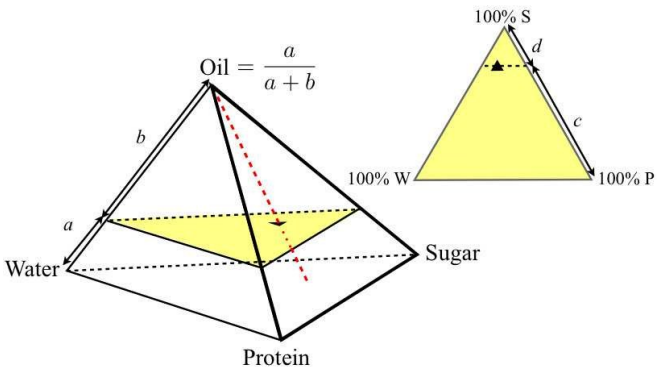


**Fig. 2** Quaternary composition space of caramel (regular tetrahedron, oil fraction = $a/(a+b)$) and ternary composition space of the continuous phase at a fixed oil fraction (equilateral triangle, sugar fraction = $c/(c+d)$), with ▲ = SMC. Samples along the red dashed line have different oil fractions but invariant continuous phase composition. The yellow triangle is the slice of composition space shown in Fig. 3.

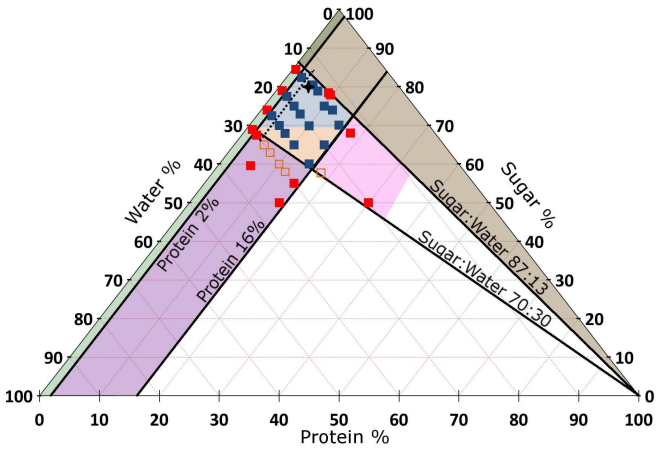


**Fig. 3** Composition space of the continuous phase of caramel at 15.7% oil (triangular slice in Fig. 2). A selection of samples for which we have measured the rheology are shown as points, amongst which red = denote failed caramels, orange = a non-standard cook and blue = a standard cook. The percentages refer to the continuous phase only and add up to 100% for any point. The star is standard model caramel (SMC). Areas: Blue = caramels with $G' < G''$, Orange = caramels with $G' > G''$, both at 1 Hz and 0.1% strain amplitude. Other colours represent various types of 'caramel failure'. Green = emulsification failure. Brown = transition to toffee texture. Pink = over-frothing. Purple = aggregate formation; deep inside this region, the caramel boils over during cooking and therefore cannot be made (the red points). The oscillatory rheology of all samples within the diamond-shaped blue-orange 'caramel region' obey time-composition superposition (tCS), Section 5.3, except those to the left of the black dashed line.

most exclusively to the single 'cut' in this tetrahedron at the oil fraction of SMC, giving a triangular composition space, Fig. 2. 'Roaming' this 'SMC-triangle' corresponds to changing the composition of the continuous phase in which a constant weight fraction of fat droplets is dispersed.

We measured a few samples along the dashed red line in the tetrahedron in Fig. 2, changing the oil fraction but keeping the continuous phase composition constant. We failed to make caramel at 0% fat: the premix frothed into a protein-stabilised foam, suggesting that oil plays an anti-foaming role. Thereafter, increasing the oil fraction leads to stronger caramels (Fig. S1, electronic supplement). We infer that the fat droplets are bonded to the matrix and act as 'active fillers'.[18]

We do not further investigate variable oil content, but keep it constant at that of SMC, viz., 15.7%. Instead, we vary the proportions of sugar, protein and water in the continuous phase. We find that that materials with the organoleptic properties of caramel could be made inside a well-defined diamond-shaped region in the SMC-triangle (orange and blue in Fig. 3).

## 4.2 The physics of caramel failure

The boundaries of the caramel region fall into two pairs, Fig. 3: two are constant-protein lines (at ≈ 2% and 16% ), and two extrapolate to the 100% protein corner, and are therefore constant (sugar:water) ratio lines (at 87:13 and 70:30). Crossing these boundaries leads to different 'failure modes'.

**4.2.1 Emulsification failure** Crossing into the green region across the the ≈ 2% constant-protein boundary, we found caramels that leaked oil. At ≈ 1% protein, a fat layer coalesced on the surface during cooking. Interestingly, the surface coverage of oil-in-water droplets by milk proteins decreases rapidly below a total protein concentration of ≈ 2%.[20] Thus, we suggest that beyond the blue-green boundary, there is insufficient protein to stabilise the drops of molten fat.

**4.2.2 The 'cremè Chantilly transition'** Crossing the ≈ 16% constant-protein boundary into the pink region, we find excess foaming when the sweetened condensed skim milk is combined with the remaining ingredients. The effect is similar, but not identical, to the foaming found at zero fat content already reported in Section 4.1. Preparing a premix at this level of protein is reminiscent of making a sweetened whipped cream, or *cremè Chantilly*, where one whips high-fat-content cream with up to ≈ 15% sucrose using cooled utensils, the latter to give fat crystals. The latter and the milk proteins together stabilise an air foam. We have few or no fat crystals, so that substantial amount of protein is needed to provide enough bubble stabilisation. If the SCSM turns into *cremè Chantilly*, caramel making becomes impossible.

**4.2.3 The 'toffee transition'** Crossing the ≈ 87:13 constant (sugar:water) line into the brown region, we obtained brittle, toffee-like samples. Operationally, it was difficult to dissolve enough sucrose to make the relevant sweetened condensed milk at 50 °C. We suggest that the proximity of the

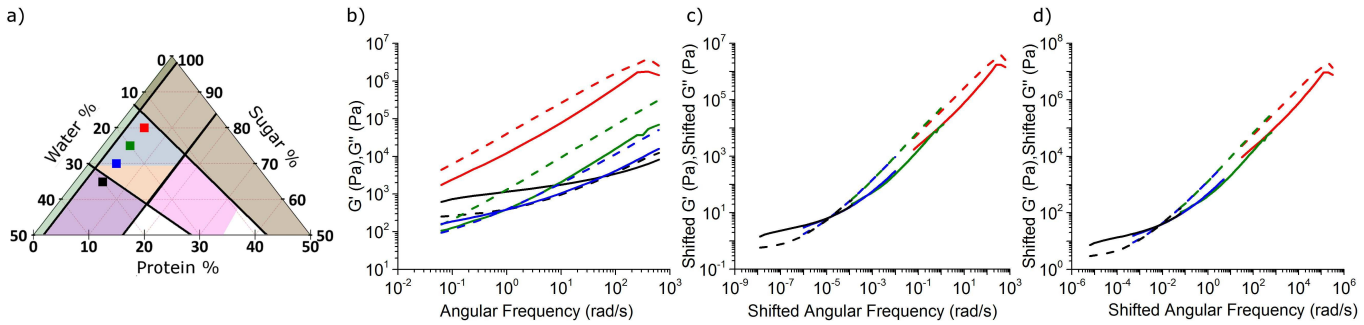


**Fig. 4** (a) Series of caramels with constant protein content and increasing water content in the 15.7% oil slice. (b) The rheology of standard model caramel, red curve, and associated caramels in (a). (c) Time-composition superposition analysis of the rheology of standard model caramel. We shifted all of the other curves in part (b) relative to the red curve. The result gives the rheology of standard model caramel over 9 decades in time and 5 decades in moduli.(d) Master curve created by shifting red, blue and black curves relative to the green curve. Solid lines: $G'$, Dashed lines: $G''$. Compositions are Red: 5%P, 15%W, 80%S; Green: 5%P, 20%W, 75%S; Blue: 5%P, 25%W, 70%S; Black: 5%P, 30%W, 65%S.

vitrification, which occurs at $\gtrsim 90\%$ sugar in aqueous sucrose solution,[21] accounts for the transition to toffee.

**4.2.4 Over-rapid protein aggregation** Crossing the $\approx$ 70:30 constant (sugar:water) line into the purple region, we found that aggregates form at the top of the heated premix, although caramel making is still possible just inside this region. Deeper into the region, coagulated aggregates completely covered the liquid surface and the mixture boiled over rapidly, halting caramel production. This suggests that our protein mixture is less stable against aggregation at lower sugar content, consistent with the majority literature.[14] Moreover, less sugar means lower boiling point[22] and viscosity,[21] increasing the risk of boil over. These effects together account for our observations at this boundary.

## 5 Caramel rheology: results

Caramel rheology is relevant for the applied scientist and the consumer. Previous studies[23–25] neither explored composition space systematically nor derived structural data from rheometry. We measure $G'(\omega)$ and $G''(\omega)$ throughout the caramel region and beyond, and interpret our results in terms of polymer physics.

### 5.1 Standard model caramel

In our accessible frequency range, $0.01\,\mathrm{Hz} < f < 100\,\mathrm{Hz}$ (or $0.63\,\mathrm{rad\,s^{-1}} \lesssim \omega \lesssim 630\,\mathrm{rad\,s^{-1}}$), SMC is a viscoelastic liquid, Fig. 4(a) (red curves), with loss tangent $\tan\delta = G''/G' = 3.4$. The data are consistent with

$$G''(\omega) \sim G'(\omega) \sim \omega^{\Delta}, \qquad (1)$$

with $\Delta \approx 0.8$. This signifies proximity to gelation in a system that form a branched network by bond percolation between monomers, for which $\frac{2}{3} < \Delta < 1$. This exponent relates to how the viscosity diverges and elasticity emerges below and above the percolation threshold.[26–28] Consistency requires[29]

$$G''/G' = \tan(\pi\Delta/2), \qquad (2)$$

or $G''/G' \approx 3.1$ for $\Delta \approx 0.8$; we measure a ratio of 3.4, Fig. 4(a) (red curves). These findings suggest that the matrix in caramel is a percolated protein gel.

We next characterised a series of samples, shown as points in Fig. 4(a), in which the protein fraction remains that of SMC, but with decreasing (sugar:water) ratio. As the water content rises, Fig. 4, both moduli drop, but $G'/G''$ rises, until the last caramel in this series becomes a viscoelastic solid ($G' > G''$) at $f = 1\,\mathrm{Hz}$. This transition (at $f = 1\,\mathrm{Hz}$) from liquid-like (blue, Fig. 3) to solid-like (orange, Fig. 3) occurs along other sequences of samples in the caramel region.

### 5.2 Rheological superposition: an overview

The evolution of viscoelastic spectra with composition, Fig. 4(a), is reminiscent of the effect of temperature, $T$, on polymeric viscoelastic spectra, where time-temperature superposition (tTS) often applies.[30] This means that $\log G'(\omega)$ and $\log G''(\omega)$ over the full $\log\omega$ range do not change shape when $T$ changes, but only shift along the $\log\omega$ axis. Thus, $T$ 'tunes' a single 'master clock' for all relaxation modes in the system (a $T$-dependent friction), and different modes can be brought into the experimentally-accessible time (or, equivalently, $\omega$) window by changing $T$. Alternatively, spectra obtained over a limited $\omega$ range at different $T$ can be shifted relative to each other along the $\log\omega$ axis and 'glued' together to give 'master curves' for $G'(\omega)$ and $G''(\omega)$ over many decades of $\omega$ (Supplement Fig S2 shows schematically how this is done in the simplest case.). Only a small number of 'canonical' shapes of master curves exist.[31]

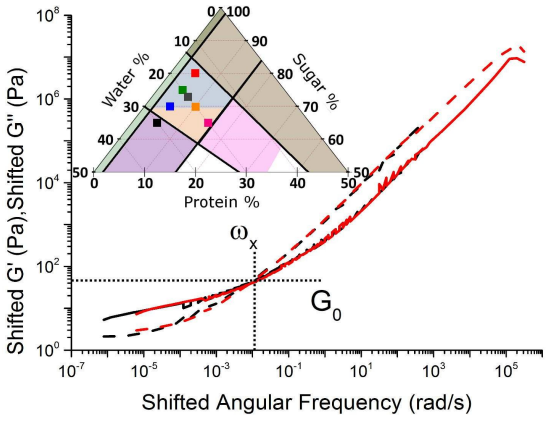


**Fig. 5** Overlay of two master curves obtained using tCS on the two sequence of samples shown as points in the inset, with spectra shifted related to the reference sample common to the two sets. Solid lines: $G'$, dashed lines: $G''$. Compositions are Red: superposition of 5%P caramels; Black: superposition of 20%W caramels .

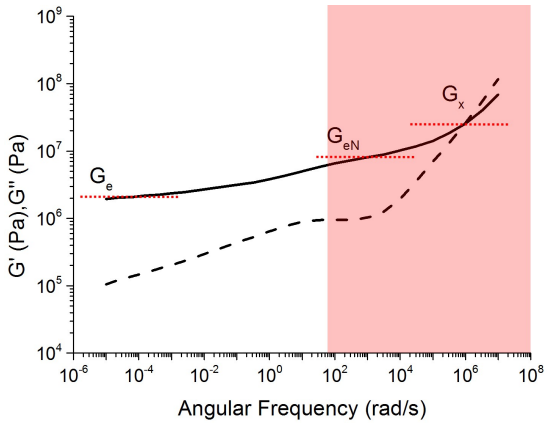


**Fig. 6** Ferry's 'type VII' master curves for a 'very lightly cross-linked amorphous polymer', here a vulcanised styrene-butadiene random copolymer. The shaded part corresponds to the caramel master curves in Fig.5. Solid lines: $G'$, dashed lines: $G''$.

In systems being 'cured' towards gelation by gradual cross-linking, time-cure superposition (tQS) applies.[27,28] Spectra for different curing times are shifted both horizontally (along $\log\omega$) and vertically (along $\log G$) to obtain master curves. If tQS works, then curing time 'tunes' two interrelated variables, a time scale, via the viscosity, and an elasticity scale, via proximity to percolation.[27] (Recall that viscosity and modulus both diverge at percolation.[26])

### 5.3 Time-composition superposition for caramel

Caramels obey tCS. Consider the sequence of constant-protein-content samples in Fig. 4(a) (red = SMC) and their $G'(\omega)$ and $G''(\omega)$ spectra, Fig. 4(b). We shift the data for the three green, blue, black samples along the frequency and moduli axes relative to the SMC data (red) to obtain the 'master curves' of SMC over 9 decades of $\omega$, Fig. 4(c). Doing the same to the data for the second sample in the sequence (green, Fig. 4(a, b)) gives its master curves, Fig. 4(d), which are identical to those for SMC, Fig. 4(c), but with rescaled axes.

We now show that the same master curves are obtained for a reference sample irrespective of the compositions of the other samples used to perform tCS. Figure 5 (inset) shows the same sequence of constant-protein-content samples as Fig. 4(a) (with the same colour scheme), but also a sequence of constant-water-content samples that overlap with the first sequence in a common, reference sample (green). The master curves for this reference sample already obtained by shifting spectra along the constant-protein-content sequence, Fig. 4(d), are replotted in Fig. 5 as the red curves. The master curves for the same reference sample obtained by shifting spectra along the constant-water-content sequence (Fig. S3, electronic supplement) are plotted as the black curves in Fig. 5. The red and black plots are therefore the results of two different tCS routes to the master curves of the reference sample (green in the inset) over 11 decades of $\omega$, and they overlap. Note that the limited number of samples we made with varying fat content, Sec. 4.1, can also be analysed by tCS to produce a master curve that agrees with that in Fig. 5 (data not shown).

Comparison of Fig. 5 with the master curve categories given by Ferry[31] shows that caramel behaves as a 'very lightly crossed linked amorphous polymer'. We show Ferry's exemplar, a vulcanised rubber, in Fig. 6. Thus, caramels are 'filled rubbers' (with fat droplets as fillers).

We find that all other sample sequences in the caramel region in Fig. 2 give master curves of identical form (e.g., Fig. S4 in electronic supplement), except for the samples to the left of the (dashed) $3\pm1\%$ protein line in Fig. 2 (for which see Section 6.3). With this exception, then, *all caramels are instances of a single 'universal material'* with rheology given by Fig. 5. To find the rheology of any particular caramel, we simply rescale the two axes using numerical factors given by Eqs 4 and 7 given below.

We note that tCS also holds for colloidal gels formed by carbon black particles,[32] where master $G'(\omega)$ and $G''(\omega)$ curves are obtained by shifting data for samples with different particle and dispersant concentrations. A key difference with caramel, due to the different nature of gelation, will be pointed out below.

### 5.4 Time-cure superposition for caramel

We also carried out a limited number of experiments in which we fixed the composition but varied the curing time. Instead of

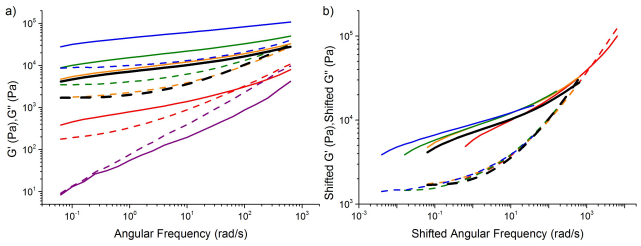


**Fig. 7** (a) The viscoelastic spectra of caramel with a fixed composition cooked in a sealed tube at 90 °C in an oil bath for varying lengths of time. (b) Time-cure superposition (tQS) using the data in (a) and the orange curve (2 hours cooking) as reference. In both parts, the rheology of a mixture cooked in the conventional way to the same final composition as the sealed mixture is shown in black. Solid lines: $G'$, Dashed lines: $G''$. Composition 7%P, 30%W, 63%S. Time cooked: purple 0 h, red 1 h, orange 2 h, green 3 h, blue 7 h. Also see Fig. S5

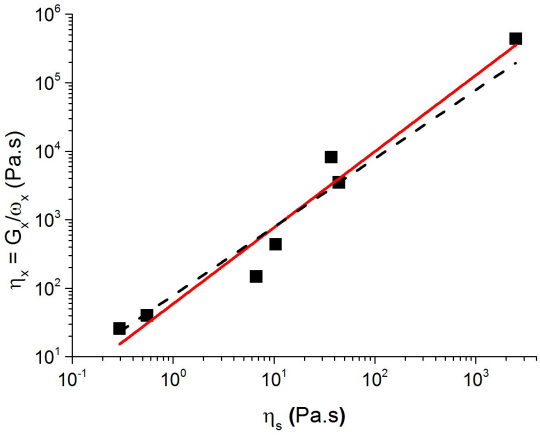


**Fig. 8** The cross-over viscosity, $\eta_\times = G_\times \omega_\times^{-1}$ of a number of caramels plotted against the measured viscosity of the background sugar solution in each sample. Red line: best fit to $\eta_\times = \eta_0 \eta_s^\beta$ with $\eta_0 = 59$ (Pa.s)$^{-0.1}$ and $\beta = 1.1 \pm 0.1$. The black dashed line has unit slope.

boiling off water at 120 °C from an initial mixture that is more dilute than the target final composition, we prepared mixtures at the target final compositions sealed in 5 ml glass vials and cooked in an oil bath at 90 °C for variable periods of time. The data, Fig. 7(a), can be put into master-curve form using time-cure superposition, Fig. 7(b). The implication is that it is neither composition (previous section) nor cooking time (this section) *per se* that is important, but the extent of cross-linking, which can be tuned by composition, or curing time, or a combination of both. However, since we have most data on tCS, the rest of our discussion will be based on composition.

## 6 Caramel rheology: emergence of simplicity

### 6.1 The physical significance of tCS

In tCS, high or low frequency modes are brought into the experimental window by 'tuning' the composition. This can happen in two ways. First, 'tuning' the composition and therefore the viscosity of the solvent of a polymeric system accesses different time scales.[33] For us, since the background sugar solution (70-87% sugar) is close to its glass transition,[21] we expect that viscosity is mainly 'tuned' by the (sugar:water) ratio.

The second effect relates to tQS, where extent of reaction determines connectivity, which controls elasticity. Thus, tQS in general involves not only rescaling time, but also moduli. We cook our caramels for approximately the same time, so that curing time is also approximately constant.‡ Instead, we tune connectivity by composition, e.g., higher sugar content stabilises our proteins, so that the same curing time achieves a lower degree of reaction and therefore connectivity.

Thus, as we roam composition space, we are in fact tuning only two 'master parameters', viscosity and connectivity. We now explore how viscosity and connectivity act together to produce the observed tCS in caramels. To do so, we propose to use the crossover point in the master curves, $(\omega_\times, G_\times)$, Fig. 5 to characterise the shifting time and moduli scales in tCS.

### 6.2 Viscosity and time

The characteristic viscosity of a caramel can be estimated by

$$\eta_\times = G_\times \omega_\times^{-1}. \quad (3)$$

We now show that $\eta_\times$ is directly controlled by the viscosity of the aqueous sugar solution in the continuous phase, which is a solution of sucrose and the various sugars in the glucose syrup. In our work, the ratio of sucrose to glucose syrup solids is constant. We measure the viscosity, $\eta_s$, of a number of aqueous sugar solutions with concentrations matching those found in various samples for which we have determined $\eta_\times$. The resulting $\eta_\times$ vs. $\eta_s$ plot, Fig. 8, can be fitted by

$$\eta_\times = \eta_{s0} \eta_s^\beta, \quad (4)$$

with $\eta_{s0} = 59$ (Pa s)$^{-0.1}$ and $\beta = 1.1 \pm 0.1$. Indeed, given the data scatter, we may take this result as consistent with $\eta_\times \propto \eta_s$. Thus, the viscosity of caramels, $\eta_\times$, is a simple function of the viscosity of the background aqueous sugar solution, $\eta_s$.§

### 6.3 Connectivity and elasticity

Three moduli characterise a cross-linked amorphous polymer: $G_e$, $G_{eN}$ and $G_\times$, Fig. 6. The equilibrium or rubber

‡ But not exactly, because, e.g., the boiling point of samples differ

§ Note that the constant $\eta_{s0}$ in Eq. 4 is not universal, but depends on, *inter alia*, the composition of the glucose syrup and sugar-protein interactions.

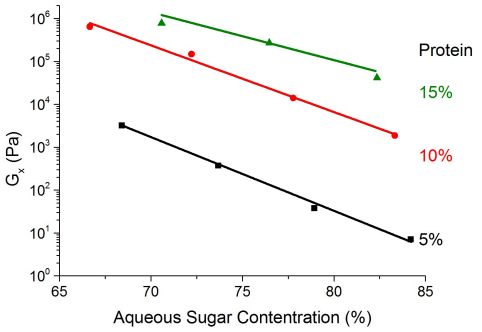


**Fig. 9** The dependence of the cross-over modulus, $G_\times$ on the (sugar:water) ratio at the standard oil fraction for three different protein concentrations. Lines are exponential fits.

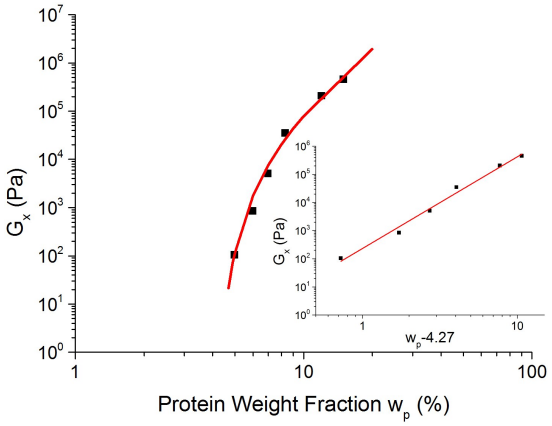


**Fig. 10** The dependence of the cross-over modulus, $G_\times$ on protein concentration, $w$, at the standard oil fraction and a constant sugar:water ratio of 2.9. The error bars for these data points are the size of the points or lower. The red curve is a fit to $G_\times \sim \mathfrak{G}(w-w_c)^f$, Eq. 6, with $\mathfrak{G} = 318$ Pa, $w_c = 4.27\%$ and $f = 3.17$. The inset shows the same data and fitting in a plot against $\log(w_p - 4.27\%)$.

plateau modulus, $G_e$, is controlled by the density of (permanent) chemical cross-links, which is directly related to the 'effective molecular weight', $M_{\rm eff}$, of the polymeric strands between cross-linking points:[30]

$$G_e = \frac{\rho}{M_{\rm eff}} RT, \tag{5}$$

where $\rho$ is the mass density of the material and $R$ is the gas constant. The equilibrium entanglement modulus, $G_{eN}$, is controlled by the density of entanglement points (which can slip at long times); a corresponding effective molecular weight between entanglement points can be defined. The cross-over value, $G_\times$, is an upper bound for either of these quantities.

We find that $G_\times$ weakens with increasing (sugar:water) ratio $w_{\rm s}$ at fixed protein concentration, Fig. 9. The small range of $w_{\rm s}$ encompassing the caramel region does not permit definitive identification of the functional form of this dependence, but our data is consistent with an exponential decrease with a pre-factor dependent on the protein concentration, $w_{\rm p}$.

Turning to the dependence on protein concentration, we find that $G_\times$ scales with $w_{\rm p}$ in a 'critical' fashion:

$$G_\times \propto (w_{\rm p} - w_{\rm p0})^f, \tag{6}$$

with $w_{\rm p0} = 4.27\%$ and $f = 3.17$. We will discuss the physical implications of this in Section 7. Thus, our results suggest

$$G_\times = \mathscr{G}_0 (w_{\rm p} - w_{\rm p0})^f g(w_{\rm s}), \tag{7}$$

where the dependence on sugar concentration, $g(w_{\rm s})$, may be exponential, and the constant $\mathscr{G}_0$ sets the elasticity scale.

### 6.4 Simplicity in complexity

The success of tCS means that the viscoelastic spectra of every sample to the right of the dashed line in the caramel region in Fig. 2 have the form shown in Fig. 5, with the frequency and moduli scales set by Eqs. 3, 4 and 7. It is not *a priori* obvious that such a universal description in a significant region of composition space should be possible. That it can be done demonstrates practically the power of tCS, and conceptually that a 'universal caramel' exists as far as rheology is concerned. Uncovering such simplicity in apparent complexity is a good example of the utility of a 'soft matter' approach to foods.

## 7 Caramel rheology: molecular implications

Although molecular details are not our focus, our rheology data provide constraints on molecular mechanisms; in particular, on how the protein gel matrix is formed.

Globular proteins gel in a variety of ways between two idealised limits. They can aggregate as more or less intact colloids, or unfold and cross-link as polymers. The elastic moduli of these two types of gels scale quite differently with protein concentration. For a *particulate gel* formed by the aggregation of, e.g., intact casein micelles or carbon black,

$$G \sim w_{\rm p}^{\delta}, \tag{8}$$

where the exponent $\delta$ is details-dependent,[34] with observed values[32,35,36] up to $\delta \sim 4$ or 5. On the other hand, if the picture of percolating cross-linked polymeric strands is more appropriate, one finds a critical behaviour of the form shown in Eq. 7, with exponent $f \gtrsim 2$.[37,38]

Assuming that $G_\times$ is a reasonable surrogate for $G_e$, Fig. 6, our data, Fig. 10, exclude Eq. 8, but are consistent with Eq. 6.

This evidence for percolation gelation is consistent with the observation of $G'(\omega), G''(\omega) \sim \omega^{0.8}$ for $\omega \gg \omega_\times$, Eq. 1.[26–28]

The fitted percolation threshold of $w_{p0} \approx 4\%$ makes sense of the observation that in Fig. 3, the three samples to the left of the black dashed line did *not* satisfy tCS. In each case, we find that they are liquid like, $G'(\omega) < G''(\omega)$, with the two curves more or less parallel over the whole of our accessible frequency range, but with quite different slopes in each cases, and the data do not satisfy Eq. 2. There is therefore no prospect that these would scale by tCS. The next line of samples at 5% protein all obey tCS, giving master curves consistent with Fig. 5. These observations are consistent with the finding from fitting Eq. 6 to our data that $w_{p0} \gtrsim 4\%$. It is therefore possible to *define* 'caramel', for the purposes of this study, as all cooked sugar-water-protein systems showing the universal rheology in Fig. 5.

A quantitative understanding of the effect of sugar, Fig. 9, will require detailed kinetic knowledge of the various reactions involved. Qualitatively, however, these findings suggest that sugar stabilises proteins under our conditions[14], so that higher sugar content should give rise to fewer cross-links for the same cure time, and therefore weaker elasticity.

We can interpret the range of observed $G_\times$ values, Fig. 9, using Eq. 5. The molecular weight of BLG and $\kappa$-casein are both $\lesssim 20 \times 10^3$ g/mol. This value gives an order of magnitude (OOM) lower bound for $M_{\text{eff}}$, and therefore, an OOM upper bound of $G_e \lesssim 10^5$ Pa, Eq. 5. Our highest observed $G_\times$ is $\sim 10^6$ Pa, and we know that, necessarily, $G_\times > G_e$ (Fig. 6), so that our OOM upper bound seems reasonable. Assuming that $G_\times / G_e \sim \mathbf{O}(10)$[¶], Fig. 9 suggests that $G_e \gtrsim 1$ Pa, so that Eq. 5 predicts an OOM maximum $M_{\text{eff}} \sim 240 \times 10^7\,\text{g mol}^{-1}$, or $\sim 10^5$ proteins of the size of $\beta$-lactoglobulin and/or $\kappa$-casein. Again, this does not seem unreasonable.

## 8 Neglected complexities

Throughout, we have neglected a number of potential complications. We now briefly discuss these, and indicate how they may fill out, but not invalidate, the picture we have given.

### 8.1 Imperfect superposition

Examining the results presented in Fig. 7 again, we see that there appears to be small but systematic deviations from perfect tQS at low frequencies in $G'(\omega)$. This is probably because, with longer curing, a sample will move from Ferry's Type VII master curve (weakly cross linked rubber) to Type VI (strongly cross linked rubber), which involves, *inter alia*, loss of the intermediate ($G_{eN}$) inflection in the $G'(\omega)$ spectrum (cf. Fig. 7). This is consistent with the way deviation from tQS shows up in our data (cf. Fig. 2.3 in Ferry[31]). Our tQS experiments using the oil-bath cooking method. The majority of our data for tCS were obtained from samples cooked using our standard protocol do not show systematic deviations from superposition. This is probably because our tQS experiments explored a significantly larger range of cross-link densities than in our standard-protocol, tCS, experiments. Interestingly, previous data in tQS[27] do not extend to low enough frequency to detect this effect. Future work to understand it should give additional insights into the details of structural evolution as a function of composition or curing time.

### 8.2 Proteins: caseins vs. whey

We have attempted to prepare SMC with either just WPI or casein micelles, but at the same total protein weight fraction as in the mixed-protein material. Using casein only gave essentially the same material as SMC, though with $G'(\omega)$ and $G''(\omega)$ smaller by $\approx 40\%$ over our $\omega$ range. Limited experiments at other compositions gave similar results. There is therefore no essential change upon switching to a casein-only system. On the other hand, using WPI only in the same recipe gave a translucent material that fractured easily. This is clearly *not* a caramel. Thus, casein protein plays the dominant role in the formation of the gel matrix.

### 8.3 Maillard reactions: more than browning

The essential difference between sucrose and all the sugars found in glucose syrup is that the former is non-reducing, while all of the others are reducing. Only the latter can participate in Maillard reactions.[16] Replacing all of the sucrose with glucose produced samples differing little from our standard caramels except $\approx 20\%$ weaker moduli over the accessible $\omega$ range. However, replacing all the sugar content of glucose syrup with sucrose[‖] led to retarded caramel formation. A very lightly coloured solid gel resulted only after $\sim 29$ h of incubation at 90 °C in our oil bath. Presumably, it took this length of time for a small amount of sucrose to invert into its reducing monosaccharide components (i.e. glucose and fructose), which could then participate in Maillard reactions. The latter therefore play an essential role in caramel formation.

To explore what this role is, we repeated the sucrose-only experiment with enough acetic acid added to bring the pH of the starting pre-mix to $\approx 5$. Now, an uncoloured caramel with elastic moduli in the usual range was formed after 2 h of incubation at 90 °C. The absence of browning indicates that Maillard reactions have not occurred to any significant extent during this time period. Since carboxylic acids are produced in Maillard reactions,[16] these results taken together suggest

¶ Whilst this holds for non-attractive polymer systems, it has not been extensively studied in attractive gel systems, and caution is warranted

‖ Note that the sucrose does not crystallize at this composition under our conditions

that in our standard recipe, a key role played by the Maillard reactions is to lower the pH enough for the kind of protein aggregation needed for caramel formation.

### 8.4 Gelation: the details

That the protein matrix should have the character of a polymeric, rather than a colloidal, gel is surprising, because casein micelles are essential to gelation (Section 8.2). The molecular nature of the polymer-like protein network in caramel remains to be elucidated. Moreover, we have assume throughout, albeit tacitly, that the gel is homogeneous. This is unlikely to be true in practice. Again, the role of inhomogeneities remains to be investigated.

### 8.5 The role of the fat

Figure S1 in the electronic supplement shows that increasing oil content strengthens caramel rheology, so that the droplets are bonded with the protein matrix.[18] If our interpretation of Fig. 9 is correct, i.e., that sugar stabilises proteins against thermal denaturation, so that higher sugar content produces weaker protein matrices, then higher sugar content may also weaken the bonds between the proteins stabilising the fat droplets and the gel matrix, leading to weaker caramels.

Separately, it is known that oils may partition into the core of casein micelles, which have hydrophobic cores that can encapsulate hydrophobic compounds such as vitamin D[39]. The effect of such potential oil incorporation is unknown, but seems unlikely to overturn any of our central conclusions.

## 9 Summary and conclusions

The high-dimensional composition space of sugars, proteins, water and oil is the basic 'confectionary space' encompassing many classes of products. Within one slice of this space, we find that caramels inhabit a well-defined region. Within this region, cooking a 'premix' of these ingredients leads to gelation of the sugar-protein matrix, with protein-staiblised oil droplets chemically-bound to the matrix. Future work should explore composition space more widely, using the oil bath method to extend the accessible range (Section 5.4).

Investigating the location of the boundaries of the caramel region gives insights into the structure of caramel. The viscoelastic spectra of caramels satisfy time-composition superposition, so that roaming composition space 'tunes' only two basic parameters: the viscosity of the aqueous sugar solution and the connectivity of the protein gel network. The universal rheological spectra of all caramels are shown in Fig. 5, with the scales set by Eqs. 4 and 7.

That such simplicity and universality are there to be found is not *a priori* obvious from the complexity of the ingredients and the recipe. Our results show how coarse-grained soft-matter physics can be applied to whole food systems.

Relevant data for this work have been deposited at the following site: `http://dx.doi.org/10.7488/ds/318`.

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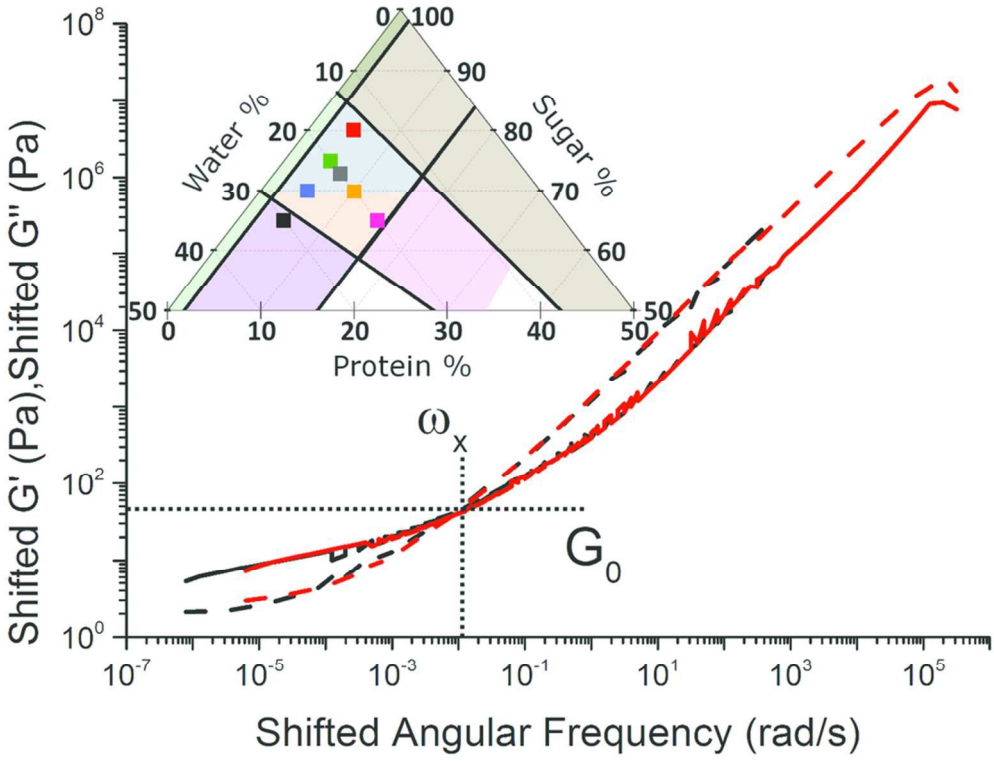
GA text:

Master rheological spectra of our caramels over 12 orders of magnitude of frequency.

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