





Critical stresses in mechanochemical reactions†

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The rates of mechanochemical reactions are generally found to increase exponentially with applied stress. However, a buckling theory analysis of the effect of a normal stress on an adsorbate that is oriented perpendicularly to the surface that reacts by tilting suggests that a critical value of the stress should be required to initiate a mechanochemical reaction. This concept is verified by using density functional theory calculations to simulate the effect of compressing a homologous series of alkyl thiolate species on copper by a hydrogen-terminated copper counter-face. This predicts that a critical stress is indeed needed to initiate methyl thiolate decomposition, which has a perpendicular C–CH₃ bond. In contrast, no critical stress is found for ethyl thiolate with an almost horizontal C–CH₃ bond, while a critical stress is required to isomerize propyl thiolate from a *trans* to a *cis* configuration. These predictions are tested by measuring the mechanochemical reaction rates of these alkyl thiols on a Cu(100) substrate by sliding an atomic force microscope tip over the surface and finding a critical stress of ~0.43 GPa for methyl thiolate, ~0.33 GPa for propyl thiolate, but no evidence of a critical stress for ethyl thiolate, in accord with the predictions. These results provide insights not only into mechanochemical reaction mechanisms on surfaces, but also on the origin of critical phenomena in stress-induced processes in general. It also suggests novel approaches to designing robust surface films that can resist wear and damage.

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Introduction

Mechanochemical reactions have been known for many millennia; such a reaction was described by Theophrastus in his treatise “On Stones” (Περὶ λίθων).¹ Historically, the first theories of mechanically induced processes were developed to describe the energy dissipated during solid–solid sliding (friction),^{2–5} and liquid shear (viscosity).^{6,7} The physical principles that underpin these theories of mechanical energy dissipation also apply to mechanochemistry.⁵ Evans and Polanyi presented an early analysis of mechanochemical reaction rates⁸ by using transition-state theory to show that the pressure-dependent rate constant of a chemical reaction, $k(P)$ could be written as $k(P) = k_0 \exp\left(-\frac{P\Delta V^\ddagger}{RT}\right)$, where k_0 is the rate at zero pressure, P is the pressure and ΔV^\ddagger is an activation volume and is broadly interpreted as the difference in volume between the reactant and transition states. If the reaction activation energy in the absence of an imposed stress is E_{act}^0 , and assuming that the pre-exponential factor is constant, the above equation is equivalent to writing $E_{\text{act}}(F) = E_{\text{act}}^0 + P\Delta V^\ddagger$. This is commonly

known as the Bell equation,⁹ and predicts that the stress-induced activation energy, and therefore the reaction rate, tends continuously to the zero-pressure value as the pressure decreases to zero. The following paper demonstrates that this is not always the case and that situations exist in which there is a critical stress below which a mechanochemical reaction does not occur.

Fundamental mechanochemical experiments have been carried out by attaching a reactant (known as a mechanophore) to an atomic force microscopy (AFM) tip and measuring the force needed to extend and finally cleave one or more bonds at some well-defined force reminiscent of the critical forces found here for sliding on an adsorbed monolayer, but with a different physical origin.^{10–17} Because of the ability to accurately measure the force acting directly on the mechanophore, this can lead to extremely precise measurements of force-induced bond scission rates, but which are often difficult to interpret because of the uncertainty in the way in which the force is exerted by the tip. More recently, mechanochemical reactions have been induced by sliding over adsorbate-covered surfaces^{16,18–26} where it is found that the decomposition of surface-anchored hydrocarbon species occurs by the adsorbate initially tilting towards the surface to weaken the bond and ultimately induce its cleavage to result in a mechanochemical reaction. The energetics of reaction pathways can be calculated using quantum mechanical methods²⁷ so that, for example, it is found that methyl thiolate (CH₃–S_(ads)) overlayers adsorbed on copper react by the C–S bond tilting towards the surface to react to form adsorbed sulfur

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Theoretical methods

Density functional theory (DFT) calculations were performed with the projector augmented wave method^{36,37} as implemented in the Vienna *ab initio* simulation package, VASP.^{38–40} The exchange–correlation potential was described using the generalized gradient approximation of Perdew, Burke and Ernzerhof.⁴¹ A cutoff of 400 eV was used for the plane-wave basis set, and the wavefunctions and electron density were converged to within 1×10^{-6} eV. The first Brillouin zone was sampled with a $4 \times 4 \times 1$ Monkhorst–Pack grid.⁴² Geometric relaxations were considered to be converged when the force was less than 0.01 eV Å⁻¹ on all unrestricted atoms. van der Waals' interactions were implemented using the DFT-D3 method as described by Grimme *et al.*⁴³

The lattice constant used for Cu(100) was 3.575 Å. The system consisted of two (2×2) Cu(100) slabs to mimic the experimental saturated coverages of alkyl thioliates on Cu(100).⁴⁴ The alkyl thiolate molecule was adsorbed onto a 6-layer slab in a hollow site. The bottom three layers of that slab were frozen while the top three layers were allowed to relax. The second slab was 3-layers thick and passivated with hydrogen to render the interacting surface inert. All atoms in this slab were kept frozen to simulate an infinitely hard surface. Compression of the methyl thiolate molecule was simulated by bringing the small, infinitely hard slab down in 0.1 Å steps, and decompression was simulated by raising the slab up in 0.1 Å steps.

Results and discussion

To investigate critical phenomena in the methyl thiolate mechanochemical decomposition, the most stable structure was compressed by a slab consisting of stiff, passivated Cu(100) counterface. The separation between the slabs was decreased from an initial value of 0.85 nm and decreased in 0.01 nm steps. The structure was relaxed at each interval and a movie of the process is shown in Fig. S3.† This shows that the methyl thiolate first compresses elastically while maintaining its vertical geometry, but then suddenly tilts to an angle of $\sim 68^\circ$ to drastically decrease the energy of the system. The slab is then retracted to allow the methyl thiolate molecule to move back to its original vertical configuration. The resulting plot of energy *versus* slab separation is shown in Fig. 1(●), which also schematically illustrates the critical buckling process described above. A long-range interaction is seen as the slabs approach, and is due to the different charges that are present on the methyl-thiolate and hydrogen-covered surfaces due to their different work-functions.⁴⁵ This is consistent with the snap into contact seen in force–distance curves measured by an AFM.²⁹ This results in an energy minimum at a slab separation of ~ 0.66 nm and then a rapid parabolic increase as the slabs come closer together. As the slabs reach a critical separation of ~ 0.5 nm, the methyl thiolate undergoes a sudden tilt to reduce the energy from ~ 150 kJ mol⁻¹ to ~ 52 kJ mol⁻¹. The compressed state was then relaxed by incrementally moving the slabs apart and the resulting energies are also plotted in Fig. 1(■). Now the tilt angle decreases as the slab separation

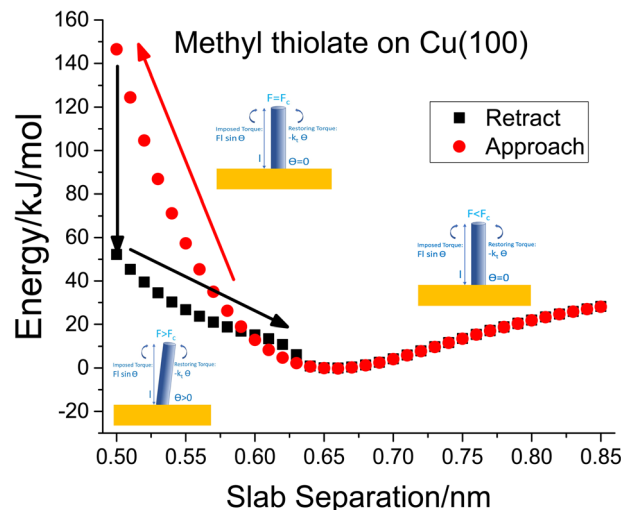


Fig. 1 Plot of the energy *versus* slab separation for the compression of a vertical methyl thiolate species on Cu(100) as a function of the distance from a hydrogen-atom-covered Cu(100) surface for the approach of the two slabs (●) until the initially vertical methyl thiolate species tilts. The structural changes associated with the approach and retraction of the slabs is shown in movie S3.† Shown also are cartoons that illustrate the onset of critical buckling.

increases to ~ 0.66 nm when the C–S bond of the methyl thiolate becomes vertical once again. At larger slab separations, the energy follows the variation as found during the approach.

To investigate whether critical stresses can be found, experiments were carried out by sliding an AFM tip over a saturated methyl thiolate overlayer at various normal loads and by imaging the sample at a low, non-perturbative load to observe the grooves formed on the surface due to the shear-induced removal of the methyl thiolate species from the surface. As shown in Fig. 2, linear features are formed on the surfaces in flat regions that are away from surface steps that become deeper as sliding proceeds. The depth of the groove is taken to be proportional to the extent of the reaction. Note that sliding was along the direction that gave the maximum rate⁴⁶ and rastering experiments showed that the methyl thiolate decomposes *via* C–S bond scission to adsorb sulfur on the surface in a similar reaction as found for a ball-on-flat rubbing.^{24–26,28} In addition, the width of the wear track for each experiment is taken to correspond to the outer diameter of the contact and enables the normal contact stresses to be measured with reasonable accuracy.²⁹ Both the width of the wear tracks and the values of indentation diameters measured during compression obtained in previous experiments²⁹ are plotted *versus* normal load in the Fig. S2.† Note that the shape of the indentation profile could be modeled by assuming a Hertzian stress distribution with a Bell-like dependence of mechanochemical reaction rate with contact pressure.^{9,29} The variation of contact area with normal load is modeled using both the Derjaguin–Muller–Toporov (DMT)⁴⁷ and Johnson–Kendall–Roberts (JKR)⁴⁸ contact theories using the measured tip radius, where the JKR model gives reasonable agreement with the experimental values which were used to calculate the contact stresses (Fig. S2†). The influence of the



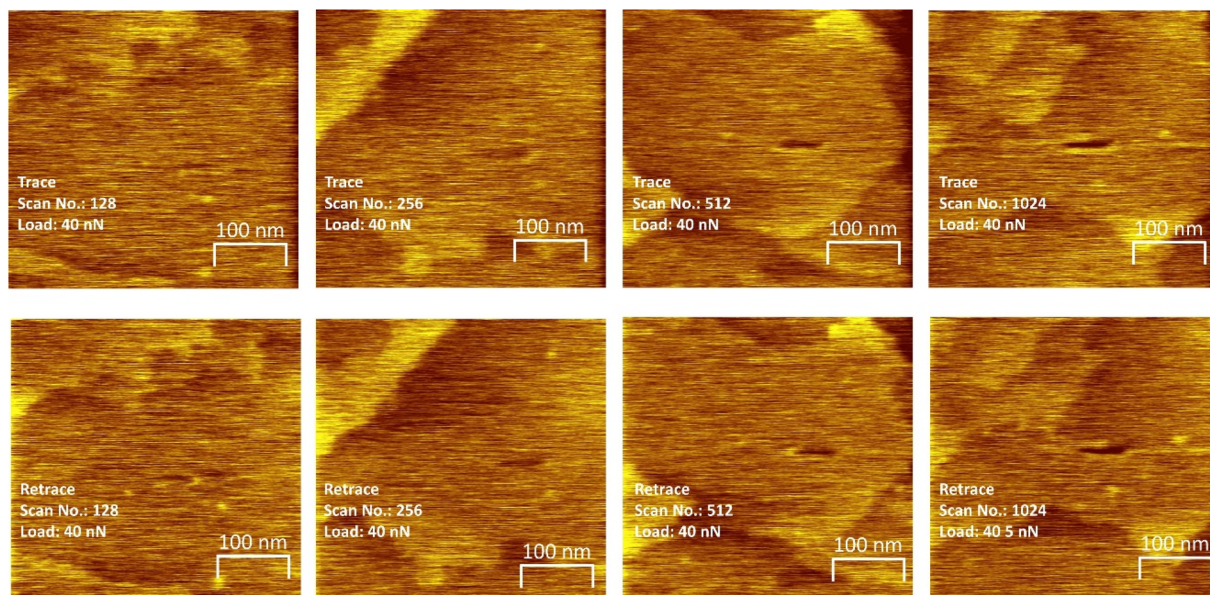


Fig. 2 Low-load AFM images of methyl-thiolate-covered Cu(100) after having been scanned various times in the forward (top traces) and the reverse (bottom traces) direction at a load of 40 nN, where the scan times are shown marked on each image.

presence of a thin film of methyl thiolate on the copper substrate was also gauged⁴⁹ and the thin films present on the copper surface made a negligible difference to the calculated results.

The resulting groove depths are plotted as a function of the number of passes over the surface for several values of the normal load of the AFM tip in Fig. 3 for loads for which a groove could be detected. The groove depth increases exponentially with the number of passes to an asymptotic value that is in

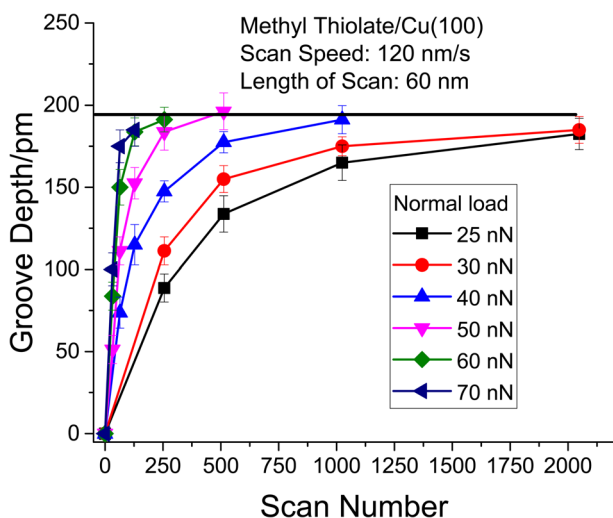


Fig. 3 Plot of the depth of the wear track as a function of the number of passes over a methyl thiolate saturated Cu(100) surface showing an exponential increase in the depth of the wear track, indicative of first-order reaction kinetics. The maximum depth for all mechanochemical reactions is ~ 195 pm, which agrees well with the calculated thickness of a methyl thiolate films.

accord with the height of a methyl thiolate species above the surface indicating a first-order reaction rate where the total reaction time equals the number of passes multiplied by the time that a point on the surface is in contact with the tip, t_c . The results are analyzed to yield a rate constant, k_p per the number of passes. The lowest loads showed no detectable wear, and the maximum reaction rates for these loads (normal stresses) were calculated by assuming that the wear depth was equal to or less than the noise in the AFM image. Note that these experiments were interspersed with those at higher loads where a wear track was observed to ensure that there were no changes to the tip that might have prevented reaction. In addition, pull-off forces were measured periodically between experiments, and showed no significant variation.

The results are plotted in Fig. 4 as $\ln(k_p)$ versus the average contact stress,^{16,19} and reveal a clear threshold normal stress of ~ 0.43 GPa below which no mechanochemical reaction could be detected. The points below this threshold represent the maximum possible reaction rate assuming that the groove depth is of the order of the noise in the image of the surface, and the arrows emphasize this. The variation in rate with stress above this threshold can be described using the Bell model⁹ in which the mechanochemical rate constant under the influence of some stress, $k(\sigma)$, is given by $k(\sigma) = k_0 \exp\left(\frac{\sigma \Delta V^\ddagger}{k_B T}\right)$, where k_B is the Boltzmann constant, and k_0 is the rate constant in the absence of an applied stress so that $\ln k_t(\sigma) = \ln k_t^0 + \frac{\sigma \Delta V^\ddagger}{k_B T}$.

This analysis is for reaction kinetics measured as a function of time, k_t , while the experiment yielded rates as a function of the number of passes, but they are related by $k_t \cong k_p/t_c$. t_c depends on the sliding speed and contact width. Since the sliding speed was constant for all experiments, and the contact width varies



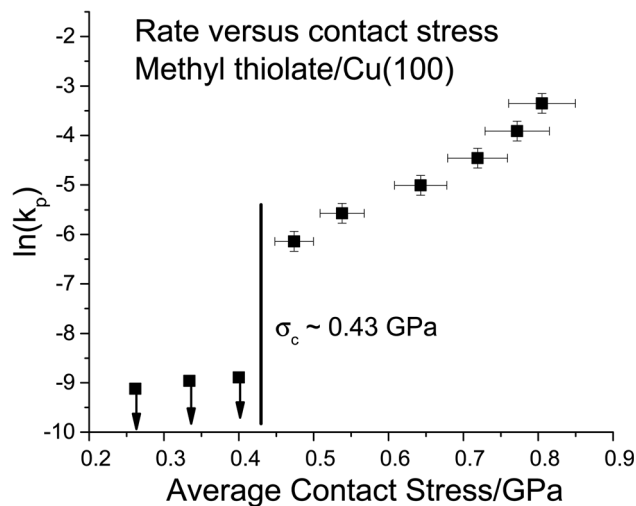


Fig. 4 Plot of $\ln(k_p)$ versus the normal stress in GPa (■) for the rate of mechanochemical decomposition of methyl thiolate species on Cu(100), where k_p is the rate constant calculated per pass over the surface. Note that the rates for low values of normal stress were estimated by assuming that the depth of any wear track was less than the noise in the image of the scanned surface. Here the arrows indicate that the points represent the maximum rates. The vertical line shows the value of the critical stress, $\sigma_c \sim 0.43$ GPa.

only slowly with the force exerted on the tip, the activation volume measured from plots of either $\ln(k_t)$ or $\ln(k_p)$ versus stress will be approximately the same. It should, however, be noted that this analysis does not take into account the stress distribution across the contact. Nevertheless, the relative values of activation volumes for different adsorbates collected under identical conditions should be correct. A linear fit to the data above the critical stress of ~ 0.43 GPa yields an activation volume of $32 \pm 3 \text{ \AA}^3$ per molecule (Table 1).

To further investigate critical phenomena, calculations and experiments were carried out for ethyl and propyl thiolate species on Cu(100). The terminus of adsorbed ethyl thiolate species is expected to be relatively close to parallel to the surface as illustrated by the most stable structure determined by DFT (Fig. 5A and S3†). The compression of an ethyl thiolate slab is illustrated in Fig. S3,† which shows that the molecule tilts under compression and returns to its original structure when the slab is retracted. This is emphasized by the data in Fig. 5A, which plots the S–C1 angle (indicated as an inset to Fig. 5A) as a function of slab separation. This remains reasonably constant as the slab approaches at an angle of $\sim 10^\circ$ as the slab separation decreases to $\sim 7.4 \text{ \AA}$ so that the van der Waals' interaction of the terminal ethyl group with the surface causes the adsorbate

to tilt slightly compared to methyl thiolate on Cu(100). As the slab separation decreases further, the molecule starts to tilt to reach a maximum angle of $\sim 50^\circ$ at a slab separation of $\sim 5 \text{ \AA}$; normal stresses can significantly distort the molecule. The tilt angle follows exactly the same reverse pathway when the slabs are separated; there is no evidence of hysteresis. The corresponding plot of energy versus distance for ethyl thiolate (analogous to that shown in Fig. 1) is displayed in Fig. S4.† This predicts that there should be no critical stresses for the sliding-induced mechanochemical decomposition of ethyl thiolate species on Cu(100) and this is borne out by the results shown in Fig. 5B, which plots $\ln(k_p)$ versus contact stress. The rate constants are obtained from the groove depths as a function of the number of passes over the surface as shown in Fig. S5.† Here, the ethyl thiolate was grafted onto the surface from both diethyl disulfide^{25,50} and ethanethiol. They should form identical ethyl thiolate species, and this is verified by finding that they have identical mechanochemical reactions rates. The results show that the rate constant per pass again varies linearly with the applied normal stress over a wide range of values from ~ 0.2 to ~ 1.1 GPa, so obeys the Bell model over the whole range; there is no evidence of the existence of a critical stress for ethyl thiolates adsorbed on Cu(100). Note that the lowest applied stress here corresponds to an almost zero applied normal force (where the actual forces and normal stresses are calculated by including the adhesion between the tip and the substrate). The slope yields a value of activation volume of $43 \pm 1 \text{ \AA}^3$ per molecule (Table 1).

The terminal C–C group of propyl thiolate on Cu(100) is close to perpendicular to the surface, but now with a bend in the chain (see inset to Fig. 6A). Similar compression calculations were carried out and the results are displayed in Fig. S3† where a normal stress induces a significant geometrical change. This is illustrated in Fig. 6A, which plots the angle of the CH_3 –S plane with respect to the surface as a function of the slab separation. The plane is close to perpendicular to the surface during approach, but then undergoes a drastic change to an isomeric state as the slab separation reaches $\sim 5.2 \text{ \AA}$, where the plane moves to an angle of $\sim 8^\circ$ with respect to the surface, but with only a slightly higher energy than the initial configuration. As the slab retracts, the CH_3 –S plane angle increases slightly to $\sim 20^\circ$ at a slab separation of 7.9 \AA , but the angle remains constant indicating that the propyl thiolate reaches a new stable configuration to form a metastable isomer. The approach/retract curve has a significant hysteresis suggesting that there should be a critical stress for the initiation of mechanochemical reactivity. This effect is emphasized by the plot of energy versus distance in Fig. S6.†

Table 1 Values of the activation volumes, $\ln k_p(0)$ and critical stresses for the mechanochemical reactions of methyl, ethyl and propyl thiolate on copper measured from the slopes and intercepts of plots of $\ln k_p$ versus normal stress

	Activation volume/ \AA^3	$\ln k_p(0)$	Critical stress/GPa
Methyl thiolate	31.6 ± 2.5	-9.9 ± 0.5	0.43
Ethyl thiolate	42.6 ± 1.1	-11.3 ± 0.2	None
Propyl thiolate	39.4 ± 3.0	-9.9 ± 0.4	0.33



bifurcation mechanism involved. Roughly speaking there seems to be a general tendency that a shorter molecular length and higher tilting stiffness constants will result in a higher critical force, but this trend will depend in detail on the structure and should be determined for each specific case.

However, this general concept offers the possibility of being able to design tailored adsorbates that are very mechanochemically resistant and could find applications as lubricant additives, as so-called friction modifiers.^{51–53} As an example, carbon nanotube have been proposed to deform by buckling^{54,55} so that assemblies of short, monodispersed, vertical carbon nanotubes can be expected to be very resistant to mechanical damage.

It should also be noted that similar critical effects have been noted for a classical surface tribochemical reaction, that of the antiwear lubricant additive, ZDDP,⁵⁶ and other examples of effects that occur only when a critical stress is applied are given in ref.⁵⁴.

The values of the activation volumes, calculated from the linear portion of the plots of $\ln k_p$ versus normal stress, are summarized in Table 1. The value for ethyl thiolate decomposition, in which there is no critical stress, is larger than for the other two alkyl thiolates, when there are critical stresses.

Furthermore, the values of $\ln k_p(0) \frac{E_{act}}{k_B T}$, which depend on the reaction activation energy, are different when there is a critical stress (methyl and propyl thiolate, $\ln k_p(0) \sim -9.9$) compared to when there is not (ethyl thiolate, $\ln k_p(0) \sim -11.3$). However, because the thermal reactions have similar activation barriers,⁵⁷ according to the Bell model, they should have essentially identical asymptotic values of $\ln k_p(0)$. The observation that they do not could have two sources. The first is that the simple linear Bell model is not sufficient to describe the experimental results and requires the inclusion of quadratic terms in the stress as in the extended-Bell model.⁵⁸ In this case, the reactions could have identical $\ln k_p(0)$ values, but have different coefficients of the F^2 term. Alternatively, the structural change that occurs when the normal stress exceeds the critical stress leads to an initial structure with a lower energy than that of the original reactant that could manifest as an overall lower reaction energy barrier. If this is the case, the activation volume for the conversion of this new initial-state structure to the activated complex would be lower than the activation volume from the lowest-energy initial state to the activated complex. Being able to test whether these ideas are correct will require predictive models for mechanochemical reactions rates.

Conclusions

These results illustrate how adsorbed mechanophores consisting of alkyl thiolate species on copper that react by tilting towards the surface to weaken the C–S bond can exhibit critical stresses in cases in which there is hysteresis in the approach/retract curve. In the case of a vertical methyl thiolate species, the critical stress induces molecular tilt predicted by beam stability theory where a critical normal force is needed to induce molecular tilt. This is confirmed by DFT calculations of the

compression of a methyl thiolate species adsorbed on a Cu(100).

These ideas are further tested using longer-chain alkyl thiolates and are confirmed by finding that an ethyl thiolate, which has a terminus of the alkyl group that is close to parallel to the surface has no hysteresis in the approach/retract curve and the mechanochemical activity shows no critical stress. Critical behavior is found for propyl thiolate where the critical process involves a conformational change due to a normal-stress induced rotation about a C–C bond, implying that critical phenomena can occur either by structural or conformational changes.

The existence of such critical mechanochemical stresses implies that these overlayers are extremely durable under stresses below the critical value and will not be removed. A more fundamental understanding of such effects may result in the design of super mechanically stable surface films.

Data availability

The experimental data can be found in the ESI† and manuscript and is referred to throughout the manuscript.

Author contributions

W. T. T. designed the experiment and wrote the paper and analyzed the data with F. S. R. R. collected the experimental data and N. H. performed the calculations.

Conflicts of interest

The authors declare no competing financial interest.

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