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Geometry-driven carrier extraction enhancement in photovoltaic cells based on arrays of subwavelength light funnels

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Texturing the front surface of thin film photovoltaic cells with ordered or disordered arrangements of subwavelength structures is beneficial in terms of efficient light harvesting as well as efficient carrier extraction. Previous studies demonstrated efficient broadband absorption of solar radiation with surface arrays of subwavelength inverted cones (light funnels – LFs). In the current work, we use three-dimensional finite-difference time-domain electromagnetic calculations as well as three-dimensional device calculations to examine carrier extraction from photovoltaic cells that are composed of LF arrays on top of underlying substrates. For the selected geometry under examination, we show a broadband absorption enhancement of 14% for the LF photovoltaic cell compared with a cell based on the respective optically optimized nanopillar arrays. However, we show that the nominal power conversion efficiency is 60% higher in the LF cell which is due to the enhancement of both open-circuit voltage and short-circuit current. The higher open-circuit voltage in the LF cell is due to the higher injection of photocarriers, and the higher short-circuit current is a result of the unique LF geometry that supports efficient carrier extraction due to the naturally occurring gradients of the quasi-Fermi levels and minority carrier conductivity that allow for enhanced contact selectivity. We believe that this work paves the way towards a new approach for carrier collection in photonic devices for energy applications.

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1. Introduction

Surface arrays composed of subwavelength structures find great applications in the field of photovoltaics as they offer the possibility for both efficient carrier collection and enhanced broadband light absorption of solar radiation.^{1–20} These properties allow for the utilization of scarce and expensive materials for photovoltaic applications and realization of thin-film photovoltaics as well as providing opportunities for efficiency enhancement in the limit of ultra-thin photovoltaics.²¹ Callahan *et al.* suggested that the $4n^2$ Yablonovitch limit for light trapping can be exceeded by allowing absorber local density optical states (LDOSs) that are higher than the respective absorber LDOS bulk values.²² Yu *et al.* developed a statistical temporal coupled-mode theory and demonstrated the possibility of exceeding the Yablonovitch limit in a thin film using a front shallow two-dimensional (2D) grating.²³ Sturmberg *et al.* described absorption enhancement in dense nanopillar (NP) arrays using Bloch modes and showed that absorption enhancement is mainly governed by mode coupling with impinging illumination, moderate mode concentration and

Fabry–Perot oscillations.²⁴ Surface decoration with subwavelength features (*i.e.* *e.g.* nanorods, nanocones, NPs, *etc.*) was investigated both experimentally and numerically and broadband absorption enhancement of solar radiation was demonstrated.^{5,25–43}

Photovoltaic cells based on subwavelength features were experimentally realized with carrier extraction schemes such as all back-side contacts, radial configurations in which the p–n junction is aligned in a core–shell geometry, and axial configurations where the junction is positioned along the height of the subwavelength structure.^{28,29,41,42,44–46} Kayes *et al.* presented a model for pillar arrays with radial junctions and demonstrated carrier extraction enhancement due to the short collection lengths.⁴⁷ Christesen *et al.* examined horizontally aligned silicon nanowires and showed that the open-circuit voltage (V_{oc}) of axial and radial junctions can reach values of $V_{oc} > 0.7$ V and that radial junctions are more immune to surface recombination.⁴⁸ Wong *et al.* calculated the electrical properties of a thin-film photovoltaic cell based on silicon NP arrays and argued the superiority of radial junctions in terms of power conversion efficiency (PCE).²⁰ Wang *et al.* numerically studied axial NP and nanohole arrays and showed that a thin and highly doped emitter provides the optimum compromise in terms of short circuit current (J_{sc}) and V_{oc} .⁴⁹ Li *et al.* analytically modeled NP and nanohole arrays and showed that a high junction depth entails a decrease in efficiency.⁵⁰ Shalev numerically explored

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the effect of junction depth in axial and radial NP arrays and showed that the optimal junction depth in the axial configuration is an interplay between minority carrier diffusion lengths and carrier extraction lengths.³⁵

In a recent series of publications we introduced light funnel (LF) arrays for efficient light trapping and numerically demonstrated broadband absorption of solar radiation.^{12,51–55} Fabrication of silicon LF arrays was also demonstrated.¹² With LFs we refer to subwavelength structures that are inverted with respect to the incoming illumination, such as inverted cones, inverted hyperboloids, parabolic light concentrators (CPC), *etc.* We showed that LF arrays serve as anti-transmission layers in contrast to NP arrays that function as efficient anti-reflection layers.^{26,36} We suggested that the origin of the superior absorption is due to the unique inverted LF geometry that provides enhanced probability for photonic mode excitation and enables strong coupling of the incoming illumination with the individual LFs.

In the present work we numerically examine carrier collection in photovoltaic cells based on LF arrays. Specifically, we consider a photovoltaic cell based on LF arrays on top of a thin substrate with an axial configuration. We show that although the broadband absorption enhancement of the LF cell is 14% higher than that of an equivalent NP photovoltaic cell, the overall photovoltaic efficiency is 60% higher due to geometry-

driven efficient carrier extraction in photovoltaic cells based on LF arrays.

2. Results and discussion

Fig. 1a presents an illustration of a LF array on top of an underlying substrate. The total height of the array-substrate complex is set to 1.5 μm and the period of the both the NP and the LF arrays is set to 500 nm with a top diameter (D_t) of 400 nm to comply with the optically optimized geometry for the absorption of solar radiation.⁴³ The geometry that provides the highest broadband absorption for both the NP array-substrate complex (henceforth, the NP complex) and LF array-substrate complex (henceforth, the LF complex) is for a substrate thickness of 0.3 μm and an array height of 1.2 μm (not shown). Furthermore, the broadband absorption of the LF complex is maximized for a LF bottom diameter (D_b) of 100 nm. The selected dimensions are further indicated for a single unit cell in a LF array in Fig. 1a. Also, the electrical configuration is shown where a shallow axial junction (red line) is considered with a 20 nm n-type phosphorus-doped emitter and a p-type boron-doped absorber with a bottom hole contact. The top emitter contact is indicated by a black filled circle and the bottom absorber contact is indicated by a solid black line. The white lines mark the extent of the depletion region. In order to focus on the specific contribution of the LF geometry to carrier

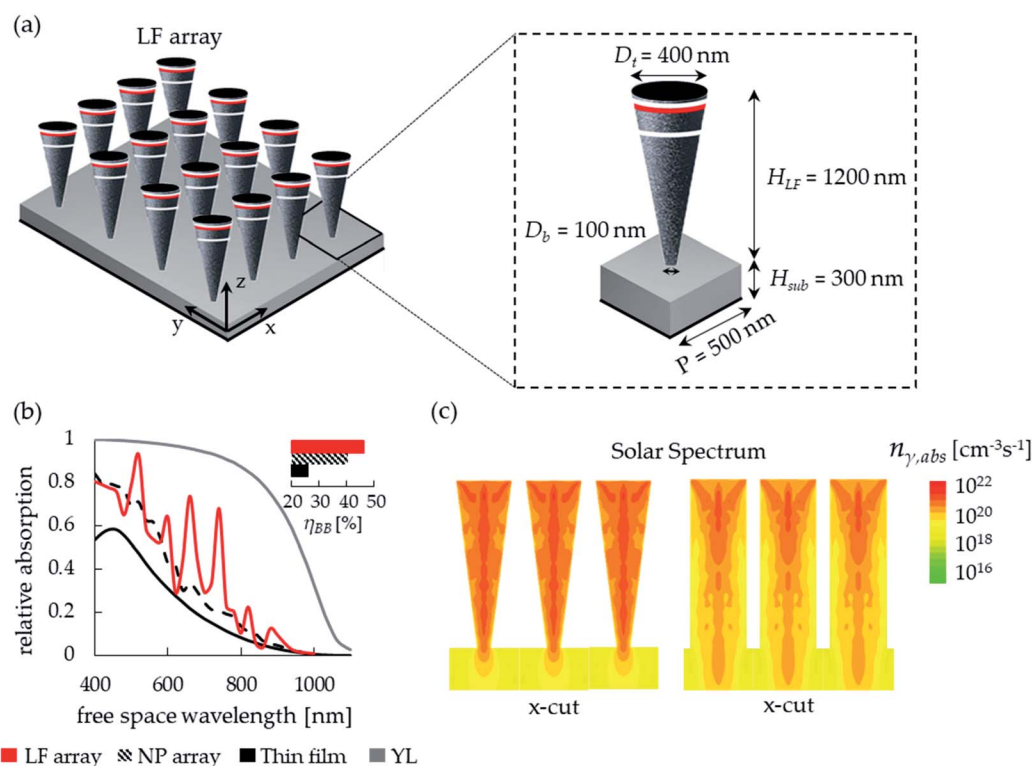


Fig. 1 (a) A schematic of a silicon LF array with an axial junction on top of a thin silicon substrate. The schematic of the unit cell provides the geometry considered in the current work. The black circle on top of the LF indicates the top emitter contact and the bottom black rectangle indicates the bottom absorber contact. (b) Relative absorption spectra of the LF complex, the respective NP complex, a 1.5 μm thin film and the Yablonovitch limit. The inset provides the respective broadband absorption efficiencies. (c) Cross-sections of the LF complex and the NP complex presenting $n_{\gamma,abs}$ under the illumination of the solar spectrum (AM 1.5 G).



collection we do not consider an anti-reflective coating (ARC), a bottom reflector and a back-surface field (BSF). Fig. 1b presents the absorption spectra of the selected LF complex, the NP complex, a thin film of 1.5 μm thickness and the respective Yablonovitch limit (YL). The inset in Fig. 1b presents the broadband absorption efficiency (η_{BB}) with a 14% enhancement of the LF complex over the optically optimized NP complex. Fig. 1c shows the absorbed photon density ($n_{\gamma,\text{abs}}$) under illumination of AM 1.5 G solar radiation for both the LF and NP complexes, in which the stronger excitation of the LF complex is evident.

In the following photovoltaic analysis, we construct LF and NP photovoltaic cells from single unit cells in the respective complexes, as presented in the inset in Fig. 1a for the LF cell. Fig. 2a shows the optical generation profiles along the vertical axes of the NP and LF complexes under both J_{sc} and V_{oc} conditions, where the higher optical generation in the LF complex is evident. Fig. 2b presents current–voltage (I – V) curves for an absorber acceptor doping level (N_{A}) of 10^{18} cm^{-3} for both NP and LF photovoltaic cells, where the photocurrent enhancement of the LF cell is a direct consequence of the enhanced optical generation. We next follow the transition from a NP cell into a LF cell by gradually decreasing the NP bottom diameter from $D_{\text{b}} = 400 \text{ nm}$ to $D_{\text{b}} = 350 \text{ nm}$, 300 nm , 200 nm

and 100 nm . The absorption and the optical generation for each geometry were calculated (not shown). Fig. 2c shows the dependency of J_{sc} and V_{oc} on N_{A} for different D_{b} values. A gradual increase in both V_{oc} and J_{sc} is noticeable with the decrease in D_{b} for the full range of N_{A} values. Note that V_{oc} reaches a maximum for $N_{\text{A}} = 10^{18} \text{ cm}^{-3}$ which is a direct consequence of the saturation current dependency on N_{A} and minority carrier lifetimes which also depend on N_{A} . The respective electron diffusion lengths (L_{n}) are also presented in Fig. 2c. Fig. 2d presents the dependency of the nominal power conversion efficiency (nPCE), defined as $J_{\text{sc}} \times V_{\text{oc}} / P_{\text{in}}$ where P_{in} is the power of the solar spectrum at AM 1.5 G, on N_{A} for all the considered D_{b} values. The nPCE values of all cells peak at $N_{\text{A}} = 10^{17} \text{ cm}^{-3}$. The highest nPCE = 8% is obtained for the smallest $D_{\text{b}} = 100 \text{ nm}$ as compared with the NP cell with an nPCE of 5% which reflects an nPCE enhancement of 60%. This is surprising as the η_{BB} enhancement is only 14%. In order to understand the origin of the 60% nPCE enhancement we next carefully examine the behavior of J_{sc} and V_{oc} of both LF and NP cells.

The V_{oc} enhancement of the LF cell over the NP cell decreases with an increase in N_{A} with a highest value of 15% for $N_{\text{A}} = 10^{15} \text{ cm}^{-3}$, and with a corresponding J_{sc} enhancement of 23% (see Fig. 2c). V_{oc} is equal to the splitting of the quasi-Fermi levels ($\varepsilon_{\text{fc}} - \varepsilon_{\text{fv}}$, where ε_{fc} is the electron quasi-Fermi level and ε_{fv} is the

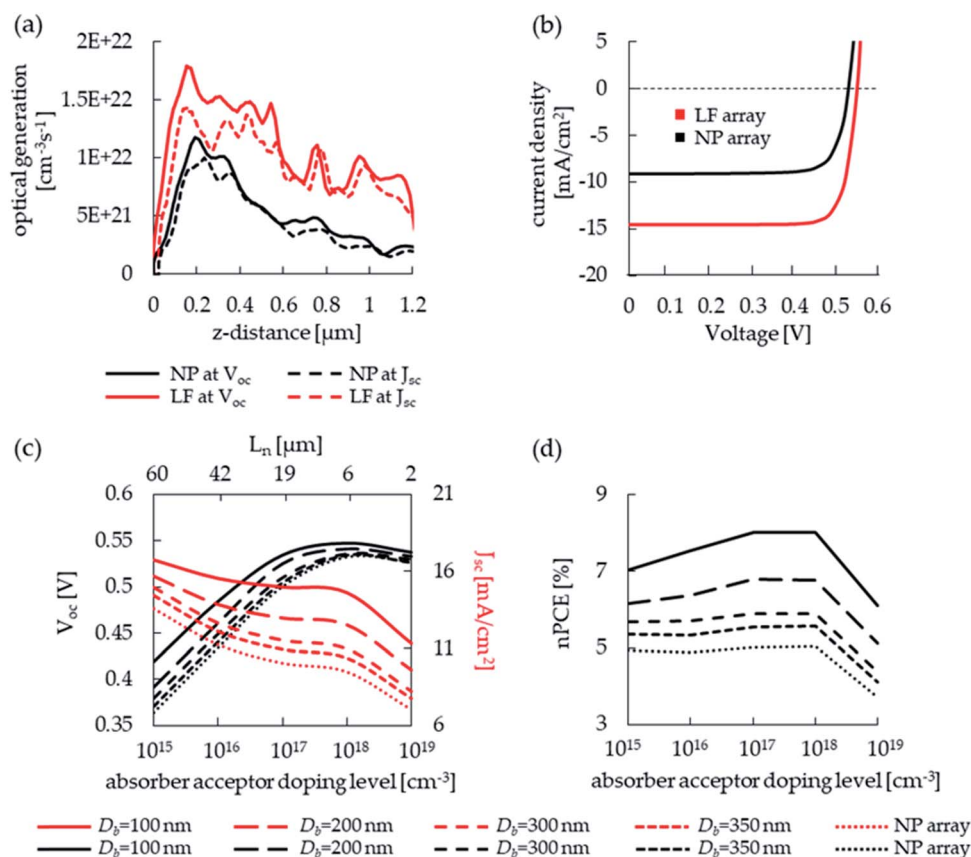


Fig. 2 (a) Optical generation profiles along the z-axis for the LF and NP cells under V_{oc} and J_{sc} conditions. Note that $z = 0$ is the top of the LF. (b) I – V curves of the LF cell and the NP cell for $N_{\text{A}} = 10^{18} \text{ cm}^{-3}$ in which the J_{sc} enhancement in the LF cell is evident. (c) The dependency of V_{oc} and J_{sc} on N_{A} for different D_{b} values. The top x-axis presents the respective electron minority carrier diffusion lengths. (d) The dependency of nPCE on N_{A} for the different D_{b} values.

hole quasi-Fermi level), between the top emitter electron contact and the bottom absorber hole contact, and it is equal to the free energy delivered to the load. Fig. 3a and b present the energy band diagrams along the vertical axes of the LF cell and the NP cell for $N_A = 10^{15} \text{ cm}^{-3}$ and 10^{19} cm^{-3} , respectively. The cross-sections of LF and NP cells above the band diagrams visualize the considered orientation. The V_{oc} values extracted from the energy band diagrams for $N_A = 10^{15} \text{ cm}^{-3}$ are 419 mV and 364 mV for the LF and the NP cells, respectively, and similarly for $N_A = 10^{19} \text{ cm}^{-3}$ the V_{oc} values are 537 mV and 527 mV. The V_{oc} values extracted from the energy band

diagrams are in agreement with the V_{oc} values extracted from the I - V curves (Fig. 2c). Next, we examine the origin of the quasi-Fermi level splitting and its dependency on N_A . For a p-type absorber (1) $V_{oc} = kT \ln(1 + \Delta n_e/n_{e0})$, where k is the Boltzmann constant, T is the cell temperature (300 K), Δn_e is the injected photoelectron density and n_{e0} is the equilibrium electron density.⁵⁶ Fig. 3c and d show the Δn_e profiles where for $N_A = 10^{15} \text{ cm}^{-3}$ the densities are higher than for $N_A = 10^{19} \text{ cm}^{-3}$ due to the doping-dependent lifetimes (see methodology). Also, while for $N_A = 10^{15} \text{ cm}^{-3}$ Δn_e of the LF is significantly higher, for $N_A = 10^{19} \text{ cm}^{-3}$ Δn_e values of the LF and NP are similar.

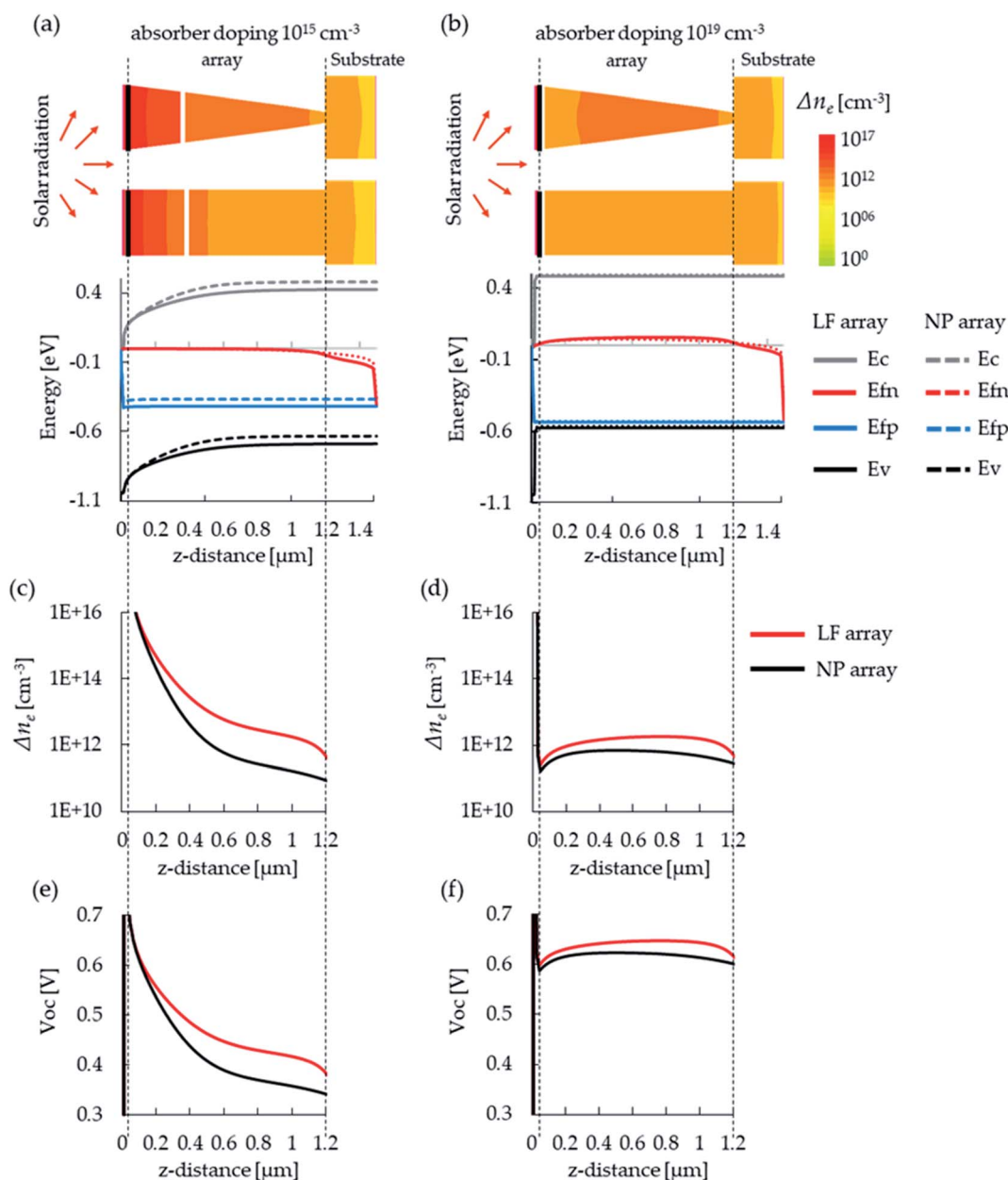


Fig. 3 V_{oc} conditions: (a) energy band diagrams along the z -axis for LF and NP cells for $N_A = 10^{15} \text{ cm}^{-3}$. The cross-sections on top show the respective electron density distribution as well as the location of the metallurgical axial junctions (black line) and depletion lines (white lines). (b) The same as (a) for $N_A = 10^{19} \text{ cm}^{-3}$. (c) Δn_e profiles along the z -axis for $N_A = 10^{15} \text{ cm}^{-3}$. (d) The same as (c) for $N_A = 10^{19} \text{ cm}^{-3}$. (e) Spatially resolved V_{oc} along the z -axis for $N_A = 10^{15} \text{ cm}^{-3}$. (f) The same as (e) for $N_A = 10^{19} \text{ cm}^{-3}$.



Fig. 3e and f present the respective calculated spatially resolved V_{oc} profile for a p-type absorber according to (1). The origin of the higher V_{oc} of the LF cell for $N_A = 10^{15} \text{ cm}^{-3}$ is now apparent; the higher broadband absorption and the optical generation of the LF cell entail a higher population of electron minority carriers in the absorber which, for most of the 1D profile, is about one order of magnitude higher than that in the NP cell. This considerably higher excitation of the absorber directly translates into a higher V_{oc} . This difference in absorber excited minority carriers disappears for $N_A = 10^{19} \text{ cm}^{-3}$ due to the higher Shockley–Read–Hall (SRH) recombination. However, note that a higher N_A presents a higher V_{oc} due to the absorber n_{e0} which is three orders of magnitude smaller for $N_A = 10^{19}$

cm^{-3} . The enhanced absorber photoelectron density for $N_A = 10^{15} \text{ cm}^{-3}$ is also apparent in the 2D cross-section presented in Fig. 3a. Therefore, the higher V_{oc} at $N_A = 10^{15} \text{ cm}^{-3}$ in the LF cell is a combination of a higher carrier injection and a lower level of recombination.

The J_{sc} enhancement of the LF cell compared with the NP cell increases with N_A from 24% to 61% for $N_A = 10^{15} \text{ cm}^{-3}$ to 10^{19} cm^{-3} , respectively (see Fig. 2c). The generation of photocurrent reflects the conversion efficiency of chemical energy into electrical energy. The electron current is described by $J_e = \sigma_e / q \text{ grad}(\epsilon_{fn})$, where $\text{grad}(\epsilon_{fn})$ is the gradient of the electron quasi-fermi level, q is the elementary charge and σ_e is the electron conductivity equal to $n_e q \mu_e$ where n_e is the electron density and

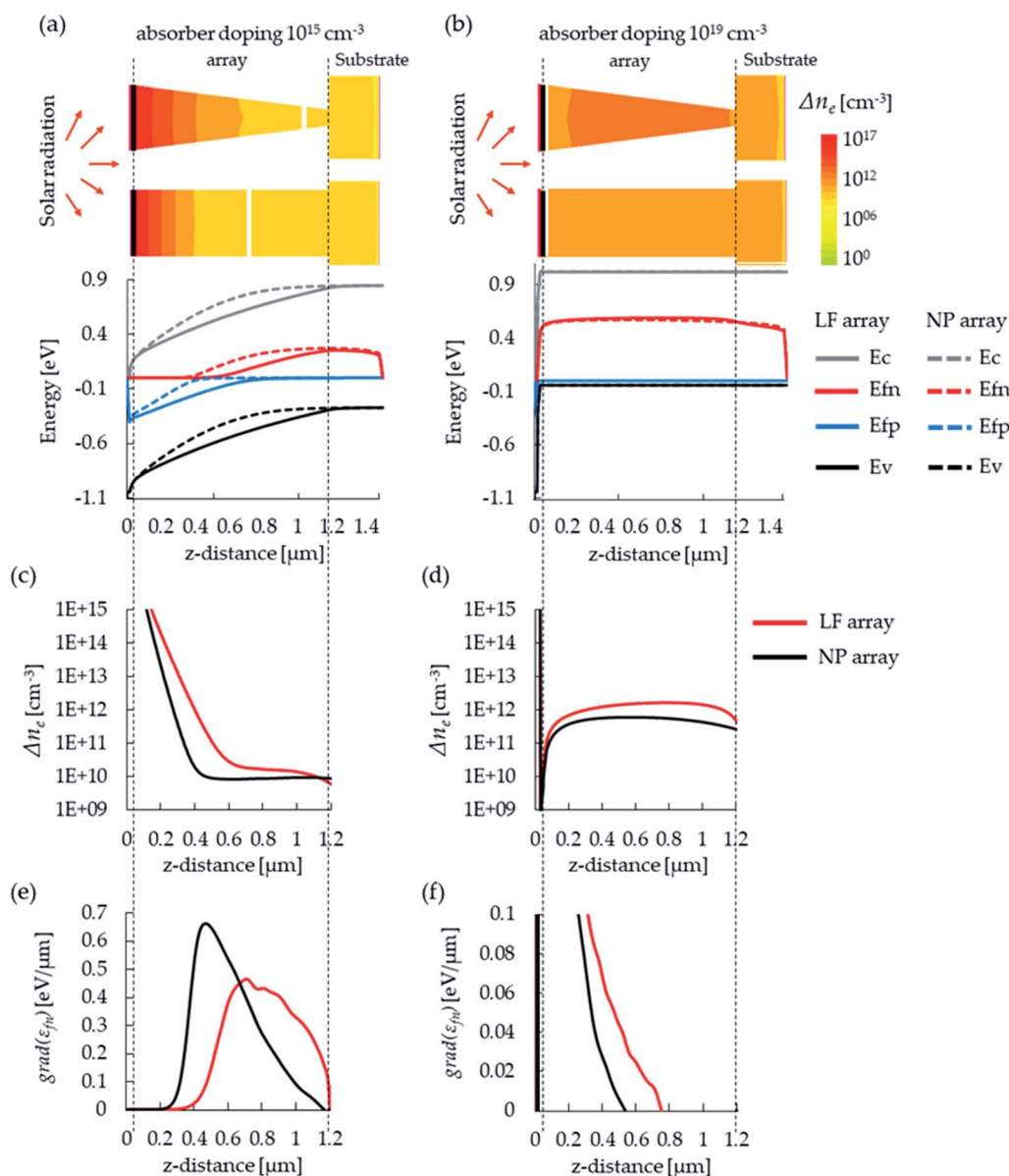


Fig. 4 J_{sc} conditions: (a) energy diagrams along the z -axis for LF and NP cells for $N_A = 10^{15} \text{ cm}^{-3}$. The cross-sections on top show the respective electron density distribution as well as the location of the metallurgical axial junctions (black line) and depletion lines (white lines). (b) The same as (a) for $N_A = 10^{19} \text{ cm}^{-3}$. (c) Electron density profiles along the z -axis for $N_A = 10^{15} \text{ cm}^{-3}$. (d) The same as (c) for $N_A = 10^{19} \text{ cm}^{-3}$. (e) $\text{grad}(\epsilon_{fn})$ profiles along the z -axis for $N_A = 10^{15} \text{ cm}^{-3}$. (f) The same as (e) for $N_A = 10^{19} \text{ cm}^{-3}$.



μ_e is the electron mobility. Hence a higher σ_e and $\text{grad}(\varepsilon_{\text{fn}})$ along the electron path towards the emitter contact will induce greater emitter selectivity towards electrons and therefore a higher J_e . Fig. 4a and b show the energy band diagrams of the NP and LF cells under J_{sc} conditions for $N_A = 10^{15} \text{ cm}^{-3}$ and 10^{19} cm^{-3} , respectively, Fig. 4c and d present the respective n_e which is linearly proportional to σ_e , and Fig. 4e and f present the respective $\text{grad}(\varepsilon_{\text{fn}})$ for which it is positive. For $N_A = 10^{15} \text{ cm}^{-3}$ n_e , and hence σ_e , in the LF cell increases towards the emitter contact more appreciably which provides an enhanced emitter selectivity towards electrons in the LF cell compared with that of the NP cell. $\text{grad}(\varepsilon_{\text{fn}})$ for $N_A = 10^{15} \text{ cm}^{-3}$ is positive for both cells, which indicates a decrease in ε_{fn} towards the emitter, but it is not necessarily higher in the LF cell as shown in Fig. 4e. Overall for $N_A = 10^{15} \text{ cm}^{-3}$ the combined effect of n_e and $\text{grad}(\varepsilon_{\text{fn}})$ results in 24% J_{sc} enhancement. For $N_A = 10^{19} \text{ cm}^{-3}$ (Fig. 4f) both σ_e and $\text{grad}(\varepsilon_{\text{fn}})$ (*i.e.* where $\text{grad}(\varepsilon_{\text{fn}}) > 0$) are higher in the LF cell. Therefore, the combined enhancement of σ_e and $\text{grad}(\varepsilon_{\text{fn}})$ results in an overall J_{sc} enhancement of 61% in the LF cell compared with the NP cell. Importantly, the origin of the higher $\text{grad}(\varepsilon_{\text{fn}})$ in the LF cell is due to the gradient in the electron chemical potential which is due to the higher n_e at the LF bottom part which is a direct consequence of the unique LF inverted geometry.

3. Conclusions

LF arrays provide efficient broadband absorption of solar radiation that is superior to recent advances in the field. In the current work we show that the unique LF inverted geometry provides additional opportunities for efficient carrier extraction and photovoltaic efficiency enhancement. We show that the relatively high absorption affects the open-circuit voltage on the one hand, and the gradient of the quasi-Fermi level and the minority carrier conductivity in the absorber allow for short-circuit current enhancement, on the other hand. These effects coupled with the right selection of doping levels result in a significant efficiency enhancement. We believe this approach to be important to other absorption-based photonic devices in which carrier extraction is important.

4. Methods

4.1. Finite-difference time-domain electromagnetic calculations

We use 3D finite-difference time-domain (FDTD) electromagnetic calculations with the Advanced TCAD package by Synopsys (Mountain View, CA, USA). The optical excitation is performed with a normally incident plane wave polarized along the x-axis in the spectral range of 400–1100 nm in 20 nm steps. The simulation box size is set to the size of the square unit cell with a periodic boundary condition along the lateral dimensions, and the boundary condition along the vertical axis is set to complementary perfectly matched layers (CPML). The periodic boundary condition is applied to normally incident plane wave excitation using the total-field scattered-field (TFSF) formulation. Both the magnetic and electric fields are

copied directly from the periodic facet to the opposing one during field update. The numbers of absorbed photons, reflected photons and transmitted photons are extracted at each wavelength using sensors that are located above and below the unit cell, and the respective relative absorption, reflection and transmission are calculated. The absorbed photon density ($n_{\gamma,\text{abs}}$) is calculated for each wavelength. $n_{\gamma,\text{abs}}$ is calculated by dividing the absorbed power density ($W = -\nabla S_{\text{AV}} = \frac{1}{2} \sigma |E|^2$), where S_{AV} is the time-averaged Poynting vector, σ is the non-zero conductivity and E is the electric field) by the energy of the incident photon. For efficient and accurate FDTD calculations, the maximum mesh cell size is kept smaller than 1/10th of the wavelength in silicon (more than 10 nodes per wavelength). The broadband absorption efficiency (η_{BB}) is the relative absorption averaged and weighted with the solar spectrum. The considered solar spectrum is Air Mass 1.5 Global (AM 1.5 G). The optical constants of the silicon material are taken from the literature.⁵⁷

4.2. Electrical device calculations

We use 3D device calculations (Sentaurus, Synopsys Inc.) to examine the optoelectronic and the photovoltaic performance. The Poisson and the Continuity equations are solved at each mesh point for a carrier generation profile, which is calculated from η_{BB} . The bottom and top contacts define the vertical boundary conditions. The calculated photovoltaic cells are composed of a degenerately phosphorus-doped $5 \times 10^{19} \text{ cm}^{-3}$ emitter (n-type) and a boron-doped absorber (p-type). The carrier generation profile is calculated as follows: for excitation energy greater than or equal to the bandgap energy, the quantum efficiency is set to one, and otherwise, it is set to zero. In every mesh point, the Poisson and the Continuity equations are solved, in which the doping-dependent Shockley–Read–Hall (SRH) recombination, Auger recombination, the bandgap renormalization for degenerately doped silicon and the doping dependent mobility are all accounted for. We consider a standard Czochralski (cz) silicon and the material parameters are set accordingly. The rate of Auger recombination is calculated in the following manner:⁵⁸

$$R_{\text{net}}^{\text{A}} = (C_n n + C_p p) (np - n_{\text{i,eff}}^2), \quad (1)$$

where C_n and C_p were set to $2.9 \times 10^{-31} \text{ cm}^6 \text{ s}^{-1}$ and $1 \times 10^{-31} \text{ cm}^6 \text{ s}^{-1}$, respectively.⁵⁸ The rate of SRH is calculated in the following manner:⁵⁸

$$R_{\text{net}}^{\text{SRH}} = \frac{np - n_{\text{i,eff}}^2}{\tau_p(n + n_1) + \tau_n(p + p_1)}, \quad (2)$$

where n and p are the respective electron and hole carrier densities, $n_{\text{i,eff}}$ is the effective intrinsic density (accounting for bandgap narrowing), τ_n and τ_p are the respective electron and hole lifetimes, and n_1 and p_1 are:

$$n_1 = n_{\text{i,eff}} \exp\left(\frac{E_{\text{trap}}}{kT}\right) \quad (3)$$



$$p_1 = n_{i,\text{eff}} \exp\left(\frac{-E_{\text{trap}}}{kT}\right), \quad (4)$$

where E_{trap} , the difference between the defect level and the intrinsic level, is set to zero. The dependency of SRH recombination on doping is reflected in the dependency of carrier lifetime on doping:

$$\tau_{\text{doping}}(N_A + N_D) = \tau_{\text{min}} + \frac{\tau_{\text{max}} - \tau_{\text{min}}}{1 + \left(\frac{N_A + N_D}{N_{\text{ref}}}\right)^{\gamma}}, \quad (5)$$

where N_A and N_D are the acceptor and donor doping levels, respectively. We select $\gamma = 1$, $\tau_{\text{min}} = 0$, and $N_{\text{ref}} = 10^{16} \text{ cm}^{-3}$ for both holes and electrons, and $\tau_{\text{max}} = 10^{-6}$ seconds for electrons and holes, respectively. The considered diffusion coefficient for the electron minority carriers is $36 \text{ cm}^2 \text{ s}^{-1}$.

Conflicts of interest

The authors declare no conflict of interest.

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