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Strain-induced tunable valley polarization and topological phase transition in SVSiN₂ monolayer†

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The potential application of a two-dimensional (2D) ferrovalley semiconductor in the field of valleytronics has sparked extensive research interest. Using first-principles calculations, we predict that the SVSiN₂ monolayer is a promising ferrovalley material with excellent dynamical and thermal stability, and its Curie temperature is around room temperature. A giant valley polarization of −72.73 meV is obtained by shifting the magnetization direction from in-plane to out-of-plane. The valley-contrasting properties of the SVSiN₂ monolayer can be remarkably modulated by in-plane strains. Most importantly, topological phase transition is predicted to be realized by a 5.5–6% tensile strain, which is verified by the nonzero Chern number and the nontrivial edge state. Compared to the in-plane strain modulation, the valley-dependent properties of the SVSiN₂ monolayer are robust to vertical electric fields. Our findings could enrich the physical understanding of the effects of manipulating the valley-dependent properties of 2D ferrovalley semiconductors, facilitating potential applications of 2D Janus monolayers for valleytronics.

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1 Introduction

A valley, which is defined as a local extremum in momentum space, can be used to manipulate information encoding, transfer, and processing.¹ Correspondingly, valleytronics that relying on manipulating the emergent degree of freedom of a valley, has received increasing research focus in recent years.² However, valleys may degenerate in terms of energy aspect due to the protection of time reversal symmetry. As a result, breaking the degeneracy of valleys is crucial for fabricating high-storage density and low-energy electronic devices.³ Over the past decade, the 2D transition metal dichalcogenides (TMDs) monolayer with broken inversion symmetry and spin-orbit coupling (SOC) has extensively promoted the development of valleytronics.^{4–7} Non-equilibrium distributions for valley carriers in TMDs can be realized by many routes, including the valley contrasting optical selection rule, the Zeeman effect of the external magnetic field, magnetic atom doping, and magnetic proximity effect.^{6–11} However, some drawbacks are accompanied with the implementation of these routes. For example, the optical pumping method demands harsh experimental conditions. The efficiency of valley polarization generated by an external magnetic field is very low.

Regarding magnetic atom doping, it may lead to unstable valley polarization as a result of introducing impurity scattering between different valleys. Fortunately, the 2D intrinsic ferrovalley materials provide new opportunities to solve these issues. Therefore, it is necessary to explore novel intrinsic ferrovalley semiconductors (FVS) with emerging valley-related properties.

Monolayered FVS exhibit not only spontaneous valley polarization, but also valley-contrasting transport under the optical selection rule resulting from spin-valley coupling. This is attributed to the presence of inherent long-range ferromagnetism combined with the SOC effect, and furthermore, the ferromagnetism is crucial because it breaks the time-reversal symmetry of the system.^{12,13} In addition, some emergent quantum states, such as topological states and half-valley-metal (HVM) states, are predicted to be achievable using a finite strain on the FVS material.^{14,15} However, only a few 2D materials are shown to exhibit spontaneous valley polarization, such as the monolayers of 2H-VSe₂,¹⁶ Nb₃I₈,¹⁷ NbX₂,¹⁸ and GdI₂.¹⁹ Moreover, most 2D monolayers under consideration essentially possess an in-plane easy magnetization axis. In contrast, the FVS materials with tunable multiple valley states and out-of-plane magnetization are rarely reported.²⁰ Correspondingly, searching for a new intrinsic FVS materials is of great importance to broaden the practical application of the valleytronics.²¹

To date, most intrinsic FVS materials are synthesized or proposed on the basis of binary or ternary chemical compounds.^{22–27} In recent years, layered 2D materials MoSi₂N₄ and WSi₂N₄ have been prepared through chemical vapor deposition (CVD).²⁸ Many theoretical investigations are devoted

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to the understanding of MA_2Z_4 ($\text{M} = \text{Cr}, \text{Mo}, \text{W}, \text{V}, \text{Nb}, \text{Ta}, \text{Ti}, \text{Zr}$ or Hf ; $\text{A} = \text{Si}$ or Ge ; and $\text{Z} = \text{N}, \text{P}, \text{As}$) based 2D materials, using first principles calculations. The MA_2Z_4 family has emerging topological, magnetic, valley, superconducting, and catalytic properties.^{29–34} Hence, the physical properties of various MA_2Z_4 -based van der Waals (vdW) heterostructures have also been investigated to explore their electronic and optoelectronic applications.^{35,36}

In this work, we propose a Janus SVSiN_2 monolayer with five layers of atoms, which can be obtained from the VSi_2N_4 monolayer by replacing one side of the N–Si–N atom with an S atom. It can be regarded as a 2D Janus material with reflection symmetry breaking.³⁷ The SVSiN_2 monolayer is predicted to be a FVS material with a Curie temperature of 260 K. It has excellent thermal and dynamical stability. We predict that a large valley polarization of -72.73 meV can be achieved by switching the magnetization direction of the SVSiN_2 monolayer from the in-plane direction to the out-of-plane direction. A tight-binding model is used to elucidate the anomalous valley Hall effect (AVHE) induced by the valley polarization and the opposite Berry curvatures at the K/K' valleys in the SVSiN_2 monolayer. Strain and electric field are also introduced to tune the valley polarization and Berry curvature of the system. Most importantly, a biaxial tensile strain of 5.5–6% can induce valley quantum anomalous Hall effect. Our findings broaden the knowledge of 2D ferrovalley materials and deepen the understanding of strain-induced topological and valley states in the Janus SVSiN_2 monolayer.^{38–41}

2 Computational methods

All our first-principles calculations are based on density functional theory (DFT) implemented using the Vienna *ab initio* simulation package (VASP).^{42,43} The Perdew–Burke–Ernzerhof (PBE) exchange–correlation function of the generalized gradient approximation (GGA) was utilized to calculate the structural relaxation and electronic structure.⁴⁴ We use the GGA+*U* method to describe the strong correlation correction of V-3d orbitals. We test various *U*-values and compare them with the electronic structures obtained from the hybrid functional HSE06,⁴⁵ which typically gives an accurate electronic structure. It is found that the calculated results obtained from GGA+*U* and HSE06 agree well when $U_{\text{eff}} = 3.2$ eV. To avoid interlayer interactions, a vacuum layer of 20 Å is considered along the *z*-axis direction. The cutoff energy is 500 eV for the plane-wave basis. To fully optimize the structure, the convergence criteria for total energy and atomic residual force are 1×10^{-8} eV and $0.001 \text{ eV } \text{\AA}^{-1}$, respectively. The first Brillouin zone integration is carried out using $16 \times 16 \times 1$ Γ -centered *k*-grids.⁴⁶ The $9 \times 16 \times 1$ Monkhorst–Pack *k*-meshes are used to calculate ferromagnetic (FM)/antiferromagnetic (AFM) energy using rectangular superlattices. Table S1 (ESI†) shows that the effects of dipole correction on the geometric structure and electronic property are negligible. The calculations regarding the SVSiN_2 monolayer will not consider the dipole correction hereafter. The SOC effect is

considered to study the magnetocrystalline anisotropy and electronic properties of the SVSiN_2 monolayer. The phonon dispersion of a $4 \times 4 \times 1$ supercell is calculated using density functional perturbation theory and PHONOPY code.⁴⁷ The *ab initio* molecular dynamics (AIMD) simulations were carried out using a $4 \times 4 \times 1$ supercell at 300 K. The VASPBERRY subroutine is used to calculate the materials' Berry curvature and circular polarization.⁴⁸ In addition, we construct the maximum localized Wannier function (MLWF) using the WANNIER90 package,⁴⁹ and calculate the edge states and anomalous Hall conductivity with the help of WANNIERTOOLS subroutine.⁵⁰ Based on the Heisenberg model, we perform Monte Carlo (MC) simulations on a $10 \times 10 \times 1$ supercell using the multi-dimensional Curie Temperature Simulation Package.⁵¹ All crystal structures are visualized by VESTA software.⁵²

3 Results and discussion

3.1 Atomic structure and stability

We first study the atomic and electronic structures of SVSiN_2 , as shown in Fig. 1(a) and (b). The stacking order of the SVSiN_2 monolayer is S–V–N–Si–N, which can be considered to be a Janus structure. The lattice constant of the SVSiN_2 monolayer is $a = b = 2.952$ Å. The crystal symmetry of the SVSiN_2 monolayer is C_{3v} . Similar to the TMDs, the inversion symmetry of the SVSiN_2 monolayer is also broken. We conduct AIMD simulations to explore the thermal stability of the SVSiN_2 monolayer, as illustrated in Fig. 2(a).

During a simulation time of 5 ps, the simulated results show that the total energy fluctuation is not significant, and is always near the equilibrium value at a temperature of 300 K. As shown in the inset of Fig. 2(a), there is no significant structural break in the final snapshot of the SVSiN_2 monolayer. The calculated AIMD result indicates that the SVSiN_2 monolayer possesses excellent thermal stability at room temperature. The phonon dispersion shown in Fig. 2(b) illustrates that there is no imaginary frequency in any branches, ensuring the dynamical stability of the SVSiN_2 monolayer. The structural stability is

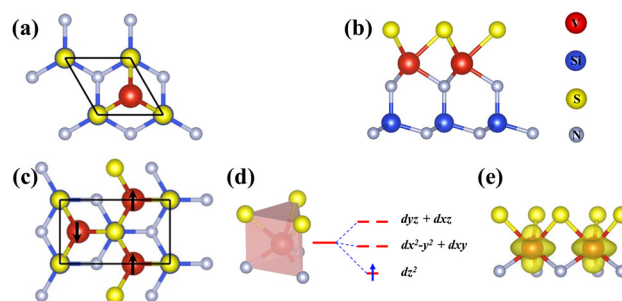


Fig. 1 Top- (a) and side-views (b) of the primitive structure of the SVSiN_2 monolayer. (c) The top view of a rectangular supercell for magnetic ground state calculations. For the AFM configuration, the spin directions are marked with black arrows. (d) A schematic diagram of the d-orbital energy levels of the V ion in a trigonal prismatic crystal field, and (e) shows the spin density distribution of the SVSiN_2 monolayer.



Fig. 2 (a) AIMD calculation and (b) phonon spectrum of the SVSiN₂ monolayer.

evaluated by its formation energy (E_{form}), which is defined as:

$$E_{\text{form}} = \frac{E_{\text{total}} - E_{\text{t}}(\text{S}) - E_{\text{t}}(\text{V}) - E_{\text{t}}(\text{Si}) - 2E_{\text{t}}(\text{N})}{N} \quad (1)$$

where E_{total} is the total energy of the SVSiN₂ monolayer, and E_{t} is the energy of each constituent element in their standard state (per atom). The calculated formation energy of the SVSiN₂ monolayer is -0.93 eV per atom, which is very close to the corresponding value (-0.96 eV per atom) reported previously for the SMOsiN₂ monolayer.⁵³ The negative formation energy indicates the possible experimental feasibility of the 2D monolayer. Therefore, the SVSiN₂ monolayer is predicated to be more feasible in experimental fabrication compared to the SeMoSiN₂ ($E_{\text{form}} = -0.77$ eV per atom) and TeMoSiN₂ ($E_{\text{form}} = -0.46$ eV per atom) monolayers.⁵³

3.2 Magnetic ground state

We investigate the electron occupancy in V atoms based on crystal field theory. In a trigonal prismatic crystal field environment, the V-d orbitals split into a low-lying d_{z^2} orbital, followed by (d_{xy} , $d_{x^2-y^2}$) and (d_{xz} , d_{yz}) orbitals. Among them, an unpaired electron occupies the d_{z^2} orbital, which is evidenced by the spin density distribution of the occupied V-d orbital exhibited in Fig. 1(d) and (e), which generates a net magnetic moment of $1\mu_{\text{B}}$ into the SVSiN₂ monolayer. In Fig. S1(a) (ESI[†]), we evaluate the effects of different U_{eff} values on the magnetic moments of the V atom. The calculated results show that the atomic magnetic moments obtained are in the range 2–4 eV, which agrees well with the theoretical values. The average distance between two V atoms in the SVSiN₂ is 2.952 Å. Such a large atomic distance results in a weak direct exchange interaction force between the V atoms. And the super-exchange mechanism is considered to dominate the interaction between V atoms since the V–N–V angle is close to 90°. According to the Goodenough–Kanamori rule,^{54,55} the SVSiN₂ monolayer adopts FM-ordered ground states and forms FM coupling, which is attributed to the overlap of V- d_{z^2} and N-p orbitals.

We also calculate the energy difference (ΔE) with respect to different U_{eff} values between the AFM- and FM-ordered states by $\Delta E = E_{\text{AFM}} - E_{\text{FM}}$, as presented in Fig. S1(b) (ESI[†]). The rectangular supercell shown in Fig. 1(c) is employed for the ΔE calculation. The results indicate that the SVSiN₂ monolayer remains in the FM ground state with the U_{eff} value changing within the range 0–5 eV. Compared to the calculated ΔE results

under different U_{eff} with the corresponding HSE06 results, we find that two calculations agree well when $U_{\text{eff}} = 3.2$ eV. The calculated local magnetic moment of the system in Fig. S1(a) (ESI[†]) is about $1.044\mu_{\text{B}}$ with $U_{\text{eff}} = 3.2$ eV, which is consistent with the above analysis in Fig. 1(d). Moreover, the band structures of the SVSiN₂ monolayer under different U_{eff} values is shown in Fig. S2 (ESI[†]). It can be seen that the SVSiN₂ is a half-metal when $U_{\text{eff}} = 0$ eV. When the U_{eff} value changes in the range 3–4 eV, the band structure of the SVSiN₂ monolayer is qualitatively consistent with that obtained from HSE06. In addition, the projected density of states shown in Fig. S3 (ESI[†]) demonstrates that there is no significant difference in orbital contributions between PBE+ U and HSE06. Therefore, in the following discussion, we choose $U_{\text{eff}} = 3.2$ eV to investigate the spin valley coupling of the SVSiN₂ monolayer.

When the SOC effect is considered, the direction of susceptibility depends on the area where the electron clouds overlap, which can be described by the magnetic anisotropy energy (E_{MAE}) and is calculated by:

$$E_{\text{MAE}} = E_{\text{MCA}} + E_{\text{MSA}} \quad (2)$$

where E_{MCA} and E_{MSA} refer to the magnetic crystal anisotropy energy and magnetic shape anisotropy energy, respectively. The E_{MCA} is attributed to the SOC effect, and it is defined as:

$$E_{\text{MCA}} = E_{[100]} - E_{[001]} \quad (3)$$

where $E_{[100]}$ ($E_{[001]}$) represent the total energy of the SVSiN₂ monolayer with an in-plane (out-of-plane) magnetic moment.⁵⁶ The E_{MSA} is contributed by the dipole–dipole (D–D) interaction, which tends to make the direction of spin parallel to the monolayer.⁵⁷ The D–D interaction can be defined as:

$$E_{\text{D-D}} = \frac{\mu_0}{8\pi} \sum_{i \neq j} \frac{1}{r_{ij}^3} \left[\vec{M}_i \cdot \vec{M}_j - \frac{3}{r_{ij}^2} (\vec{M}_i \cdot \vec{r}_{ij}) (\vec{M}_j \cdot \vec{r}_{ij}) \right] \quad (4)$$

where $\vec{M}_i$ represents the magnetic moment of the V atom at position i , and $\vec{r}_{ij}$ represents the vector of V atoms at positions i and j . Correspondingly, E_{MSA} can be expressed as:

$$E_{\text{MSA}} = E_{\text{D-D}}^{[100]} - E_{\text{D-D}}^{[001]} = \frac{3\mu_0 M^2}{2 \cdot 4\pi} \sum_{i \neq j} \frac{1}{r_{ij}^3} \cos^2 \theta_{ij} \quad (5)$$

where θ_{ij} is the angle between $\vec{M}_i$ and $\vec{r}_{ij}$. The E_{MCA} values calculated at different k -meshes are plotted in Fig. S4 (ESI[†]). It is noted that the E_{MCA} results are almost unchanged when the k -meshes are increased from $16 \times 16 \times 1$ to $28 \times 28 \times 1$, indicating that a converged result is obtained. The E_{MAE} is predicted to be $-93.08 \mu\text{eV}$ with $E_{\text{MCA}} = -75.88 \mu\text{eV}$ and $E_{\text{MSA}} = -17.20 \mu\text{eV}$. Our calculated value of E_{MSA} agrees well with $E_{\text{MSA}} = -17 \mu\text{eV}$ reported in the case of the monolayered VSIGeN₄.⁵⁸ It is noticed that the calculated E_{MSA} values are approximately -14 to $-17 \mu\text{eV}$ for VSIGeN₄ ($-16 \mu\text{eV}$) and VSIN₄ ($-14 \mu\text{eV}$) and VSIN₄ ($-17 \mu\text{eV}$) monolayers,⁵⁹ suggesting that the D–D interaction between the V atoms are very similar. In contrast, the E_{MCA} is defined as the energy difference between the in-plane (x -direction) spin configuration and out-of-plane (z -direction) spin configuration. Our calculated E_{MSA}

indicates that the SOC effect makes the SVSiN₂ monolayer have in-plane spin configuration, which is more prominent than that in the VSi₂N₄ monolayer ($E_{\text{MCA}} = -42$ to -64 μeV).^{29,59} Moreover, we calculated the influence of different U_{eff} values on E_{MCA} . With the enhancement of the Coulomb repulsion effect, it is expected to induce the spin configuration of the SVSiN₂ monolayer to shift from an in-plane to out-of-plane direction. This anticipation is confirmed by Fig. S5 (ESI[†]). The calculated E_{MCA} is found to change to a positive value when $U_{\text{eff}} = 5$ eV. Hence, the negative E_{MAE} means that the magnetization axis of the SVSiN₂ monolayer is parallel to the plane of the monolayer, revealing that the SVSiN₂ monolayer is a 2D XY magnet.^{60,61} In principle, the magnetization orientation of the SVSiN₂ monolayer can be elaborately modulated from the in-plane direction to the out-of-plane direction by overcoming a 93.08 μeV energy barrier. Furthermore, the negative E_{MAE} is also obtained in the 2D VSi₂N₄ and Janus VSiGeN₄ and VSiSnN₄ monolayers.⁵⁹

To further explore the nature of the in-plane E_{MAE} , we calculate the orbital contribution of the V atom to the E_{MCA} , as shown in Fig. S6 (ESI[†]). For V-d orbitals, the in-plane E_{MCA} is mainly contributed by hybridization of $d_{xy}/d_{x^2-y^2}$, d_{z^2}/d_{yz} , and d_{z^2}/d_{xz} . However, the E_{MCA} contribution of the V atom in the V-p orbital is one order of magnitude greater than that in the V-d orbital. Therefore, the in-plane E_{MAE} mainly originates from the hybridization of the p-orbitals. The Curie temperature (T_c) of the SVSiN₂ monolayer is estimated on the basis of the Heisenberg model:

$$H = - \sum_{\langle ij \rangle} J_{ij} S_i \cdot S_j - D(S_i^z)^2 \quad (6)$$

where S_i is the spin operator ($S = 1/2$), J_{ij} is the strength of the exchange interaction between site i and j , and D is the single-ion anisotropy constant. Our DFT calculations extrapolate $J = 65.5$ meV and $D = 93.08$ μeV . We also perform MC simulations which predict a T_c of about 260 K, as shown in Fig. 3. The SVSiN₂ monolayer has a higher T_c than that of the CrX₃ (X = F, Cl, Br, I)

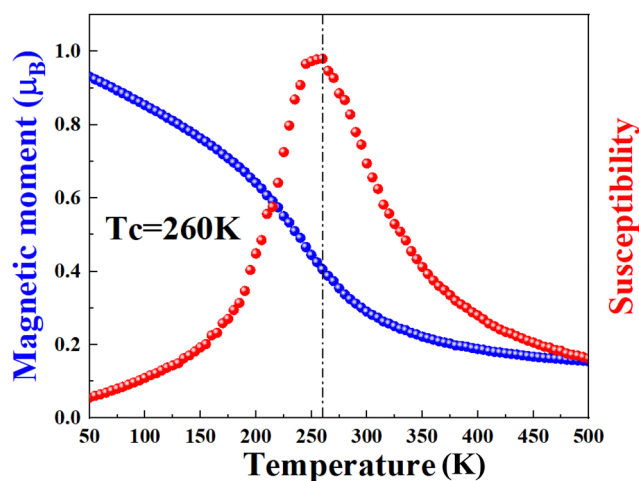


Fig. 3 The Curie temperature of the SVSiN₂ monolayer based on Monte Carlo simulations.

monolayer,⁶² which is desirable for the practical application of valleytronics.

3.3 Electronic structure

The band structure of the SVSiN₂ monolayer is shown in Fig. 4. When the SOC is not considered, the electronic bands are completely spin polarized, as shown in Fig. 4(a). The valence band maximum (VBM) and conduction band minimum (CBM) of the SVSiN₂ monolayer is located at the G and M point, respectively, leading to an indirect bandgap of about 0.53 eV. We define the valley splitting of the valence band Δ_{VB} (conduction band Δ_{CB}) as:

$$\Delta_{\text{VB}} = E_K^{\text{VB}} - E_{-K}^{\text{VB}} (\Delta_{\text{CB}} = E_K^{\text{CB}} - E_{-K}^{\text{CB}}) \quad (7)$$

where E_K^{VB} and E_{-K}^{VB} (E_K^{CB} and E_{-K}^{CB}) denote the energy extremum of the K ($-K$) valley valence and conduction band, respectively. It is found that the valley-dependent electronic states are fully spin polarized, *i.e.*, both the CBM and VBM at the $K/-K$ valleys have a contributing up-spin component. The valley polarization is protected by time-reversal symmetry, and the in-plane magnetization does not break such symmetry. Therefore, valley splittings for the valence band Δ_{VB} and for the conduction band Δ_{CB} are absent when the magnetization axis is along the $+x$ direction, as confirmed in Fig. 4(b). In contrast, the time-reversal symmetry is broken when the magnetization axis is along the out-of-plane direction, leading to a prominent Δ_{VB} of about -72.73 meV as shown in Fig. 4(c). The conduction band splitting is small and is predicted to be a mere 4.32 meV. When the magnetization direction is reversed to the $-z$ direction, the valley splitting of the Δ_{VB} (Δ_{CB}) is 72.73 (-4.32) meV, as presented in Fig. 4(d). Notably, the up-spin component at the $K/-K$ valleys is fully polarized when the magnetization direction is in the $+z$ direction, and the $-z$ magnetization direction will flip the full polarization to the down-spin component at the $K/-K$ valleys.²⁹ For the SVSiN₂ monolayer, the $+z$ ($-z$) directed magnetization selectively stimulates the hole carrier at the $-K$ (K)

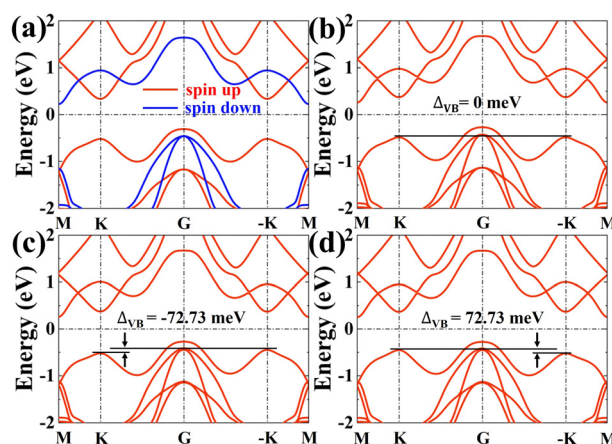


Fig. 4 (a) The band structure of the SVSiN₂ monolayer without SOC. (b)–(d) The band structure of the SVSiN₂ monolayer with SOC, where (b)–(d) represent the magnetic moment of V ions in the $+x$, $+z$, and $-z$ directions, respectively.

(*K*) valley-coupled with up (down) spin polarization, as shown in Fig. 4(c) and (d), respectively. As a consequence, both spin and valley are locked with the magnetization direction. This phenomenon is also observed in the RuClBr monolayer.⁶³ It provides the possibility to switch opposite spin polarizations at the *K*–*K* valleys by intentionally manipulating the magnetization direction of the SVSiN₂ monolayer. Similar valley polarization phenomena are also obtained in the MoSi₂N₄/CrI₃ and MoTe₂/MnSe₂ heterostructures resulting from the magnetic proximity effect.^{64,65} Moreover, such spin polarization at the *K*–*K* valleys is completely different from the spin-valley locking in the MoS₂ monolayer, where the *K*–*K* valleys are simultaneously coupled with up/down spins, respectively.⁶⁶

To further examine the characteristics of valley splitting in the SVSiN₂ monolayer, we derive a simple model to describe the intensity of valley splitting for the SVSiN₂ monolayer:⁶⁷

$$\begin{aligned}\hat{H}_{\text{soc}} &= \alpha \hat{L} \cdot \hat{S} \\ &= \lambda \left(\hat{L}_z \cos \theta + \frac{1}{2} \hat{L}_+ e^{-i\phi} \sin \theta + \frac{1}{2} \hat{L}_- e^{+i\phi} \sin \theta \right)\end{aligned}\quad (8)$$

where λ is the coupling strength of the SOC. Based on Fig. 4(a), we find that both valence band and conduction band at the *K*–*K* valley are contributed by the spin-up electronic states. Therefore, this model only considers interactions between the same spin states. According to Fig. 5(a), the valence band valley of the *K*–*K* point is mainly contributed by the $d_{xy}/d_{x^2-y^2}$, and the conduction band valley is governed by d_{z^2} . Therefore, the basis function of the valence band valley (conduction band valley) can be described as:

$$|\psi_v^{\pm}\rangle = \frac{1}{\sqrt{2}}(|d_{x^2-y^2}\rangle + i\tau|d_{xy}\rangle) \quad (|\psi_c\rangle = |d_{z^2}\rangle) \quad (9)$$

where τ is the valley index and equals 1 (–1) at the *K* (–*K*) valley. Hence, when the magnetization direction is parallel to the *z*-axis, the matrix elements of the SOC operator $\hat{L} \cdot \hat{S}$ are based on d-orbitals.⁶⁸ The valence band (conduction band) valley splitting can be expressed as:

$$\Delta_{\text{CB}} = \langle d_{z^2} | \hat{H}_{\text{soc}} | d_{z^2} \rangle - \langle d_{z^2} | \hat{H}_{\text{soc}} | d_{z^2} \rangle = 0 \quad (10)$$

$$\begin{aligned}\Delta_{\text{VB}} &= \langle \psi_v^1 | \hat{H}_{\text{soc}} | \psi_v^1 \rangle - \langle \psi_v^{-1} | \hat{H}_{\text{soc}} | \psi_v^{-1} \rangle \\ &= i \langle d_{xy} | \lambda \hat{L}_z | d_{x^2-y^2} \rangle - i \langle d_{x^2-y^2} | \lambda \hat{L}_z | d_{xy} \rangle = 4\lambda\end{aligned}\quad (11)$$

When the magnetization direction is parallel to the *x*-axis, $\hat{H}_{\text{soc}} = \lambda \hat{L}_x$, the valley of the valence band (conduction band) splits into $\Delta_{\text{CB}} = \Delta_{\text{VB}} = \langle \psi_v^1 | \lambda \hat{L}_x | \psi_v^1 \rangle - \langle \psi_v^{-1} | \lambda \hat{L}_x | \psi_v^{-1} \rangle = 0$. The above analyses are consistent with our valley splitting results obtained from first principles calculations. The significant differences between valence band valley splitting and conduction band valley splitting are attributed to different basis functions determined by different orbital contributions of different *K*–*K* valleys.

For 2D hexagonal lattices, there may be anomalous Hall effects in the FVS materials without the assistance of a magnetic field. In the following, we will study the valley-related transport properties of the SVSiN₂ monolayer. The transport properties related to valleys are closely related to the Berry curvature. For a 2D system, the Berry curvature can be expressed as:

$$\Omega_z(k) = - \sum_n \sum_{n' \neq n} f_n \frac{2\text{Im} \langle \psi_{nk} | v_x | \psi_{n'k} \rangle \langle \psi_{n'k} | v_y | \psi_{nk} \rangle}{(E_n - E_{n'})^2} \quad (12)$$

where f_n is the equilibrium Fermi Dirac distribution function. ψ_{nk} and E_n is the Bloch wave function and its eigenvalues, respectively. v_x and v_y are the velocity operators along different

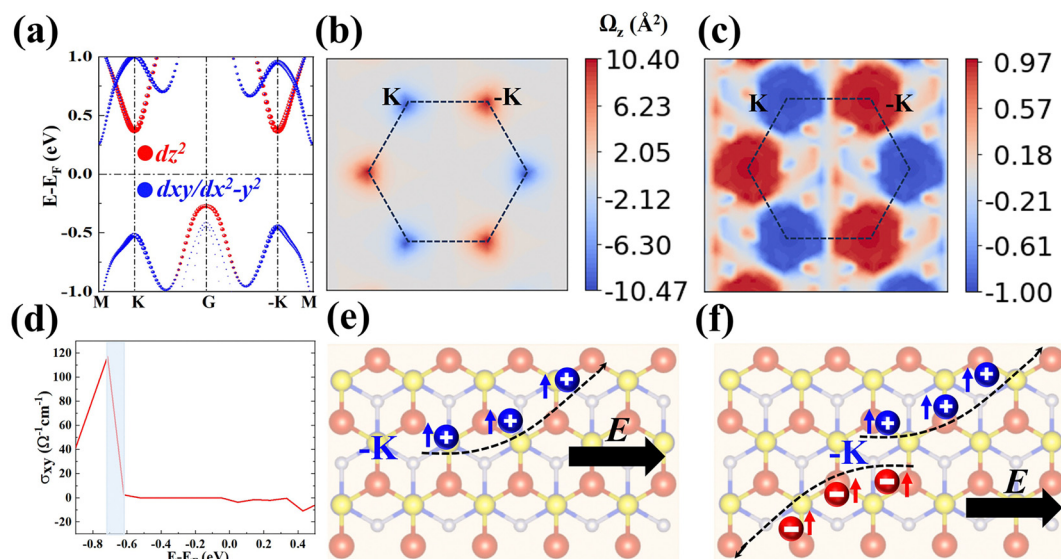


Fig. 5 The (a) orbital resolved electronic structure, (b) Berry curvature, (c) circular polarization, and (d) anomalous Hall conductivity of the SVSiN₂ monolayer. The Fermi level (E_F) is set to zero. (e) Schematic diagram of anomalous valley Hall effect under hole doping, with a V ion magnetic moment direction of +*z*. The blue arrow indicates the spin up state. (f) Schematic diagram of the anomalous valley Hall effect under specific frequency of right-handed circularly polarized light. Blue and red spheres represent hole and electron, respectively.

directions.^{69,70} Here, the Berry curvature is obtained by summing all occupied states. Fig. S7 (ESI†) shows that the band structure based on the tight-binding model is consistent with the DFT results. From Fig. 5(b), it can be seen that the Berry curvature at the K and $-K$ valleys has opposite signs and different absolute values. Since the anomalous velocity $v \propto -\vec{E} \times \vec{\Omega}_z$, the non-zero and opposite Berry curvatures indicate that the SVSiN₂ monolayer exhibit opposite anomalous velocities at the $K/-K$ valleys. In contrast, the Berry curvature is close to zero at other positions in the momentum space. The anomalous Hall conductivity σ_{xy} can be calculated by integrating the Berry curvature over the whole occupied states:⁷¹

$$\sigma_{xy} = \frac{e^2}{h} \frac{1}{2\pi} \int_{\text{BZ}} d\mathbf{k}^2 \Omega(\mathbf{k}).$$

As shown in Fig. 5(d), the presence of AVHE is confirmed by the non-zero σ_{xy} highlighted by the shaded area. Furthermore, we have proposed a theoretical design to achieve AVHE, as shown in Fig. 5(e). Owing to the remarkable valley splitting of VBM at the $K/-K$ valleys, we can modulate the E_F to achieve hole doping at the desired valley, e.g., the $-K$ valley shown in Fig. 4(c).

In addition, the non-zero berry curvature indicates that the $K/-K$ valley has chirality, in which the circularly polarized light selection rule can be described as:

$$\eta(\mathbf{k}) = \frac{|P_+(\mathbf{k})|^2 - |P_-(\mathbf{k})|^2}{|P_+(\mathbf{k})|^2 + |P_-(\mathbf{k})|^2} \quad (13)$$

where $P_{\pm}(k)$ represents the interband transition matrix.⁷² As shown in Fig. 5(c), the left-handed (right-handed) circularly polarized light is related to the K ($-K$) valley.

Using a specific frequency of right circularly polarized light, an electron-hole pair with the same spin can be generated at the $-K$ valley, and the electron (hole) will accumulate at the top

(bottom) of the sample, as shown in Fig. 5(f). The valley-contrasting transport properties are similar to those in the MoS₂ monolayer.⁶⁶

3.4 Strain effects and topological phase transition

The exchange interaction in the SVSiN₂ monolayer is related to the overlap of orbital wave functions between ions. Therefore, the distance between magnetic ions or the distance (bond angle) between magnetic ions and ligand atoms, has a substantial impact on the electronic properties of the SVSiN₂ monolayer. Strain engineering has been widely used to modulate the electronic structure of 2D materials. One of the main advantages of 2D materials is that their tensile properties are much higher than their bulk counterparts.⁷³ Therefore, we examine the effect of biaxial strain within $\pm 3\%$ on the electronic structure of the SVSiN₂ monolayer. Here, the biaxial strain is simulated by changing the lattice constant of the crystal cell and can be defined as:

$$\varepsilon = \left(\frac{a - a_0}{a_0} \right) \times 100\% \quad (14)$$

where a_0 and a represents the lattice constants of the SVSiN₂ monolayer without and with biaxial strain, respectively. As shown in Fig. 6(a) and Fig. S8 (ESI†), both in-plane tensile and compressive strains tend to reduce the bandgap of the SVSiN₂ monolayer and maintain the characteristics of an indirect bandgap. Compared to the pristine SVSiN₂ monolayer, the CBM of the SVSiN₂ monolayer is shifted from the M -point to the $K/-K$ valley when an in-plane tensile strain is applied. Moreover, biaxial strains could tune the valley splitting of the SVSiN₂ monolayer, as shown in Fig. 6(d). It is found that when the strain is increased from -3% to 3% , the valley splitting of the valence band is linearly enhanced. We further plot the orbital resolved band structures of the SVSiN₂ monolayer under -3% and 3% biaxial strains, as shown in Fig. S9



Fig. 6 (a) The bandgap of the SVSiN₂ monolayer under different strains. The Berry curvature distributions of the SVSiN₂ monolayer under (b) -3% and (e) 3% strain. The circular polarization of the SVSiN₂ monolayer under (c) -3% and (f) 3% strain. (d) The valley splitting for the conduction band Δ_{CB} (left column and red color online) and valence band Δ_{VB} (right column and blue color online) of the SVSiN₂ monolayer under different strains.



Fig. 7 The (a) band structure of the SVSiN₂ monolayer containing SOC under biaxial strain. The corresponding (b) orbital-resolved band structure and (c) edge state of the SVSiN₂ monolayer under biaxial strain.

(ESI[†]); the features of its conduction band at the $K/-K$ valleys dominated by the d_{z^2} orbital, remains as the biaxial strain ranges from -3 to 3% . According to eqn (11), the valley splitting of the valence band remains a small value.

The in-plane biaxial strains give rise to the prominent influence on the Berry curvature at the $K/-K$ valleys, as shown in Fig. 6(b) and (e). The variation of the Berry curvature at the $K/-K$ valleys is consistent with the trend of valley splitting of the valence band, *i.e.*, a tensile strain induces a greater Berry curvature difference at the $K/-K$ valleys. Furthermore, both the CBM and VBM at the $K/-K$ valleys are shifted towards the E_F when a tensile strain is applied, as shown in Fig. S9 (ESI[†]). It is

expected that the bandgap at the $K/-K$ valleys could be closed when a sufficiently large strain is performed on the SVSiN₂ monolayer. Most importantly, the bandgap closure generally implies the presence of a strain-driven topological transition associated with a nontrivial electronic state.⁷⁴ We therefore calculate the orbital-resolved electronic structure and edge states of the SVSiN₂ monolayer under 5.3 – 6.2% biaxial strain.

It can be seen from Fig. 7(a) and (b) that the SVSiN₂ monolayer is a valley-half-semiconductor (VHSC) when $\varepsilon < 5.5\%$. In contrast, the bandgap of the SVSiN₂ monolayer at the $-K$ valley is essentially closed when a strain of $\varepsilon = 5.5\%$ is applied. Moreover, the VBM at the $-K$ valley is contributed by the d_{z^2} orbital of the V atom, revealing the presence of strain-driven band inversion. Therefore, a valley-half-semimetal (VHSM) state is obtained under $\varepsilon = 5.5\%$. When the tensile strain is continuously increased, the bandgap at the $-K$ valley reopens and the SVSiN₂ monolayer enters the valley quantum anomalous Hall (VQAH) state. When $\varepsilon = 6\%$, the bandgap of the SVSiN₂ monolayer at the K valley is closed, and a similar band inversion for the CBM is clearly observed at the K valley. Similar strain induced valley-dependent band inversion was also observed in the VSIN₄ monolayer and Janus VSIGeN₄ monolayer.^{34,41,58} The band inversion is a strong implication of the nontrivial topological phase.^{40,74} The bandgap at the K valley reopens and the SVSiN₂ monolayer becomes VHSC when $\varepsilon > 6\%$.

To understand the mechanism of multiple topological phase transitions, we analyzed the orbital projection band structure and edge states, as shown in Fig. 7(c). Under a tensile strain of 5.7% , it is found that an edge state crosses the Fermi level, and it connects the VBM at the K valley and the CBM at the $-K$ valley. The strain induced edge state in the SVSiN₂ monolayer is very similar to the case of the strained (4.5 – 4.8%) VSICN₄



Fig. 8 (a) The bandgap of the SVSiN₂ monolayer under a vertical electric field. Berry curvature distributions of the SVSiN₂ monolayer under (b) $-0.3 \text{ V } \text{\AA}^{-1}$ and (e) $0.3 \text{ V } \text{\AA}^{-1}$ vertical electric fields. The circular polarization of the SVSiN₂ monolayer under (c) $-0.3 \text{ V } \text{\AA}^{-1}$ and (f) $0.3 \text{ V } \text{\AA}^{-1}$ vertical electric fields. (d) The valley splitting for the conduction band and valence band of the SVSiN₂ monolayer under different vertical electric fields.

monolayer.⁴¹ The topologically nontrivial phase is characterized by the nonzero topology invariant. The Chern number $\mathbb{C}$ is obtained by integrating the Berry curvature in the first Brillouin zone, and the calculated $\mathbb{C}$ in the strain range 5.5–6% is -1 . The nonzero topology invariant shows that the 5.5–6.0% strained SVSiN₂ monolayer possesses nonzero intrinsic quantum anomalous Hall conductivity σ_{xy} according to:⁷⁴

$$\sigma_{xy} = -\mathbb{C}G_0 \quad (15)$$

where $G_0 = \frac{e^2}{h}$ is the quantum conductance. The VQAH is predicated to be achieved in the SVSiN₂ monolayer using a 6% in-plane tensile strain. The SVSiN₂ monolayer provides a new platform to explore valley-contrasting properties and strain-driven topological state transitions.

3.5 Effects of external electric field

In addition, we explore the effects of external electric field on the valleytronics properties of the SVSiN₂ monolayer, as shown in Fig. 8. The bandgap of the SVSiN₂ monolayer exhibits a decreasing trend in the range from negative electric field to positive electric field. Compared to the strain modulation, the vertical electric field gives rise to negligible influence on the bandgap variation, as confirmed in Fig. 8(a). Fig. S10 (ESI[†]) demonstrates that their band structures are almost unaffected by the electric field. The valleytronic properties of the SVSiN₂ monolayer are robust to the vertical electric fields. Therefore, the vertical electric field has a weak impact on the valley splitting and Berry curvature, as verified in Fig. 8(b)–(f). The different tuning behavior of biaxial strains and vertical electric fields on the SVSiN₂ monolayer enrich the understanding of its valley-dependent properties, and are helpful to the development of FVS devices.

4 Conclusions

Based on first-principles calculations, we have demonstrated that the SVSiN₂ monolayer is a promising FVS material. Our calculation results indicate that: (1) the SVSiN₂ monolayer is a 2D XY magnetic material with a Curie temperature of 260 K, and its in-plane magnetic anisotropy energy mainly originates from the hybridization of the p-orbitals, exhibiting excellent thermal and dynamical stability. (2) A giant valley polarization of -72.73 meV and opposite Berry curvatures can be achieved in the SVSiN₂ monolayer by shifting the magnetization from the in-plane to out-of-plane direction, leading to an anomalous valley Hall effect. (3) The valley-contrasting properties of the SVSiN₂ monolayer can be significantly tuned by in-plane biaxial strains. Specifically, the 5.5–6.0% strain driven topological phase transition is confirmed by the band inversion and nontrivial edge state. The calculated nonzero Chern number demonstrates that the strained SVSiN₂ monolayer possesses nonzero intrinsic quantum anomalous Hall conductivity to realize the valley polarized quantum anomalous Hall effect. (4) Compared to the in-plane strain modulation, the valley-related property of the SVSiN₂ monolayer is rather robust to the

vertical electric fields. Overall, our research has broadened the scope of 2D FVS materials, which is beneficial for practical applications of the SVSiN₂ monolayer for valleytronic devices.

Conflicts of interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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