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# Solvation of cationic copper clusters in molecular hydrogen†

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Multiply charged superfluid helium nanodroplets are utilized to facilitate the growth of cationic copper clusters ( $\text{Cu}_n^+$ , where  $n = 1-8$ ) that are subsequently solvated with up to 50  $\text{H}_2$  molecules. Production of both pristine and protonated cationic Cu clusters are detected mass spectrometrically. A joint effort between experiment and theory allows us to understand the nature of the interactions determining the bonding between pristine and protonated  $\text{Cu}^+$  and  $\text{Cu}_2^+$  cations and molecular hydrogen. The analysis reveals that in all investigated cationic clusters, the primary solvation shell predominantly exhibits a covalent bonding character, which gradually decreases in strength, while for the subsequent shells an exclusive non-covalent behaviour is found. Interestingly, the calculated evaporation energies associated with the first solvation shell markedly surpass thermal values, positioning them within the desirable range for hydrogen storage applications. This comprehensive study not only provides insights into the solvation of pristine and protonated cationic Cu clusters but also sheds light on their unique bonding properties.

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## Introduction

Hydrogen is the most abundant and lightest chemical element in the universe. However, due to its high reactivity, it exists, under ambient conditions on Earth, only as a diatomic molecule or bound to other elements forming compounds such as water.<sup>1</sup> Nowadays, there is an increasing hydrogen demand, since it is an important chemical species for energy storage, catalysis, metallurgy *etc.* Therefore, great efforts are being made in order to understand the interaction of hydrogen with other elements and molecules.

Copper, on the other side, has proven to be a very robust catalyst for the synthesis of alcohols, hydrocarbons<sup>2-4</sup> and an interesting candidate for hydrogen storage.<sup>5-9</sup> In all these processes understanding the interaction between Cu and  $\text{H}_2$  is highly important.

The first attempts were made already in the early 80s and became a computational benchmark for molecule-surface reactions.<sup>10-12</sup> Ever since, the continuous development of

experimental and computational methods led to a good understanding of the reaction between  $\text{H}_2$  and Cu surfaces with different crystalline structures.<sup>13-16</sup> The dissociation behavior of  $\text{H}_2$  has been summarized in theoretical studies.<sup>17,18</sup> Moreover, it has been shown that the reactivity decreases from  $\text{Cu}(211) > \text{Cu}(111) > \text{Cu}(100) > \text{Cu}(110)$ , with the last one being rather inert.<sup>19-21</sup> All types of defects on the surface decrease the  $\text{H}_2$  dissociation barrier. Involved defects were modelled with gas-phase Cu clusters to reduce the complexity of the system and to focus on the reaction between Cu and  $\text{H}_2$ .

However, the size of clusters can significantly impact their physical and chemical properties, such as the height of the dissociation barrier of the molecules attached to this cluster. Research on Ag clusters demonstrated that the size of deposited clusters is even more important for its catalytic activity than the underlying support material.<sup>22</sup>  $\text{H}_2$  binds also more strongly to the clusters than to the surfaces, and it was recently shown that  $\text{H}_2$  takes more charge from  $\text{Cu}_{13}$  than from a  $\text{Cu}(111)$  surface.<sup>13</sup>

The reaction of neutral Cu clusters with  $\text{H}_2$  has been studied mainly theoretically.<sup>23-32</sup> It was found that the chemisorption of hydrogen on clusters more likely happens on acute metal sites, in contrast to surfaces where it usually binds to hollow sites.<sup>27</sup> The adsorption of the first  $\text{H}_2$  molecule, in general, leads to the reduction of the Cu-Cu distance and elongation of the H-H bond lengths.<sup>26</sup> Moreover, the chemisorption energy of the first hydrogen atom exhibits strong cluster size-dependent even-odd oscillations, favoring the clusters with an even number of Cu atoms.<sup>33</sup> Experimentally, the reaction

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probability of  $D_2$  with Cu clusters was measured at single-collision-like conditions. In that study, it was concluded that the reactivity of Cu is so low, that it is below the detection limit.<sup>34</sup>

In contrast, Cu cations have attracted more attention among experimentalists, supported by theoretical investigations.<sup>35–39</sup> Among other transition metal ions, the reaction product of  $Cu^+$  with  $H_2$  has been extensively studied with IR spectroscopy.<sup>40</sup> Dissociation energies for the detachment of up to four  $H_2$  molecules, forming the first solvation shell, from  $Cu^+$  (0.67, 0.72, 0.38 and 0.22 eV) and from the electronically excited  $Cu^{*+}$  (0.18, 0.11 and 0.06 eV, first three ligands) have been obtained using equilibrium methods.<sup>36</sup> Similar energies were determined for  $Cu_2^+$  (0.54, 0.44, 0.21, 0.16, 0.09 and  $\sim 0.07$  eV).<sup>37</sup> Recently, bigger cationic clusters consisting of  $n = 4$  up to 7 Cu atoms have been also investigated using IR-spectroscopy, showing that clusters with  $n = 5$  have a tendency for dissociative adsorption of  $H_2$ , while other cluster sizes exhibit mainly molecular adsorption.<sup>41</sup> It has been found that not more than six  $H_2$  ligands could be strongly attached to the cation.<sup>37,41</sup>

Previously, multiple solvation layers of hydrogen molecules surrounding  $H^-$ <sup>42</sup> and  $H_3^+$ <sup>43</sup> were studied by electron impact of neutral superfluid He nanodroplets (HNDs) heavily doped with  $H_2$ , as well as the solvation of cationic impurities such as fullerenes<sup>44</sup> and  $Cs^+$ <sup>45,46</sup> by  $H_2$ . In the present investigation, by utilizing multiply charged superfluid He nanodroplets (mc-HNDs) we were able to grow  $Cu_n^+$  ( $n = 1–8$ ) solvated with up to 50  $H_2$  molecules, which became possible due to the ultracold environment of the host droplet. A similar method was also recently used to study solvation of  $Na^+$ .<sup>47</sup> One of the main novelties of this work is that both pristine and protonated cationic Cu clusters are produced. Here we present a joint effort between experiment and theory in order to understand the nature of the interaction determining the bonding in the complexes containing  $Cu^+$  and  $Cu_2^+$  cations and molecular hydrogen. These ionic complexes formed in mc-HNDs are studied by mass spectrometry and their structure and energy are evaluated by means of high-level *ab initio* electronic structure, classical optimization evolutionary algorithm (EA) and diffusion Monte Carlo (DMC) calculations. Further, we also present the experimental results on the solvation of  $Cu_n^+$  ( $n = 3–8$ ) with  $H_2$  and collision-induced dissociation (CID) studies of selected complexes.

Obtained results are of relevance from both an applied (hydrogen storage and release) and a fundamental point of view. Particular attention is addressed to the gradual transition between a prevalent covalent bonding, which governs the energy and structure of the first solvation shell, found for both Cu monomer and dimer cations, to that of an exclusive non-covalent behavior which determines the intermolecular interaction within the following shells.

## Methods

### Experimental

The data described in the following were obtained by doping of positively charged HNDs, formed *via* supersonic expansion of

pre-cooled  $^4He$  gas (99.9998%, Messer) at a temperature of 9 K and a stagnation pressure of 25 bar through a 5  $\mu m$  pinhole nozzle (Plano GmbH, A0200P). Right after passing a skimmer into the quadrupole chamber (QUAD) the HNDs are ionized with electron impact (current 350  $\mu A$  and energy 60 eV). The resulting mc-HNDs have a size of approximately  $10^6$  He atoms and an internal temperature of  $\sim 0.4$  K carrying about 10 charges.<sup>48</sup> The  $Cu_n^+$  clusters are formed by evaporation of monoisotopic  $^{63}Cu$  pellets (99,9% isotopic purity) in the sublimation source (125 W,  $\sim 1020$  K measured on the outside surface of the oven) and sequential pick up of Cu atoms into mc-HNDs, where they agglomerate around the charge centers.<sup>49</sup> A more detailed description of the instrumentation and cluster formation can be found elsewhere.<sup>50,51</sup>

The  $Cu_n^+$  ( $n = 1–8$ ) doped HNDs are guided by an RF-hexapole (EVAP) filled with  $H_2$  gas, as it was also done previously for alkali cations.<sup>47</sup> In the EVAP chamber He from the HNDs evaporates due to the high number of collisions with room temperature  $H_2$  (99.999%, Messer). Additionally, the Cu clusters react with  $H_2$  and exothermic processes also lead to He evaporation from the HND. However, too many collisions also lead to the evaporation of  $H_2$  units from the  $H_mCu_n^+$  complexes, as a consequence less  $H_2$  remains bound to the copper cluster ions. Therefore, the  $H_2$  pressure in the EVAP chamber is critical for the amount of  $H_2$  remaining attached to the copper cluster ions. Here, we will discuss only experiments performed at a pressure of  $1.8 \times 10^{-3}$  mbar, since this pressure regime allows to resolve the behavior of the complexes with less than 15  $H_2$  molecules attached to  $Cu_n^+$ . This range is of special interest in this study, since it allows the comparison with computational results. The resulting hydrogen-solvated copper cluster ions were analyzed and detected with a time-of-flight mass spectrometer (TOF-MS) to obtain the ion yield of  $H_mCu_n^+/(H_2)_kCu_n^+$  complexes as a function of the number of  $H_2$  molecules,  $k$ , (or H atoms,  $m$ ) bound to a specific copper cluster cation  $Cu_n^+$ . However, also a measurement at  $1.5 \times 10^{-3}$  mbar is performed to verify that intensity anomalies are independent of hydrogen pressure in the evaporation cell. The resulting mass spectra are illustrated in Fig. 1. Comparing those spectra, one could notice that as the hydrogen pressure in the evaporation cell decreases, the number of attached  $H_2$  increases. To facilitate the data analysis the mass spectra were analyzed with the in-house software IsotopFit.<sup>52</sup>

Additionally, protonated  $Cu_n^+$  are studied during the same measurement.  $HCu_n^+$  core ions are produced *via* proton transfer from  $H_3^+$ . The backflow of  $H_2$  from the EVAP chamber to the QUAD chamber results in the formation of  $H_3^+$  ions in the mc-HND prior to copper pickup, which transfer a proton to the first arriving copper atom.<sup>50</sup> Therefore, the solvation of  $Cu_n^+$  and  $HCu_n^+$  in  $H_2$  can be studied simultaneously. The ion intensity distributions of  $H_mCu_n^+$  ions are extracted from the mass spectra in Fig. 1 and are plotted as a function of the attached H atoms  $m$  for clusters containing up to  $n = 8$  copper atoms in Fig. S1 in ESI,<sup>†</sup> for both studied pressures. Note that all figures and tables started with S, can be found in ESI.<sup>†</sup>

To verify that both  $Cu_n^+$  and  $HCu_n^+$  are formed during protonation, additional mass spectra were recorded. In this





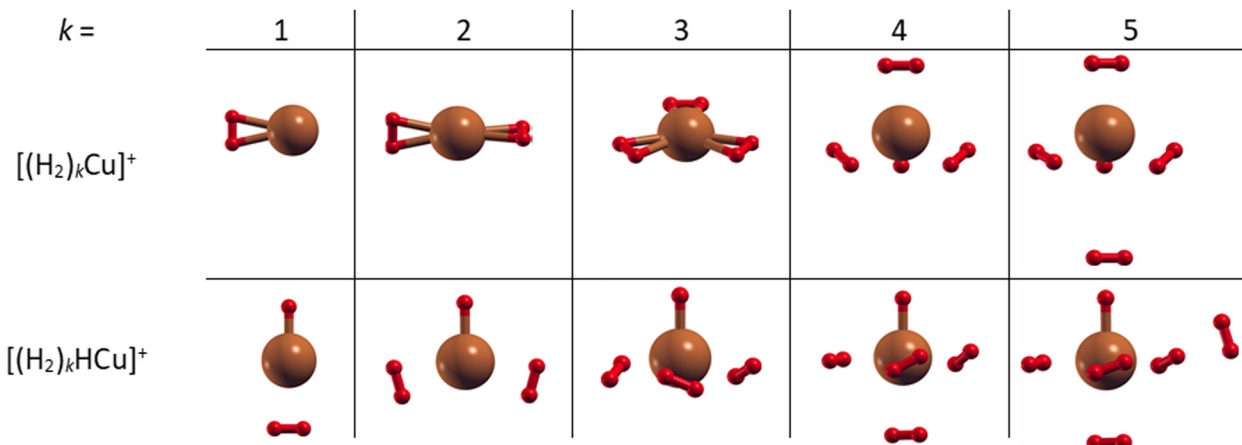


Fig. 2 Global minima structures as obtained by means of geometry optimizations at the CCSD/aug-cc-pVDZ level of theory for the  $(H_2)_kCu^+$  and  $(H_2)_kHCu^+$  ( $k = 1-5$ ) clusters. In both cases, up to four  $H_2$  molecules tend to gather around the Cu and HCu cores to form a first solvation shell. Notice that the Cu–H bonds depicted as solids are by convention those with an internuclear distance of less than 1.815 Å.

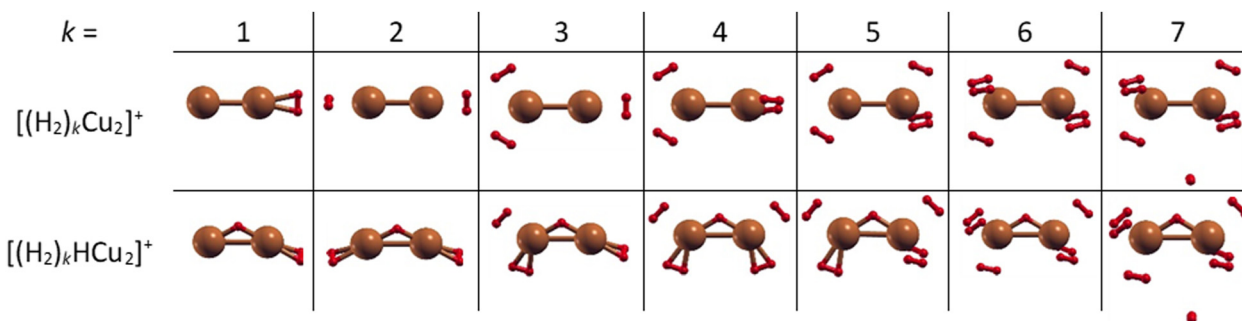


Fig. 3 Global minima structures as obtained by means of geometry optimizations at the CCSD/aug-cc-pVDZ level of theory for the  $(H_2)_kCu_2^+$  and  $(H_2)_kHCu_2^+$  ( $k = 1-7$ ) clusters. In both cases up to six  $H_2$  molecules tend to gather around the  $Cu_2$  and  $HCu_2$  cores. Notice that the Cu–H bonds depicted as solids are by convention those with an internuclear distance of less than 1.815 Å.

$(HCu_2)^+$  species the first solvation shell should include six  $H_2$  molecules as it will be discussed in the next section.

As for larger solvation shells, for the sake of simplicity, we have decided to focus only on the  $(H_2)_kCu^+$  aggregates, characterized by a closed shell character of the impurity, *i.e.*  $Cu^+$ , and being therefore more easily treatable by means of high level electronic structure calculations.

For such aggregates we have developed an analytical potential energy surface (PES) capable to correctly describe and represent the involved non-covalent interaction.

In particular, since as seen above for the most stable configuration of the  $(H_2)_5Cu^+$  aggregate the fifth  $H_2$  molecule is located farther from the Cu atom of about 1.5 Å (with respect to the inner  $H_2$  shell) and more loosely bound (see next section), we believe that it is a good approximation to obtain a PES which takes into account only for the interaction only between an external  $H_2$  molecule and the inner  $(H_2)_4Cu^+$  core, which has been considered as a rigid body. Such a PES has been built in a similar way to that recently reported for the  $(He_k-SF_6)^+$  and  $(He_k-SF_6)^+$  clusters.<sup>58</sup>

The structure of the  $(H_2)_4Cu^+$  cation has been optimized as explained above and it consists in a tetrahedral-like geometry

with the Cu atom in the center and four  $H_2$  molecules constituting the inner shell located around the metal and at about 1.83 Å from it.

Moreover, the related partial atomic charges obtained at the CCSD/aug-cc-pVTZ level of theory through the CM5 approach<sup>59</sup> have revealed that most of the cation positive charge is borne by the Cu atom while small (non negligible) charges can also be associated to the remaining H atoms.

As a following step, accurate *ab initio* estimations of the  $H_2-(H_2)_4Cu^+$  interaction potential were performed at the CCSD(T) level by considering both monomers as rigid bodies. In particular, the  $(H_2)_4Cu^+$  minimum geometry is that detailed above while the  $H_2$  internal distance  $|r|$  is fixed at its averaged value for the ground vibrational state  $r_0 = 0.766638$  Å.

A dense grid along the intermolecular coordinate  $R$  defining the distance between the external  $H_2$  unit and the Cu atom of the  $(H_2)_4Cu^+$  core, was probed for two selected approach configurations of the diatomic molecule along the main symmetry axis of the cation, as shown in Fig. 4. For both “bottom” and “top” approaches three different orientations (the main two perpendicular and one parallel) of the  $H_2$  molecules with





**Table 1** Optimized parameters for the van der Waals contribution ( $V_{vdw}$ ) to the  $H_2-[(H_2)_4Cu]^+$  PES (see eqn (3)–(5)). Parameters for the induction contribution (see eqn (6)) are indicated in the ESI.  $R_m$  are given in Å and  $\epsilon$ , in meV;  $\beta$  is dimensionless

Pair	$H_2[(H_2)_4Cu]^+$		
	$R_m$	$\epsilon$	$\beta$
$H_2-Cu$	3.822	4.98	6.1
$H_2-H$	3.250	2.11	6.1

about 44 meV at an intermolecular distance around 3.35 Å. Due to the tetrahedral-like symmetry of the inner cation three additional minima, having very similar interaction features as that found for the “bottom” approach, are indeed also expected, as we will see in the following.

In order to describe the energy and structure of the  $(H_2)_kCu^+$  (with  $k > 5$ ) clusters, the  $H_2-H_2$  interaction must be also taken into account and the latter is expressed as a sum of non-covalent plus electrostatic contributions, following the procedure indicated in the work by Kranabetter *et al.*<sup>46</sup>

As for three-body contributions to the total interaction energy, we have decided to neglect them for the  $(H_2)_kCu^+$  (with  $k > 4$ ) since the main term, that is the charge-induced dipole induced dipole contribution, provides very little corrections due to the larger distance of the outer  $H_2$  molecule from the central metal atom (bearing most of the cationic charge) with respect to those composing the first solvation shell.

## Results and discussion

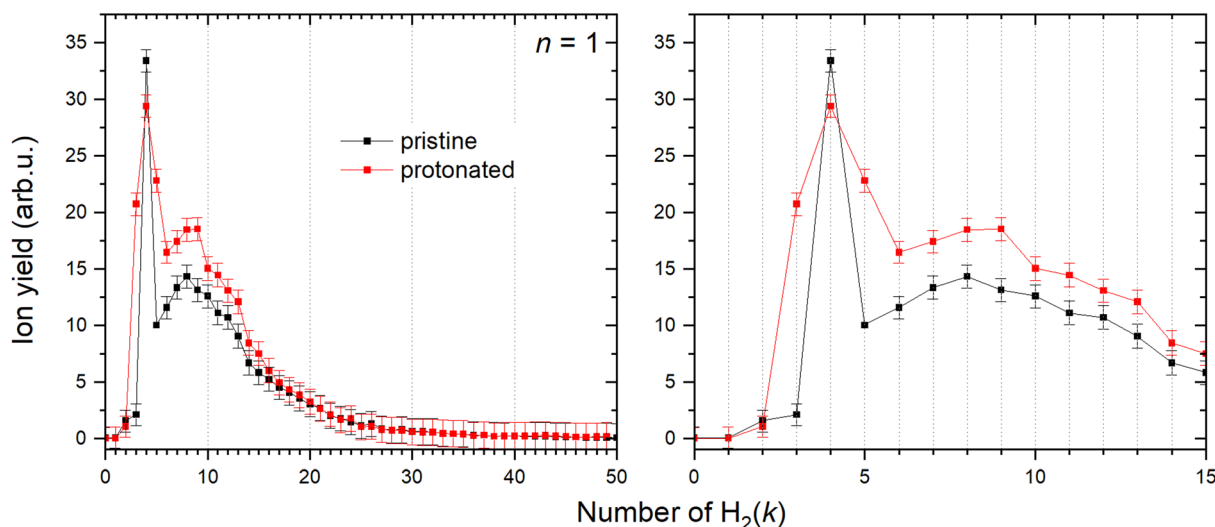
### $H_mCu^+$ clusters

It has been shown<sup>36</sup> that a copper cation forms with the first  $H_2$  molecule a bond with an evident partial chemical character. The interaction with the second  $H_2$  molecule is even stronger, and then the binding energy gradually decreases for the

attachment of additional molecules. However, the determination of the corresponding binding energies has been previously obtained only for the first six  $H_2$  attached to  $Cu^+$ .<sup>36</sup> Utilizing mc-HNDs we have managed to attach more than 50  $H_2$  molecules to  $Cu^+$ . In line with the previous findings, it becomes evident from Fig. 5 that the first stable configuration with abnormally high intensity involves the binding of two  $H_2$  molecules, a state we term “magic” henceforth. The next magic ion is formed by the attachment of four  $H_2$  molecules to  $Cu^+$ , providing the first solvation shell. The second solvation shell is formed by  $k = 8$ . When  $Cu^+$  is protonated forming the  $HCu^+$  core, also four  $H_2$  molecules are required to form the first solvation shell as shown in Fig. 5, followed by shell closures at  $k = 9$  and 13. The allocation of magic numbers adheres to the second difference method, expounded upon in our earlier publication.<sup>62</sup> Additionally, the magic-numbered ions generated by exploring other cluster sizes,  $n = 1-8$ , and  $k$  values below 15, are determined in a similar fashion and presented in Table 2.

It is known that some cluster sizes are able to dissociate  $H_2$ ,<sup>41</sup> however is very unlikely at the low temperature of the host helium droplet. The appearance in the mass spectrum of lines related to odd  $m$  can be thus rationalized by the formation of the  $HCu^+$  core, which is further solvated by  $H_2$ . This is in striking contrast to related experimental findings<sup>45,47</sup> for similar clusters formed in HND such as  $(H_2)_kNa^+$  and  $(H_2)_kCs^+$  for which the  $HNa^+$  and  $HCS^+$  species have been hardly detected due to their very low abundance, probably related to the non-chemical character of the alkali metal ion-hydrogen atom bond. Note that alkali ions are closed shell species, with empty orbital much higher in energy compared to those of a Cu ion. Therefore, their interactions with other partners are dominated by nearly pure electrostatic and polarization effects.

The experimental detection of both  $Cu^+$  and  $HCu^+$  ionic cores can be explained by the existence of two specific pathways. The first pathway would follow a charge transfer from the



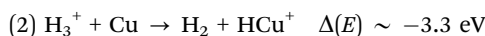
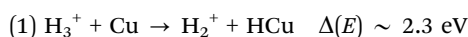
**Fig. 5** Left: Ion abundances of  $Cu^+$  (black) and  $HCu^+$  (red) solvated in the  $H_2$  with corresponding error bars extracted from the measured mass spectrum. Right: Zoom in on the complexes with first 15  $H_2$  molecules attached.



**Table 2** Putative magic numbers are listed for complexes formed with pristine and protonated clusters containing  $n = 1-8$  copper atoms. Please note that  $k$  represents number of  $H_2$  molecules bound to the cluster

$Cu_n^+, n$	Pristine, $k$	Protonated, $k$
1	2, 4, 8	4, 9, 13
2	6	2, 6, 8
3	4, 7, 9	4, 6, 11
4	4, 6, 11	5, 7
5	4, 7	5, 7
6	6	2, 6, 10, 12
7	4, 7	7
8	7, 12, 14	2, 8, 13

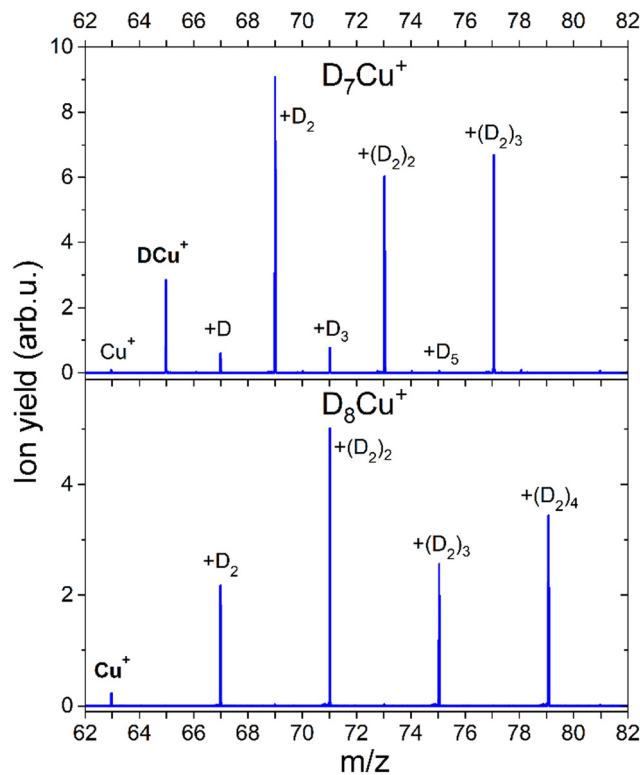
HND to Cu with a subsequent addition of molecular hydrogen. A second pathway would involve  $H_3^+$  as the first charge carrier and this species can further encounter Cu with the following outcomes,



It can be seen that the theoretical electronic energy difference  $\Delta(E)$ , obtained from reactants and products optimizations at the CCSD/aug-cc-pVTZ level of theory, clearly favors the second reaction channel promoted by  $H_3^+$ . Indeed, the optimized products' structure is shown in Fig. 2 and it is found that  $HCu^+$  is a chemical species, with a Cu–H bond length and a dissociation energy of about 1.47 Å and 3.0 eV, respectively.

The existence of a chemical bond in  $HCu^+$  is indeed a consequence of the electron configuration of the  $Cu^+$  cation whose ground state of a closed shell character reads as  $3d^{10}$ . However, for the first excited singlet state, with the  $4s^1 3d^9$  electron configuration and an open shell character, the formation of a covalent bond with a free H atom is energetically favorable. Moreover, such electron configurations with occupied 3d and unoccupied 4s and 4p orbitals are probably also responsible for the optimized geometries found for the  $(H_2)_k Cu_n^+$  and  $(H_2)_k HCu_n^+$  ( $n = 1-2$ ) clusters and which are discussed in the following.

The formation of a chemical  $HCu^+$  species has been further proven by CID measurements illustrated in Fig. 6 where results on deuterated complexes are reported to ensure a better selection of the parent peak: the  $D_m Cu^+$  clusters with  $m = 7$  and  $m = 8$  were separately selected and dissociated at the energy of 10 eV in the presence of Ar gas. For the  $m = 7$  complex, we mainly see the detachment of  $D_2$  units until  $DCu^+$  is formed, while for the  $m = 8$  aggregate the final product is  $Cu^+$ . Interestingly, CID of the complex with  $m = 7$  also shows very weak peaks at  $m = 0, 2, 4$  and 6 suggesting that there is a small probability that single D atoms can detach from the parent peak. Additional measurements were done for  $m = 7, 12, 13$  and 14 at 0, 1 and 10 eV and the corresponding mass spectra can be found in ESI,† Fig. S6. In all cases we see similar patterns, complexes with even  $m$  complexes showing exclusively the loss of  $D_2$ , while odd  $m$  precursor species exhibiting a preferential  $D_2$  loss but also low-intensity peaks for fragment ions corresponding to the



**Fig. 6** Mass spectra obtained with CID of  $D_7Cu^+$  and  $D_8Cu^+$  at 10 eV and Ar pressure of  $1 \times 10^{-5}$  mbar. The core ion is marked with the bold text. All further labels indicate how many D atoms are attached to the core ion.

detachment of single D atoms. From these additional measurements, it is also clear, that  $D_2$  molecules are weakly bound to the cluster, since they readily dissociate already with 1 eV of collision energy. The only difference between the mass spectra measured at collision energies of 1 and 10 eV is that for the precursors with  $m = 7, 13$  the intensity of the fragments with even  $m$  increases with the collision energy. The appearance of these peaks can be attributed to the neighboring masses “leaking” through the quadrupole filter. As a result, fragments unrelated to the parent ion can emerge in the mass spectrum. It could also originate from the presence of the  $H_2$  impurity, which mass equals to one D atom. This impurity might stem from the residual gas, as the pumping speed for hydrogen is very low. Additionally, there is a presence of 100 ppm  $H_2$  in the  $D_2$  cylinder, as indicated by the supplier. Another possibility is that a small fraction of  $(D_2)_k DCu_n^+$  complexes can emit D rather than  $D_2$ , which is energetically unlikely.

### Simulation results

In Fig. 7 the calculated average interaction energies  $E_{int}/k$  are reported as well as the evaporation energies  $\Delta E_{int}$  (defined as  $E_{int}^{k-1} - E_{int}^k$ ) related to the optimized global minima structures of the  $(H_2)_k Cu^+$  and  $(H_2)_k HCu^+$  ( $k = 1-5$ ) clusters given in Fig. 2. It can be noticed that for both species the calculated average interaction energies are higher (more negative) than  $-300$  meV and that the adsorption on the  $Cu^+$  cation is globally more favorable. Moreover, it is important to stress that the related



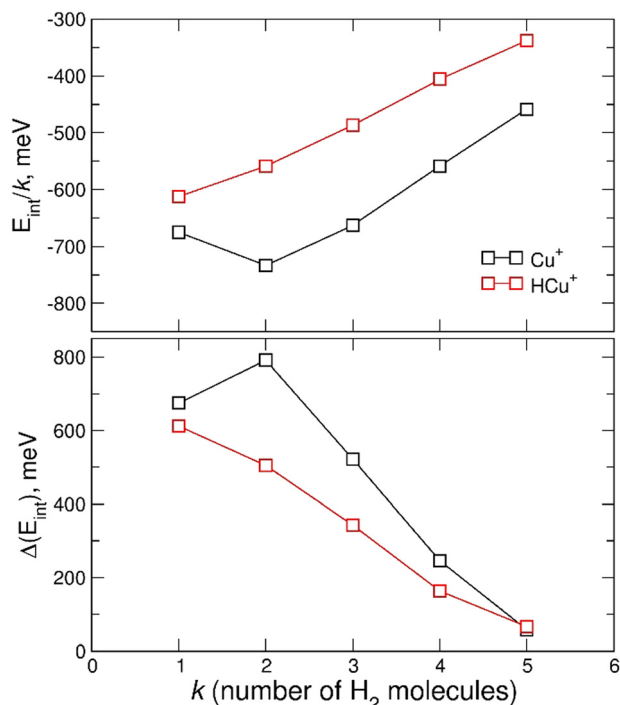


Fig. 7 Upper panel: average interaction energy  $E_{\text{int}}/k$  (in meV) obtained at the CCSD(T)/CBS level for the adsorption of  $k$  H<sub>2</sub> molecules around the Cu<sup>+</sup> and HCu<sup>+</sup> ions. Lower panel: as above but for the evaporation energy  $\Delta E_{\text{int}}$  (in meV).

evaporation energies are quite stronger than those previously predicted for the  $(\text{H}_2)_k\text{Cs}^+$ <sup>45</sup> and  $(\text{H}_2)_k\text{Na}^+$ <sup>47</sup> clusters for the same number ( $k < 5$ ) of adsorbed hydrogen molecules. Since for those clusters with alkali monocations the related interaction energy could be described exclusively in terms of non-covalent contributions, it is clear that in the case of the H<sub>2</sub> adsorption on Cu<sup>+</sup> and HCu<sup>+</sup> chemical contributions should play a role. Indeed, a similar behavior was previously found<sup>36</sup> for the  $(\text{H}_2)_k\text{Cu}^+$  ( $k = 1-4$ ) clusters with large experimental bond dissociation energies (0.67, 0.72, 0.38 and 0.22 eV for  $k = 1-4$ , respectively) which are in good agreement with present evaporation energies (0.68, 0.79, 0.52 and 0.25 eV for  $k = 1-4$ , respectively), which predict for  $k = 2$  a particularly stable configuration as already evidenced from the above discussion of the experimental data in Fig. 5. Such a behavior is a consequence of the electronic configuration of the involved Cu<sup>+</sup> and HCu<sup>+</sup> ions for which the occupied 3d and unoccupied 4s and 4p shells are available to participate in chemical bonding contributions involving the adsorbed H<sub>2</sub> molecules which can donate the electron charge from the occupied  $\sigma$  orbital.

While 3d and 4s orbital are close, the 4p orbitals are higher in energy with respect to 4s (about 5.5 eV). Since the involved interactions with H<sub>2</sub> exhibit a strength intermediate between that of canonical chemical and non-covalent cases, it has been suggested that, although the geometries for clusters with  $k = 2, 3, 4$  are close to those determined by sp, sp<sup>2</sup>, sp<sup>3</sup> hybridization of the central ion, it is more effectively controlled by a 3d4s hybridization. In particular, the associated electronic

rearrangement stimulates an electron transfer from the occupied  $\sigma$  molecular orbital of hydrogen molecule towards the empty atomic orbitals of central atomic ion which is accompanied by a 3d $\pi$ - $\sigma^*$  back-donation.<sup>36</sup> Both these stabilization effects decrease when  $k$  becomes larger than 2 and observed findings confirm that canonical hybridizations involving 4s and 4p orbitals, crucial to justify the behavior of complexes of Cu cation with molecules forming strong chemical bonds, here plays only a secondary role.

Further information can be also inferred from the optimized configurations shown in Fig. 2, where the geometries originated by the metal atom and centers of mass of the H<sub>2</sub> molecules seem to mimic those resulting from different hybridizations of the outer orbital shell of the metal. In fact,  $(\text{H}_2)_k\text{Cu}^+$  clusters with  $k = 1-2$  show a  $C_{2v}$  and  $D_{2d}$  symmetry, respectively, similar to that of a sp-like hybridization; for  $k = 3$  the Cu atom and the H<sub>2</sub> centers of mass lie on the same plane with a  $D_{3h}$  symmetry; for  $k = 4$  a quasi-tetrahedral structure seems to emerge.

On the contrary, for  $k = 5$ , when an additional H<sub>2</sub> molecule is added, the inner  $(\text{H}_2)_4\text{Cu}^+$  structure is practically unchanged while the extra molecule locates itself farther from the metal atom and the corresponding evaporation energy (see lower panel of Fig. 7) strongly reduces down to about 60 meV, that is in the same energy range previously observed for the adsorption on alkali ions, where typical non covalent interactions dominate.<sup>46,47</sup> Similar considerations also apply to the  $(\text{H}_2)_k\text{HCu}^+$  clusters whose structures show symmetries which could arise from different hybridization of the Cu<sup>+</sup> orbitals: in this case the pattern as a function of  $k$  is different (due the presence of a Cu-H chemical bond) and for  $k = 4$  a geometry similar to that for a dsp<sup>3</sup>-like hybridization of the metal can be also appreciated (see Fig. 2). An analysis of the related H<sub>2</sub> internuclear distances and partial atomic charges (obtained by means of the CM5 approach<sup>59</sup>) also evidences differences between the hydrogen molecules pertaining to the first and second shell. In fact, we have checked that for the  $k = 5$  cases the outer H<sub>2</sub> molecule is characterized by an internuclear distance that is shorter of about 0.02 Å; this is compatible with the associated positive partial atomic charges, whose value is around 0.016 a.u. and about 4 times smaller than those associated to the atoms of the innermost H<sub>2</sub> units, for which a more efficient charge exchange with the Cu ionic core is found.

Therefore, the results in Fig. 7 and Fig. S4 (ESI<sup>†</sup>), together with the above analysis, confirm that a first solvation shell composed of four H<sub>2</sub> molecules can be indeed clearly identified. Moreover, this first shell appears to be affected by chemical contributions to the bond in both  $(\text{H}_2)_k\text{Cu}^+$  and  $(\text{H}_2)_k\text{HCu}^+$  ( $k = 1-4$ ) clusters, as shown by the corresponding evaporation energies which largely exceed standard thermal values. Interestingly, even if evaporation energies are in general larger for  $(\text{H}_2)_k\text{Cu}^+$ , especially for  $k = 2$  and 3, in the case of  $k = 5$  we obtain almost coincident values in the range of 60 meV which are in good agreement again with the experimental estimation of ref. 36.







Fig. 8 Evaporation energies for (H<sub>2</sub>)<sub>k</sub>Cu<sup>+</sup> obtained by means of the classical EA (black squares) and DMC (red circles) approaches.

Based on the especially stable configuration seen in the *ab initio* calculations for (H<sub>2</sub>)<sub>4</sub>Cu<sup>+</sup> and following the discussion in the previous sections, we have employed the developed analytical PES to simulate the interaction (basically of non-covalent character) between this structure and the remaining H<sub>2</sub> units considered in a pseudoatom approximation. This interaction is provided by an ILJ expression shown in eqn (2)–(6) to obtain the evaporation energies for (H<sub>2</sub>)<sub>k</sub>Cu<sup>+</sup> with  $k > 4$  by means of a classical optimization EA and a quantum DMC approaches (see ESI,<sup>†</sup> for details). Results of our theoretical investigation are shown in Fig. 8. The feature found in the evaporation energies for  $k = 8$ , obtained both by means of the EA and the DMC calculations, suggests that the observed “magic” number in the experimental abundances (see Table 2 and Fig. 5) corresponds indeed to a stable configuration of the external molecular hydrogen which surrounds the (H<sub>2</sub>)<sub>4</sub>Cu<sup>+</sup> core. This also indicates that a second solvation shell begins at  $k = 5$  (as predicted in ref. 36) and probably closes at  $k = 8$ , which is an exclusive finding of present work.

As shown in Fig. 9, where we present the geometry found for (H<sub>2</sub>)<sub>8</sub>Cu<sup>+</sup> with the EA calculation employing the analytical PES, the extra four H<sub>2</sub> units (represented as grey spheres in Fig. 9) are located at approximately 3.4 Å from the Cu<sup>+</sup> along the axis which connects the center of mass of each inner H<sub>2</sub> molecule (in red in Fig. 9) with the metal.

### H<sub>m</sub>Cu<sub>2</sub><sup>+</sup> clusters

Contrary to Cu<sup>+</sup>, solvation of Cu<sub>2</sub><sup>+</sup> shows a very different trend depicted in Fig. 10. Both pristine and protonated clusters show the same “magic” number, for  $k = 6$ , and additionally HCu<sub>2</sub><sup>+</sup> seems to form a stable complex for  $k = 2$ .

In order to provide an explanation to the presence of the protonated species, an equivalent theoretical analysis as for Cu<sup>+</sup> (see previous section) has been carried out. A similar conclusion is evidenced with the formation of a very stable HCu<sub>2</sub><sup>+</sup> cation, whose optimized structure when interacting with one

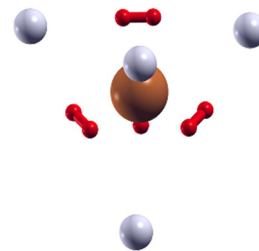


Fig. 9 Configuration obtained for the (H<sub>2</sub>)<sub>8</sub>Cu<sup>+</sup> cluster by means of the EA calculation using the ILJ potential of eqn (1)–(6) where a (H<sub>2</sub>)<sub>4</sub>Cu<sup>+</sup> rigid core is assumed and the other H<sub>2</sub> units (here shown as grey spheres) are considered under the pseudoatom approximation.

H<sub>2</sub> molecule is shown in Fig. 3. Indeed, for the HCu<sub>2</sub><sup>+</sup> cation the H atom places itself in between the Cu atoms in a triangular arrangement with a Cu–H bond length of about 1.58 Å and a dissociation electronic energy to form the Cu and HCu<sup>+</sup> (or Cu<sub>2</sub><sup>+</sup> and H) fragments of about 6.0 eV (3.3 eV) is found. Indeed, the ground state of Cu<sub>2</sub><sup>+</sup> is thought to exhibit the 3d<sup>20</sup>4σ<sup>1</sup> configuration, to which corresponds a <sup>2</sup>Σ<sub>g</sub> symmetry, and the semi occupied σ orbital can probably receive the electron borne by the H atom to form a covalent bond equally shared by both metal atoms.

CID measurements in Fig. 11 for Cu<sub>2</sub><sup>+</sup> were also performed to get the idea about the dissociation pattern of the most pronounced D<sub>m</sub>Cu<sub>2</sub><sup>+</sup> ( $m = 12, 13$ ) “magic” numbered ions, which correspond to the  $k = 6$  case for both pristine and protonated Cu<sub>2</sub><sup>+</sup> species. The dissociation pattern in both cases is similar to the one observed for complexes with Cu<sup>+</sup>, that is corresponding to the prevalent detachment of D<sub>2</sub> units. Interestingly, the complex with  $m = 12$ , shows some additional peaks (marked with an asterisk) which can be attributed to the D<sub>2</sub>O contamination. Also, for such a complex the loss of a single D atom, which could be a result of water splitting, can be appreciated. Complexes which are formed around the core containing several Cu atoms might not only loose D<sub>2</sub> but also the metal core might be fragmented if enough energy will be introduced to the system. The CID measurement of D<sub>5</sub>Cu<sub>2</sub><sup>+</sup> shown in the Fig. S7 (ESI<sup>†</sup>) illustrates the changes in the fragmentation pattern as function of energy from 10 to 60 eV. In general, the complex always tends to lose D<sub>2</sub> molecule, however at energy of 40 eV DCu<sup>+</sup> and Cu<sup>+</sup> fragments start to emerge from the noise level together with Cu<sub>2</sub>, whose signal is even lower. When 60 eV is applied it becomes clear that it is more likely to dissociate Cu from the complex rather than the last D atom attached to Cu<sub>2</sub><sup>+</sup>.

The calculated average interaction energies of the (H<sub>2</sub>)<sub>k</sub>Cu<sub>2</sub><sup>+</sup> and (H<sub>2</sub>)<sub>k</sub>HCu<sub>2</sub><sup>+</sup> ( $k = 1–7$ ) clusters are reported in Fig. 12. In this case the average interaction energies (see upper panel) are higher (more negative) than –250 meV with adsorption on the protonated cation being more favorable. The latter is probably due to the closed shell character of the HCu<sub>2</sub><sup>+</sup> which in general tends to increase the interaction with closed shell species such as H<sub>2</sub>; the same occurs also for the Cu<sup>+</sup> in Fig. 7 for which a similar trend is observed.



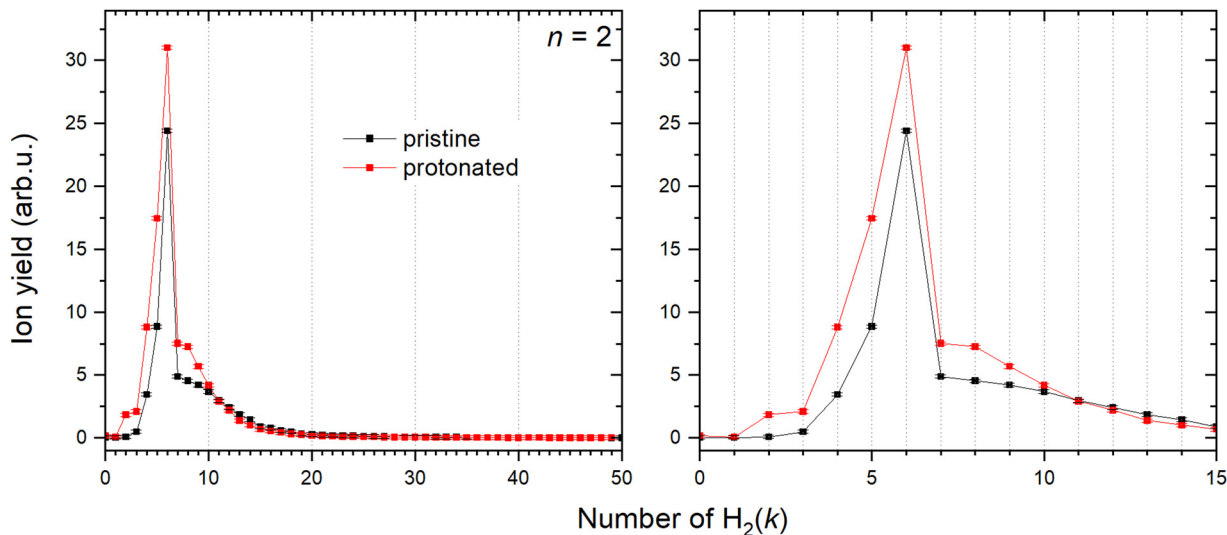


Fig. 10 Left: Ion abundances of  $\text{Cu}_2^+$  (black) and  $\text{HCu}_2^+$  (red) solvated in the  $\text{H}_2$  with corresponding error bars extracted from the measure mass spectrum. Right: Zoom in on the complexes with first 15  $\text{H}_2$  molecules attached.

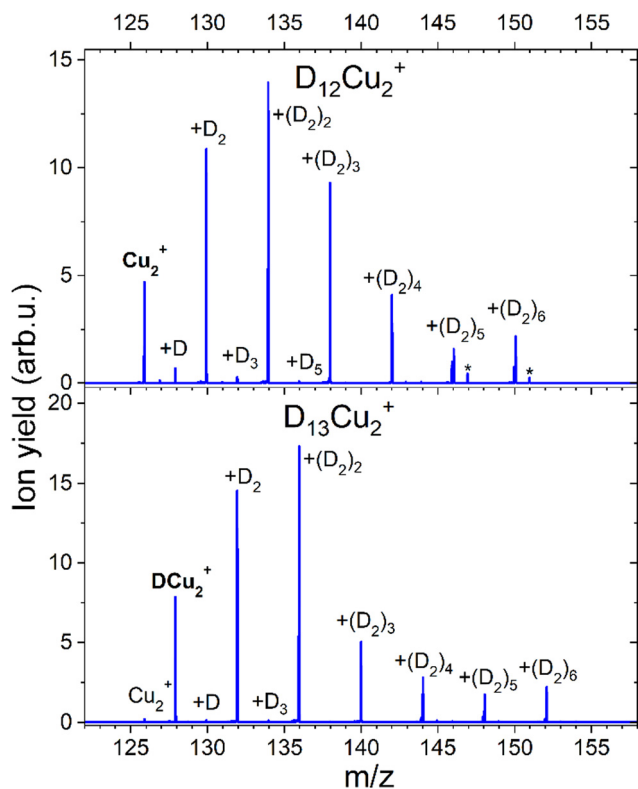


Fig. 11 Mass spectra obtained with CID of  $\text{D}_{12}\text{Cu}_2^+$  and  $\text{D}_{13}\text{Cu}_2^+$  at 10 eV and an Ar pressure of  $1 \times 10^{-5}$  mbar. The core ion is indicated with bold text. All further labels indicate how many D atoms are attached to the core ion. Complexes containing  $\text{D}_2\text{O}$  are marked with an asterisk (\*).

Moreover, in this case the evaporation energies (see lower panel) show a step-like behavior which reflects the tendency to an even distribution of the adsorbed  $\text{H}_2$  molecules on both Cu atoms up to  $k = 6$  as shown in Fig. 3. The evaporation energy

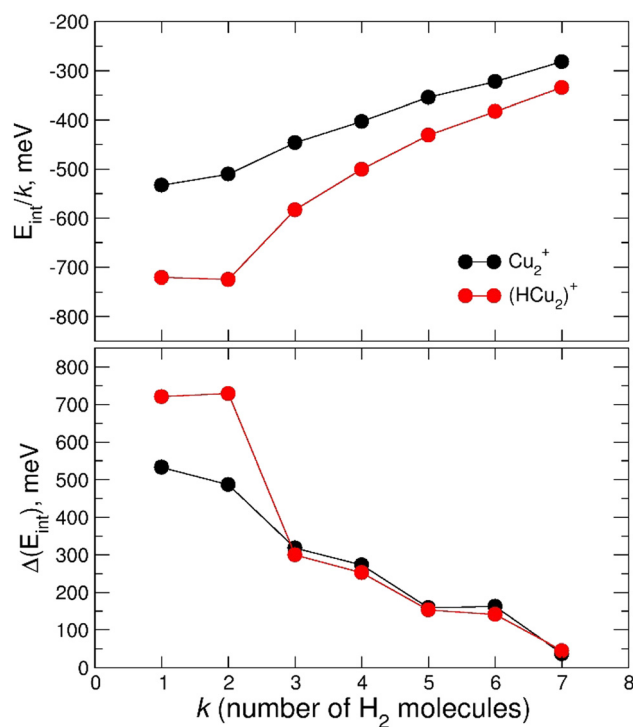


Fig. 12 Upper panel: average interaction energy  $E_{\text{int}}/k$  (in meV) obtained at the CCSD(T)/CBS level for the adsorption of  $n$   $\text{H}_2$  molecules around the  $\text{Cu}_2^+$  and  $\text{HCu}_2^+$  ions. Lower panel: as above but for the evaporation energy  $\Delta E_{\text{int}}$  (in meV).

results seem also to suggest that the  $(\text{H}_2)_2\text{HCu}_2^+$  clusters is particularly stable, which is in agreement with the experimental “magic” number reported in Table 2. A comparison between experimental bond dissociation energies (0.54, 0.44, 0.21, 0.16, 0.09 and 0.07 eV for  $k = 1-6$ , respectively)<sup>37</sup> for the  $(\text{H}_2)_k\text{Cu}_2^+$  clusters and present evaporation energies (0.53, 0.49, 0.32, 0.27,





To conclude, we believe that the present findings can be relevant not only in the applied field of hydrogen storage and release and catalysis, but also from a fundamental point of view since these clusters offer a unique opportunity to assess the gradual transition between a prevalent covalent bonding, which governs the energy and structure of the first solvation shell found for both Cu monomer and dimer cations, to that of an exclusive non-covalent behavior which determines the intermolecular interaction within the following shells.

## Author contributions

O. V. Lushchikova: conceptualization, data curation, funding acquisition, investigation, project administration, supervision, validation, visualization, writing – original draft preparation. J. Reichegger: investigation, validation. S. Kollotzek: investigation, validation. F. Zappa: investigation, methodology, validation. M. Mahmoodi-Darian: investigation. M. Bartolomei: conceptualization, formal analysis, visualization, writing – original draft preparation. J. Campos-Martínez: investigation, funding acquisition, writing – review & editing. T. González-Lezana: investigation, funding acquisition writing – review & editing. F. Pirani: conceptualization, investigation, methodology, writing – review & editing. P. Scheier: conceptualization, funding acquisition, resources, methodology, conceptualization, software, writing – review & editing.

## Conflicts of interest

There are no conflicts to declare.

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