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 Cite this: *Inorg. Chem. Front.*, 2020,
 7, 3909

Magnetic exchange interactions in symmetric lanthanide dimetallics†

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We report the synthesis and characterization of two symmetric homo-dimetallic lanthanide complexes based on methyl-substituted 8-hydroxyquinoline (HMeQ). The aryloxo-bridged core gives rise to weak magnetic coupling between pairs of Er^{III} and Yb^{III} ions, as revealed by magnetic and EPR spectroscopy studies. EPR measurements of magnetically dilute species, coupled with CASSCF-SO calculations, allows modelling of the EPR spectra of the exchange coupled species and the magnetic data simultaneously. This work adds to the database of exchange coupled {Ln₂} molecules which have been thoroughly characterised by EPR spectroscopy and modelled using an $S_{\text{eff}} = 1/2$ approach to describe the interaction of ground Kramers states, and highlights the differences between centro-symmetric and asymmetric dimetallics.

 Received 16th July 2020,
 Accepted 3rd September 2020

DOI: 10.1039/d0qi00854k

rsc.li/frontiers-inorganic

Introduction

The unique chemistry of the trivalent lanthanides (Ln^{III}) stems from their electronic configuration with the 4f orbitals shielded by filled 5s²5p⁶ subshells.¹ This makes Ln^{III} ions extremely stable, hard Lewis acids with a tendency towards high coordination numbers.² The optical and magnetic properties of lanthanide complexes have attracted much attention over the past two decades,^{3–7} for applications in medical imaging, molecular magnetism and quantum information processing (QIP).^{5–10} Dimetallic Ln^{III} complexes, where the ions are close enough to allow a magnetic interaction, can open new avenues for QIP,^{4,11–14} and also provide a simple model to study the fundamental magnetic interactions between 4f electronic manifolds.¹⁵

The 8-hydroxyquinoline pro-ligand and its derivatives are employed primarily in gravimetric analysis and as extraction reagents due to their excellent chelating properties that are applicable to many metals including lanthanides.^{16,17} Furthermore, they have attracted interest in use for preparing coordination complexes since the report of tris-8-oxoquinolinato aluminium in 1987,^{18,19} and more recently for generating polymetallic lanthanide complexes.^{20–26} We have recently used

this pro-ligand to assemble a series of asymmetric lanthanide dimetallics to study the magnetic interactions by magnetometry, electron paramagnetic resonance (EPR) and inelastic neutron scattering (INS) spectroscopies.^{27,28} We found that the exchange interactions for the asymmetric Dy₂ and Er₂ species are reasonably well described by the point-dipole model, however, there is a non-negligible superexchange component.^{27,28} For the Yb₂ asymmetric species, the point-dipole calculation underestimates the interaction, which is clearly dominated by superexchange.²⁷

Here, we study a related series of centro-symmetric molecular dimetallics (C_i point group symmetry), prepared using 2-methyl-8-hydroxyquinoline (HMeQ) with formula [Ln₂(HMeQ*)₄(NO₃)₆] where Ln^{III} = Er^{III} (1), Yb^{III} (2) and Y^{III} (3), in which the pro-ligand is deprotonated at O and protonated at N. The structures of the Y^{III}, La^{III}, Gd^{III}, Dy^{III} and Yb^{III} analogues have been reported previously,^{29,30} and here we report the novel Er^{III} analogue. Herein, we study 1 and 2 with multi-frequency EPR spectroscopy, following our previous work,^{27,28} in order to add to the database of exchange coupled species that have been comprehensively studied experimentally. We employ a pseudospin $S = 1/2$ approach to fit the EPR spectra to extract the nature of the low-lying exchange coupled states to allow benchmarking of theoretical models.³¹

Results

Synthesis

A family of three lanthanide complexes with the formula [Ln₂(HMeQ*)₂(NO₃)₆] (HMeQ* is the zwitterion deprotonated

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†Electronic supplementary information (ESI) available: Characterisation, EPR, CASSCF and SQUID data. CCDC 2015503–2015505. For ESI and crystallographic data in CIF or other electronic format see DOI: 10.1039/d0qi00854k

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at O and protonated at N; Ln = Er (**1**), Yb (**2**) and Y (**3**) were synthesised by reacting hydrated lanthanide nitrate Ln(NO₃)₃·xH₂O and HMeQ in a molar ratio of 1 : 2 in methanol. After heating to reflux for 3 hours, the solution was filtered and slowly evaporated yielding yellow block-shape crystals suitable for single crystal X-ray diffraction, which revealed the symmetric Ln^{III} dimetallics. The doped samples (Ln@**3**), where Ln = Er (**1a**) or Yb (**2a**), were synthesised using the same procedure but employing a mixture of Ln(NO₃)₃·xH₂O and Y(NO₃)₃·xH₂O in a 1 : 19 molar ratio with HMeQ in methanol (1 : 49 ratio for the **2a** EPR spectroscopy sample).

Structural description

The complexes [Ln₂(HMeQ*)₂(NO₃)₆] **1–3** crystallise in the monoclinic space group *P*2₁/*n*, Fig. 1, S1, and Table S1/2.† The structure lies about a crystallographic inversion centre. Here, the structure of **1** is described as representative of the isostructural series.

The Er^{III} site is bonded to three chelating nitrate anions, two μ-O atoms from bridging HMeQ* ligands and an O-atom from a third terminal HMeQ* unit. The Er–Er distance is 3.8725(7) Å and the Er–O–Er angle is 112.3(2)°, compared to the shorter 3.4456(8) Å distance between the two Er^{III} ions in the asymmetric dimetallic [H₂Q][Ln₂(Q)₄(NO₃)₃]·MeOH, which contains an unsubstituted oxoquinolate (HQ) molecule.²⁸ The smaller separation in the asymmetric molecule is likely a result of the reduced steric bulk which allowed three bridging ligands forcing a wider Er–O–Er angle 96.6(7)°.

The coordination of the Er^{III} site consists of nine oxygen atoms: the shortest Er–O distance, 2.189(8) Å, is to the oxygen from the terminal HMeQ*. The two bonds to the μ-O from HMeQ* have 2.328(7) and 2.334(5) Å distances. The six oxygen atoms from three chelating nitrate ligands have longer bonds with an average distance of 2.46(4) Å. Two of the nitrate ligands at Er, defined by N3 and N5, are approximately *trans* to each other. Selected angles and distances are reported in the ESI† for comparison across the series. The coordination environment of the metal can be described as a spherical

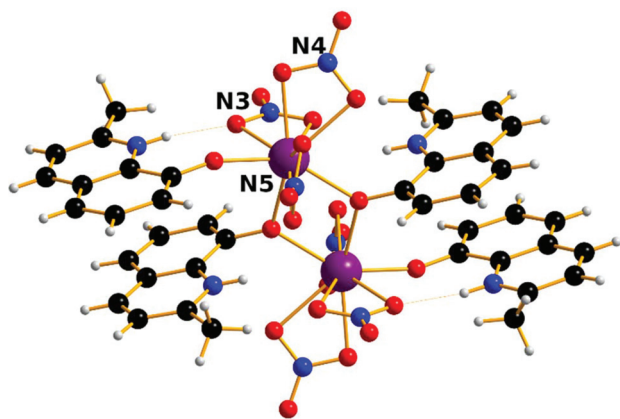


Fig. 1 Solid state molecular structure of **1**; Scheme: Er, purple; N, blue; O, red; C, grey; H, light grey.

capped square antiprism, Fig. S2,† and is confirmed by the program SHAPE, Table S3.†^{32,33} Despite the coordination environment being well-distributed on a sphere (*i.e.* arrangement of donor atoms lacking significant anisotropy), the presence of a short terminal bond to monodentate HMeQ* will contribute to the magnetic anisotropy, as was previously found for the Dy^{III} analogue, which behaves as a single-molecule magnet.²⁹

Magnetometry

The solid-state magnetic properties of **1** and **2** were studied with magnetic susceptibility measurements between 1.8–300 K. For both samples the values of $\chi_M T$ at room temperature are close to the expected value for two non-interacting Ln^{III} ions (Table S4†) and decline smoothly on cooling due to depopulation of the crystal field levels, Fig. S3.† Magnetisation data do not reveal any additional information with the Yb^{III} analogue approaching saturation at 3.8 N_Aμ_B at 7 T and 2 K, while the Er^{III} system does not saturate reaching 10.1 N_Aμ_B at 7 T and 2 K, Fig. S4.†

Investigation of [Er₂(HMeQ*)₂(NO₃)₆] (**1**)

EPR spectroscopy of magnetically dilute 1a. EPR spectroscopy was performed on magnetically diluted samples in order to establish the exchange-free properties of the Ln^{III} ions experimentally. The dilute system **1a** was measured at Q-band frequency, which revealed three rhombic *g*-values for the isolated Er^{III} site, Fig. 2. Using the PHI software,³⁴ these values are fitted using eqn (1) to give *g*₁ = 10.72, *g*₂ = 4.85 and *g*₃ = 2.68, where we omit the hyperfine coupling term as no hyperfine structure is observed.

$$\hat{H} = \mu_B \vec{B} \cdot (\vec{g}_1 \cdot \hat{S}_1 + \vec{g}_2 \cdot \hat{S}_2) + \sum_{i=1,2} \sum_{n \text{ nuclei}} A_n \vec{I} \cdot \hat{S}_i \quad (1)$$

CASSCF-SO calculations of 1. Complete active space self-consistent field spin-orbit (CASSCF-SO) calculations were employed as a means of determining the principal axes for the reference



Fig. 2 Q-Band EPR measurement at 33.995818 GHz collected at 5 K on the 5% diluted **1a** [Y{5%Er}₂(HMeQ*)₂(NO₃)₆] (black) with the fitted spectrum (red), following the procedure outlined in previous work.²⁷ *g*-Values are in Table 1, linewidths: *lw*₁ = 1.7, *lw*₂ = 2.3 and *lw*₃ = 1.3 GHz.



frame in which the g -matrix is diagonal and for validation of the experimentally determined g -values, Tables S5 and S6.† Since the system is symmetric, calculations were performed on a single Ln site, where the inactive Ln^{III} was substituted with Lu^{III} . The calculations for Er^{III} yield theoretical g -values of $g_1 = 12.8$, $g_2 = 3.19$ and $g_3 = 1.90$ (Table S5†), which are in fair agreement with EPR data for **1a**; note that there may be some change in the g -values associated with doping Er^{III} into the host lattice of **3**.²⁷ The axis associated with g_1 is oriented roughly towards the *trans*-nitrate ligands, while the g_3 axis is found to point towards one of the bridging O1 atoms, Fig. 4. The angle between the g_1 -axis and the Er–Er vector is 99.0° , where the g_1 -axis is approximately normal to the plane of the Er_2O_2 core. The first excited Kramers doublet is predicted to lie at 29 cm^{-1} , which should not be appreciably populated at the temperature of the EPR experiment (5 K). The experiment is therefore interpreted assuming it has probed only the ground doublet.

EPR spectroscopy of **1 and simulation of exchange.** EPR measurements of the pure dimer **1** were performed at S-, X-, K- and Q-band (Fig. 3), as the different frequencies provide comp-

lementary information. The spectra at Q- and K-band frequencies show splitting of each g -feature into three peaks, however at lower X- and S-band frequencies, there are fewer discernible features and much broader peaks. As a starting point, we calculate the exact point-dipole exchange matrix (eqn (S7)†) using eqn (2) for **1**,²⁸ and use this to simulate the coupled spectra with eqn (3) in PHI. To simulate these spectra we used the approach outlined in our previous work:²⁷ we employ the pseudospin $S = 1/2$ formalism where \hat{S}_1 and \hat{S}_2 are the pseudospin operators representing the ground Kramers doublets on each Ln ion and we define the principal g -values of the ground Kramers doublet on each Er^{III} ion from those experimentally determined for **1a**, while the associated orientations of the g -frames with respect to the molecular geometry are taken from CASSCF-SO calculations (Fig. 4).

$$\bar{D}_{AB} = \frac{\mu_B^2}{-2r^2} \left(\bar{g}_A \cdot \bar{g}_B - 3(\bar{g}_A \cdot \bar{R})(\bar{R}^T \cdot \bar{g}_{AB}) \right) \quad (2)$$

$$\hat{H} = -2\hat{S}_1 \cdot \bar{J} \cdot \hat{S}_2 + \mu_B(\hat{S}_1 \cdot \bar{g}_1 + \hat{S}_2 \cdot \bar{g}_2) \cdot \bar{B} \quad (3)$$



Fig. 3 EPR spectra (black lines) collected at 5 K for **1** at (a) Q-band (33.970818 GHz), (b) K-band (23.791 GHz), (c) X-band (9.37198 GHz) and (d) S-band (3.87285 GHz), with simulations in red from the parameters presented in Table 1.



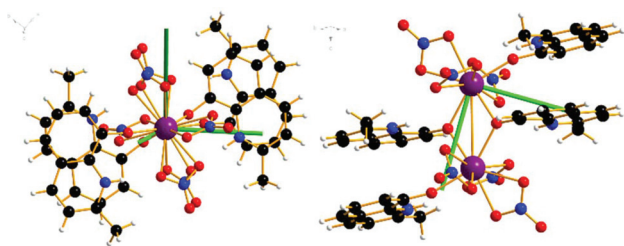


Fig. 4 Orientation of the principal g -axes ($g_1 =$ dark green) for the ground doublet from CASSCF-SO single site calculations of **1**, with view down Er–Er bond (left) and down g_1 axis (right).

These simulations (Fig. S5†) clearly show that dipolar coupling alone is not sufficient to explain the exchange interactions in **1**, and hence there must be a non-zero superexchange component. Thus, following our previous work, we fit the data of the pure species with an explicit exchange coupling Hamiltonian. In this case the principal g -values for the two Er^{III} ions are identical and their orientations are rigorously coparallel (due to the centre of symmetry), and we define the diagonal anisotropic exchange matrix such that the J_z component lies along the Er–Er vector. Note that here we perform simulations in the g -matrix reference frame where the principal g -values are associated with the Cartesian axes, and due to the centre of symmetry, the only rotations required to define the orientation of the principal g -values with respect to the molecular geometry are the α and β angles that fix J_z along the Er–Er vector. The orientation of the J_x and J_y directions are left as a fitting parameter *via* the angle γ (Fig. S21;† corresponding to clockwise rotation around J_z); when $\gamma = 0$, the angle between J_y and the terminal Er–hq oxide is *ca.* 8° (eqn (S1)–(S3) and Fig. S15†). As a result of the centre of symmetry, neither the Zeeman term (magnetic field) nor the anisotropic exchange coupling can mix the $S_{\text{eff}} = 0$ and $S_{\text{eff}} = 1$ states, and due to the $\Delta S = 0$ and $\Delta m_s = \pm 1$ EPR selection rules, the spectra are insensitive to the isotropic component of the exchange interaction. Therefore, we enforce a traceless exchange matrix for the modelling of **1** and **2**. Surveying values of the anisotropic exchange parameters in the range $-1 < J_a < +1 \text{ cm}^{-1}$ allows us to find parameters that give excellent simulations of the experimental data (Fig. 3 and Table 1). The exchange frame is shown in Fig. S15,† depicting the initial and the final fitted orientations.

We present the simulation using the traceless anisotropic interaction matrix \bar{J} , Fig. 3 and Table 1, which are in excellent agreement across all frequencies. A similar quality simulation, with slight variations in the peak intensities, is obtained using the opposite sign ($-\bar{J}$) interaction matrix, Fig. S6.† As the reported best-fit parameters are independent of the isotropic part, there is an infinite number of solutions of the form $\pm\bar{J} + n\bar{I}$, where n is any real number and \bar{I} is the identity matrix. To estimate the isotropic component, we simulate the low temperature magnetic data using our exchange models ($+\bar{J}$ or $-\bar{J}$) from EPR simulations along with a variable n , where we find good agreement for n between -0.5 and

Table 1 Simulation parameters for the fitting of EPR data for **1**

Parameter	Value(s)		
\bar{J}	$J_x (\text{cm}^{-1})$	$J_y (\text{cm}^{-1})$	$J_z (\text{cm}^{-1})$
	0.31	−0.25	−0.07
\bar{g}	g_1	g_2	g_3
	10.72 (fixed)	4.85 (fixed)	2.68 (fixed)
\bar{R}^a	$\alpha (^\circ)$	$\beta (^\circ)$	$\gamma (^\circ)$
	16.7 (fixed)	261.0 (fixed)	35.0
Linewidths (Lorentzian)	$lw_x (\text{GHz})$	$lw_y (\text{GHz})$	$lw_z (\text{GHz})$
Q-band	4.0	5.0	5.0
K-band	2.0	4.0	3.0
X-band	2.0	2.0	3.5
S-band	2.0	2.0	3.0

^a Rotation matrices use PHI convention, eqn (S1)–(S3).†

+1.0 cm^{-1} (Fig. S12†). It is worth noting that both $+\bar{J}$ and $-\bar{J}$ predict lower values for magnetic data at low temperature compared with experiment, which likely indicates a positive isotropic component is needed. Despite the excellent reproduction of the experimental EPR spectra, literature has shown that while CASSCF-SO calculations are a powerful tool for approximating the electronic structure of Ln(III)-based molecules,³⁵ the principal magnetic axes of highly-anisotropic ions are not always predicted accurately enough compared to experiment. While there tends to be good agreement for Dy(III) complexes,^{36–41} a landmark study found that the calculated axes for isostructural Er(III) and Yb(III) molecules can have significant deviations compared to experimental axes from single-crystal measurements,⁴² although there are counterexamples where theory is supported by experiment for Er(III).⁴³ However, due to the lack of single-crystal magnetometry/EPR data here, it is necessary to assess the validity of fixing the orientations of the principal g -values from CASSCF-SO calculations. Therefore, we have altered the rotation of the exchange matrix α and β angles (see above) for combinations of $\pm 5^\circ$ and $\pm 10^\circ$, and re-optimised the exchange coupling parameters; here we are relying on the highly-featured nature of the multi-frequency EPR spectra to validate our orientation model. Variations of $\pm 5^\circ$ show no visual changes to the best-fit spectra and there is no change to the fitted exchange couplings (Table S10 and Fig. S18†); at $\pm 10^\circ$ degrees the fits are less good in all cases, but the refined parameters are nearly identical across all fits (Table S10 and Fig. S17†). Therefore, we believe that the CASSCF-SO-calculated orientations are reliable for the purposes of extracting information on the low-lying exchange coupling.

Investigation of $[\text{Yb}_2(\text{HMcQ}^*)_2(\text{NO}_3)_6]$ (**2**)

EPR spectroscopy of magnetically dilute 2a. The Yb analogue was investigated in the same way, however, a 5% dilution still gave signal from the dimetallic species, so a 2% dilution was necessary to isolate a single site. Despite the weak signal from this sample, clear g_1 and g_2 features are observed in Q-band measurements, Fig. S7.† These data can be fitted with Easyspin⁴⁴ to yield principal g -values of $g_1 = 6.15$ and $g_2 = 1.82$



with g_3 unobserved (hyperfine coupling constants are calculated from the linear relation between g and A ,⁴⁵ for ^{171}Yb $A_i = 796g_i - 43$ MHz and ^{173}Yb $A_i = 232g_i - 18$ MHz, giving $A_1 = 4852$ and 1409 MHz and $A_2 = 1406$ and 404 MHz, for ^{171}Yb and ^{173}Yb respectively).

CASSCF-SO calculations of 2. CASSCF-SO calculations for 2 are in reasonable agreement with the experimental data, giving $g_1 = 7.34$ and $g_2 = 1.17$, and suggest that $g_3 = 0.68$, Table S5;† this feature is out of the field range of our Q- and K-band spectrometers, and due to the high dilution and low signal-to-noise ratio is not observable at X- and S-bands; for this CASSCF-SO-calculated g -value, A_3 is calculated to be $A_3 = 498$ and 140 MHz for ^{171}Yb and ^{173}Yb , respectively. In this case the first excited doublet lies at 223 cm^{-1} . Similar to 1, the g_1 principal axis points roughly between the two *trans*-nitrate ligands (and thus approximately normal to the Yb_2O_2 plane), while the directions of g_2 and g_3 are close to the Yb_2O_2 plane and have almost 45° angles with the Yb–Yb vector (44.0° (g_2) and 46.5° (g_3)), Fig. 5. In this case, the angle between the g_1 direction and the Yb–Yb vector is 84.3° . The similar orientations for Er^{III} and Yb^{III} arise due to the similarities in the aspherical 4f electron density distributions of the m_j states for these two ions.⁴⁶

EPR spectroscopy of 2 and simulation of exchange. For 2, the EPR spectra indicate only very small interactions between the two Yb^{III} ions due to its similar form to the EPR spectrum of 2a, Fig. 6 and S8.† In 2a, only two g -values could be seen at Q-band, and measurements at lower frequencies could not be obtained due to the weak signal from the 2% dilution. In the spectra of 2, the two observed g -values in 2a at Q-band are now split into doublets and there is an additional doublet in the region of the ‘unobserved’ high-field g -value at X- and S-band. The high-field feature shows a slight variation in effective g -values of 0.72 and 0.58 at X- and S-band, respectively, Fig. 6 (based on the mean field position of the two peaks). Here, a point-dipole calculation (eqn (2)) seems to overestimate the coupling compared to what is observed experimentally, Fig. S9 and eqn (S8),† suggesting that there is a small superexchange component in opposition to the dipolar coupling.

As before, the experimental g -values from 2a are used as the starting point for the model, with CASSCF-SO defining the orientation of the g -frames and the diagonal exchange matrix

defined with J_z along the interatomic Yb–Yb vector. Comparing the spectra of 2 and 2a, there is a clear shift in the position of the g_1 feature, which is centred at a lower field in the pure Yb_2 sample, Fig. S8.† This observation is consistent with our previous work showing that doping into diamagnetic lattices can give slight changes in the local CF environment compared to the pure sample, which manifests as shifts in the g -values.²⁷ We therefore allowed g_1 as a variable parameter in the modelling process, which gives $g_1 = 6.4$, Table 2. As the CASSCF-SO calculated g_3 value (0.68) lies between the mean observed g_3 -features (0.72 and 0.58), it is fixed for the simulations. Simulating the spectra with Easyspin⁴⁴ using eqn (4), we obtain good agreement with the observed spectra using an axially-symmetric exchange Hamiltonian, Fig. 6 and Table 2. As with the analysis of 1, the trace of the exchange matrix is fixed to zero. As axial symmetry is adequate for the simulation (where $J_x = J_y$) rotation of the exchange reference frame around J_z is irrelevant and γ is arbitrary. Again, the isotropic component does not influence the EPR spectrum, and inverting the sign of the reported exchange matrix ($-\bar{J}$) gives a similar splitting with opposite relative intensities of the g_1 peaks evident in the Q- and K-band simulations, Fig. S10.† Here, both $+\bar{J}$ and $-\bar{J}$ are in good agreement with low temperature magnetic data, Fig. S13.† Using the magnetic data as a probe of the isotropic component, in the form $\pm\bar{J} + n\bar{I}$, we find n in the range -0.5 to $+0.5\text{ cm}^{-1}$, Fig. S14.†

To assess the accuracy of the CASSCF-SO-calculated g -matrix orientations, we have again altered the rotation of the exchange matrix α and β angles for combinations of $\pm 5^\circ$ and $\pm 10^\circ$, and re-optimised the exchange coupling parameter. Two out of four variations of $\pm 5^\circ$ show good best-fit spectra while the other two are poor, but in all cases the fitted exchange coupling parameter changes by $<8\%$ (Fig. S19 and Table S10†) At ± 10 degrees the fits are significantly worse in all cases, but even here the exchange coupling only changes $<26\%$ (Fig. S20 and Table S10†). Thus we believe the CASSCF-SO-calculated orientations are reliable.

$$\hat{H} = -2\hat{S}_1 \cdot \bar{J} \cdot \hat{S}_2 + \mu_B \bar{B} \cdot (\bar{g}_1 \cdot \hat{S}_1 + \bar{g}_2 \cdot \hat{S}_2) + \sum_{i=1,2} \sum_n \hat{I}_n \cdot \bar{A} \cdot \hat{S}_i \quad (4)$$

Discussion

With these simulations in hand, we can compare the fitted exchange matrices to the point-dipolar ones. It is worth comparing both the magnitude of the overall exchange $\pm\bar{J} + n\bar{I}$, as well as the observed anisotropy between the largest and smallest parameters. We find that the point dipole matrix for 1 predicts only a single significant term as a result of the large co-parallel principal g_1 values (eqn (S7),† left). Representing this dipolar interaction in the same reference frame as the final simulation (eqn (S7),† right) shows major negative contributions (-0.15 to -0.32 cm^{-1}) in the J_{xx} , J_{xy} and J_{yx} positions. The magnitudes of these terms are comparable with those

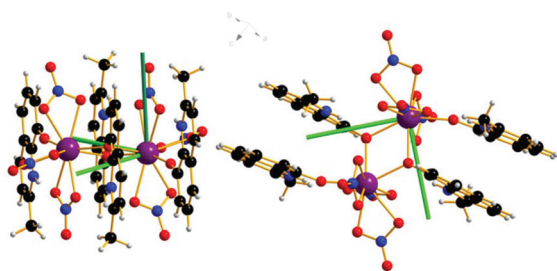


Fig. 5 Orientation of the principal g -axes ($g_1 =$ dark green) for the ground doublet from CASSCF-SO calculations of 2, with view perpendicular to Yb–Yb bond (left) and down the g_1 axis (right).



Initially focussing on the $\{\text{Er}_2\}$ compounds, the difference between the largest and smallest anisotropic exchange parameters is similar for **1** and $[\text{H}_2\text{Q}][\text{Er}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$ (0.56 and 0.78 cm^{-1} , respectively) and there are some similarities between the two sets of multi-frequency EPR spectra. All spectra have the major spectral feature occurring at low field, likely still having a strong relationship to the g_1 feature of the individual ions. In **1**, the exchange-free g -features from **1a** are still discernible as multiplet peaks, while for $[\text{H}_2\text{Q}][\text{Er}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$ it is impossible to assign the spectra in such a way. It is important to recall that $[\text{H}_2\text{Q}][\text{Er}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$ has six unique g -values corresponding to the two distinct and non-collinear Er^{III} environments,²⁷ and this is likely the origin of the increased complexity.

The biggest contrast is seen between **2** and $[\text{H}_2\text{Q}][\text{Yb}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$, where **2** is very weakly coupled and all features are clearly assignable to the g -features of the exchange-free ions; this is drastically different to the highly detailed spectra observed for $[\text{H}_2\text{Q}][\text{Yb}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$. Correspondingly, there is a large change in the difference between the largest and smallest anisotropic exchange parameters for **2** and $[\text{H}_2\text{Q}][\text{Yb}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$ (0.07 vs. 0.55 cm^{-1} , respectively). We found that dipolar coupling alone was insufficient to describe the spectra for $[\text{H}_2\text{Q}][\text{Yb}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$, and for **2** the predicted dipolar coupling produces larger splitting in the spectra than what is observed experimentally, thus suggesting that there is a superexchange component working in opposition to the dipolar interaction in **2**. These differences are all consistent with the larger Yb–Yb separation observed in **2** compared to $[\text{H}_2\text{Q}][\text{Yb}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$.

Conclusions

Multi-frequency EPR spectroscopy has been performed on magnetically dilute and pure samples of $[\text{Ln}_2(\text{HMeQ}^*)_4(\text{NO}_3)_6]$ where $\text{Ln}^{\text{III}} = \text{Er}^{\text{III}}$ (**1**) and Yb^{III} (**2**). The EPR spectra for the dilute samples show simple rhombic signals of the ground Kramers doublets, while the EPR spectra for the pure samples are highly-featured, providing direct evidence of the exchange interactions between the lowest lying doublets. By modelling the EPR spectra of pure samples of **1** and **2** using a combined experimental and theoretical approach, we have been able to effectively measure the exchange coupling. We find that dipolar coupling alone is not sufficient to explain the coupled spectra for **1**, allowing us to infer a significant superexchange component. For **2**, we find that dipolar exchange coupling is approximately twice as large as the observed exchange anisotropy, again suggesting an important, yet small, superexchange component. Compared to the asymmetric relatives of **1** and **2**, $[\text{H}_2\text{Q}][\text{Ln}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$ $\text{Ln}^{\text{III}} = \text{Dy}^{\text{III}}$, Er^{III} and Yb^{III} that we have studied previously,^{27,28} the magnitude of the anisotropic exchange is comparable for the $\{\text{Er}_2\}$ dimetallics, while the symmetric $\{\text{Yb}_2\}$ species **2** exhibits far weaker

exchange coupling than $[\text{H}_2\text{Q}][\text{Yb}_2(\text{Q})_4(\text{NO}_3)_3]\cdot\text{MeOH}$, leading to much simpler EPR spectra.

Experimental section

Reagents and general procedures

All metal salts, pro-ligands and solvent were used without further purification. Lanthanides salts $\text{Ln}(\text{NO}_3)_3\cdot x\text{H}_2\text{O}$, where $\text{Ln} = \text{Er}$, Yb and Y and 2-methyl-8-hydroxyquinoline were purchased from Sigma Aldrich.

Infrared spectroscopy, SQUID and elemental analysis

IR spectra of pure powders were recorded using a Thermo Scientific Nicolet iS5 IR Spectrometer equipped with an iD5 ATR. All magnetic measurements were performed using a Quantum Design MPMS-XL7 SQUID magnetometer equipped with a 7 T magnet. Elemental analysis of the complexes was obtained by The University of Manchester microanalytical service.

X-ray crystallography

The crystal data for compound **1** were collected on an Agilent Technologies SuperNova 4-circle diffractometer with a $\text{MoK}\alpha$ microfocus source and an EOS CCD detector at a temperature of 150 K. The crystal data for compounds **2** and **3** were collected on a Bruker X8 Prospector 3-circle diffractometer with a $\text{CuK}\alpha$ microfocus source and an APEX II detector at a temperature of 100 K.

Structure solution and refinement was performed with the Shelx package⁴⁷ using the program Olex2.⁴⁸

The structures were solved by direct methods and completed by iterative cycles full-matrix least-squares refinement against F^2 . All nonhydrogen atoms were refined anisotropically. Hydrogen atoms were calculated geometrically and refined in riding mode on their respective atoms.

Synthesis

The general procedure requires 1 mmol of 2-methyl-8-hydroxyquinoline (HMeQ) added to a solution of $\text{Ln}(\text{NO}_3)_3\cdot x\text{H}_2\text{O}$ (0.5 mmol) in methanol (20 mL), where $\text{Ln} = \text{Er}$, Yb and Y . Then the resultant solution was heated to reflux for 3 hours.²⁹ The solution was filtered and left for slow evaporation for 1 to 3 days, resulting in yellow block-shaped crystals suitable for X-ray crystallography.

The doped samples $(\text{Ln}@\text{Y}_2)$ where $\text{Ln} = \text{Er}^{\text{III}}$ (**1a**), Yb^{III} (**2a**) were prepared by mixing $\text{Ln}(\text{NO}_3)_3\cdot n\text{H}_2\text{O}$ and $\text{Y}(\text{NO}_3)_3\cdot n\text{H}_2\text{O}$ in a 5 : 95 or 2 : 98 molar ratio with HMeQ in methanol according to the synthesis method above.

$[\text{Er}_2(\text{HMeQ}^*)_2(\text{NO}_3)_6]$ (**1**). Quantities: HMeQ (0.159 g, 0.221 mmol), $\text{Er}(\text{NO}_3)_3\cdot 5\text{H}_2\text{O}$ (0.221 g, 0.5 mmol). Yield 0.137 g (62% based on Er). IR cm^{-1} : 3283(w), 3196(w), 1631(m), 1582(s), 1538(w), 1464(s), 1391(w), 1095(m), 1034(s), 893(m), 823(s), 739(s), 578(s). Elem. Anal. Calc. (%) for $\text{C}_{40}\text{H}_{36}\text{Er}_2\text{N}_{10}\text{O}_{22}$ ($M_w = 1340.06$): C, 35.76; H, 2.70; N, 10.42; Er, 24.40; found: C, 35.40; H, 2.85; N, 10.46; Er, 23.88.



[Yb₂(HMeQ*)₂(NO₃)₆] (2). Quantities: HMeQ (0.159 g, 1 mmol), Yb(NO₃)·6H₂O (0.224 g, 1 mmol). Yield 0.134 g (60% based on Yb). IR cm⁻¹: 3284(w), 3194(w), 1633(m), 1582(s), 1539(w), 1464(s), 1391(w), 1096(m), 1036(s), 894(m), 824(s), 740(s), 577(s). Elem. Anal. Calc. (%) for C₄₀H₃₆Yb₂N₁₀O₂₂ (M_w = 1356.07): C, 35.46; H, 2.67; N, 10.33; Yb, 25.54; found: C, 35.42; H, 2.72; N, 10.41; Yb, 25.39.

[Y₂(HMeQ*)₂(NO₃)₆] (3). Quantities: HMeQ (0.159 g, 1 mmol), Y(NO₃)·6H₂O (0.191 g, 0.5 mmol). Yield 0.106 g (56% based on Y). IR cm⁻¹: 3284(w), 3197(w), 1632(m), 1582(s), 1539(w), 1463(s), 1391(w), 1095(m), 1035(s), 893(m), 824(s), 740(s), 578(s). Elem. Anal. Calc. (%) for C₄₀H₃₆Y₂N₁₀O₂₂ (M_w = 1186.67): C, 40.48; H, 3.05; N, 11.80; Y, 14.98; found: C, 40.52; H, 2.95; N, 11.56; Y, 14.86.

Electron paramagnetic resonance

EPR spectra were collected at S-, X-, K- and Q-band frequencies using Bruker EMX300 and Elexsys E580 spectrometers. Measurements were performed on lightly ground polycrystalline samples restrained in eicosane as a means of avoiding magnetic torque alignment during measurements. The spectra were collected at 5 K cooled using either a closed cycle cooling system or liquid helium cooling.

Ab initio calculations

Complete active space self-consistent field spin-orbit (CASSCF-SO) calculations were performed using Molcas 8.0⁴⁹ on the isolated molecules using the structural solutions reported from XRD measurements. Due to the inversion symmetry of the dimetallic, only a single calculation on one of the ion sites is necessary to determine the exchange-free properties. The central ion is described using VTZP quality from the ANO-RCC library and the ion not in focus was replaced by the diamagnetic Lu^{III} ion.^{50,51} The first coordination sphere atoms use VDZP quality and all other atoms use VDZ quality. The active space comprises the 4f orbitals with 11 and 13 active electrons for Er^{III} and Yb^{III}, respectively. State averaged CASSCF calculations are performed for Er^{III} with 35 quartets and 112 doublets, with all states incorporated for SO coupling, while for Yb^{III} only 7 doublet states are required for CASSCF and SO coupling.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

We thank The University of Manchester and EPSRC EPR National Research Facility (NS/A000055/1) for access to the EPR spectrometers and SQUID magnetometer, and the EPSRC for funding an X-ray diffractometer (grant number EP/K039547/1). We thank Dr Jim Raftery for assistance with X-ray crystallography. M. J. G. thanks The University of Manchester

for a President's Doctoral Scholarship. S. A.-B. thanks the Higher Committee for Education Development in Iraq (HCED) for the award of a research scholarship. N. F. C. thanks The University of Manchester for a Presidential Fellowship, The Royal Society for a University Research Fellowship, and the European Research Council for a Starting Grant (ERC-2019-STG-851504). R. E. P. W. thanks the EPSRC for an Established Career Fellowship (EP/R011079/1) and the European Research Council for an Advanced Grant (ERC-2017-ADG-786734). This project has received funding from the European Research Council (ERC) under the European Union's Horizon 2020 research and innovation programme (grant agreements no. 786734 and 851504).

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