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Discovery of superconductivity in technetium borides at moderate pressures

This research conducted thorough investigations on the superconductivity, mechanical properties and phase stability of the technetium–boron binary system. Five unprecedented superconducting technetium–borides were discovered at moderate or even ambient pressure, representing a fresh group in the family of superconducting metal–borides. The 4d-electrons of technetium play a dominant role for the electron–phonon coupling in these superconducting technetium–borides, in contrast with MgB_2 . The various structures and stoichiometries of these superconducting technetium–borides suggest rich possibilities in looking for other superconducting transition-metal borides.

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Discovery of superconductivity in technetium borides at moderate pressures†

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Advances in theoretical calculations have boosted the search for high-temperature superconductors, such as sulfur hydrides and rare-earth polyhydrides. However, the required extremely high pressures for stabilizing these superconductors has handicapped further implementation. Based upon thorough structural searches, we identified a series of unprecedented superconducting technetium borides at moderate pressures, including TcB ($P6_3/mmc$) with a superconducting transition temperature of $T_c = 20.2$ K at ambient pressure and TcB₂ ($P6/mmm$) with $T_c = 23.1$ K at 20 GPa. Superconductivity in these technetium borides mainly originates from the coupling between the low-frequency vibrations of technetium atoms and the dominant technetium-4d electrons at the Fermi level. Our work therefore presents a fresh group in the family of superconducting borides, whose diversified crystal structures suggest rich possibilities in the discovery of other superconducting transition-metal borides.

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1 Introduction

The discovery of superconductivity in mercury¹ motivated a century-long race for higher-temperature superconductors. Owing to the progress in theoretical calculations,^{2–5} numerous high-temperature superconducting hydrides have been discovered in the past decade, including H₃S ($T_c \approx 191$ – 204 K at 200 GPa)^{6,7} and LaH₁₀ ($T_c \approx 274$ – 286 K at 210 GPa) with record-high superconducting transition temperatures.^{8–11} However, the stable presence of these superconducting hydrides requires very high pressures, which largely limits their potential implementations.^{12–14}

Among all Bardeen–Cooper–Schrieffer (BCS) superconductors, borides represent a unique category with superconductivity at relatively low pressures. MgB₂ has the highest superconducting transition temperature, $T_c = 39$ K, among all BCS-type superconductors at ambient pressure.¹⁵ At present, the discovered bulk superconducting borides with the same stoichiometry as MgB₂ include CaB₂ ($T_c \sim 50$ K¹⁶ or 9.4–28.6 K¹⁷ at ambient pressure, theory), NbB₂ ($T_c \sim 9.2$ K at ambient pressure, experiment^{18–20}),

OsB₂ ($T_c = 2.1$ K at ambient pressure, experiment²¹), RuB₂ ($T_c = 1.6$ K at ambient pressure, experiment²¹), ScB₂ ($T_c = 1.5$ K at ambient pressure, experiment²²), WB₂ (maximum $T_c = 15$ K at 100 GPa, experiment²³), ZrB₂ ($T_c = 5.5$ K at ambient pressure, experiment²⁴), SiB₂ ($T_c = 21$ K at ambient pressure, theory²⁵) and MoB₂ ($T_c = 32$ K at 100 GPa, experiment²⁶). Superconducting borides with other stoichiometries include X₇B₃ (X = Re and Ru with $T_c = 3.3$ and 2.6 K, respectively, at ambient pressure, experiment^{27,28}), Re₃B ($T_c = 4.8$ K at ambient pressure, experiment²⁸), X₂B (X = Mo, Re, Ta and W with $T_c = 5.1$, 2.8, 3.1 and 3.2 K, respectively, at ambient pressure, experiment²⁷), XB (X = Hf, Nb, Mo, Ta and Zr with $T_c = 3.1$, 8.3, 0.5, 4.0 and 2.8–3.4 K, respectively, at ambient pressure, experiment²⁷), FeB₄ ($T_c = 2.9$ K at ambient pressure, theory and experiment^{29,30}), XB₅ (X = Na, K, Rb, Ca, Sr, Ba, Sc and Y with $T_c = 17.5$, 14.7, 18.6, 6.6, 6.8, 16.3, 14.2 and 12.3 K, respectively, at ambient pressure, theory³¹), BeB₆ ($T_c = 24$ K at 4 GPa, theory³²), CB₆ ($T_c = 12.5$ K at ambient pressure, theory³³), MgB₆ ($T_c = 9.5$ K at 32.6 GPa, theory³⁴), ScB₆ (in $P2_1/m$ -, $C2/m$ - and $Cmcm$ -structure with $T_c = 5.8$ K at ambient pressure, 2.2 K at 500 GPa, and 2.6 K at 800 GPa, respectively, theory³⁵), XB₆ (X = Nb, La, Th and Y with $T_c = 3.0$, 5.7, 0.74 and 7.1 K, respectively, at ambient pressure, experiment²⁷), XB₇ (X = Li, Na, K, Mg, Ca and Sr with $T_c = 21.6$, 18.3, 26.2, 29.3, 7.7 and 12.7 K, respectively, at ambient pressure, theory³⁶), RbB₆ and RbB₈ ($T_c = 7.3$ – 11.6 K and 4.8–7.5 K at ambient pressure, respectively, theory³⁷), YB₆ ($T_c = 7.2$ K at ambient pressure, experiment³⁸), LaB₈ ($T_c = 14$ K³⁹ or 20 K⁴⁰ at ambient pressure, theory), XB₁₂ (X = Nb, La, Th, Y and Zr with $T_c = 3.0$, 5.7, 0.74, 7.1 and 5.8 K, respectively, at ambient pressure, experiment^{27,41–43}), ternary borides like SrB₃C₃ ($T_c = 22$ K at 23 GPa, theory and

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experiment⁴⁴), or even quaternary borides RbYbB₆C₆ and RbBaB₆C₆ (both with $T_c \approx 71$ K at ambient pressure, theory⁴⁵).

There have been extensive efforts in searching for similar metal-boride superconductors since the discovery of MgB₂ as presented above. Unfortunately, the outcomes have been discouraging in that the T_c values of most metal borides are much lower than that of MgB₂. However, the recent experimental discovery of superconducting MoB₂ with $T_c = 32$ K at 100 GPa²⁶ has ignited further enthusiasm in looking for superconducting transition-metal borides at lower pressures or even at ambient pressure. In addition, the superconducting mechanism of MoB₂ is suggested to be very different from MgB₂. In MgB₂ the B-p electrons play a dominant role in its superconductivity,^{46,47} while in MoB₂ its Mo-4d electrons contribute majorly.^{26,48} This raises two essential questions: (1) Can we find other superconducting transition-metal borides neighboring to MoB₂, with T_c at least above 10 K and at moderate pressures? (2) Does the superconducting mechanism of MoB₂ apply to other superconducting transition-metal borides? To answer these two questions, we decided to work on borides of technetium, which comes immediately after molybdenum in the periodic table.

Although technetium is rare in nature, technetium-based compounds have been investigated in multiple disciplines in the past. ATcO₃ perovskites (where A = Ca, Sr, Ba) have attracted extensive interest due to their extremely high antiferromagnetic Néel temperatures (750–1200 K).^{49–52} First-principle calculations have predicted a stable structure of ternary compound Tc₂AlB₂ with *Cmcm* symmetry at ambient pressure.⁵³ Recently, technetium hydrides were theoretically predicted and then experimentally synthesized under high pressure.^{54,55}

Technetium borides have been extensively investigated due to their outstanding mechanical properties.^{56–76} Three technetium borides have long been synthesized experimentally at ambient pressure,⁵⁶ Tc₃B (*Cmcm*) with an orthorhombic structure, and Tc₇B₃ (*P6₃/mmc*) and TcB₂ (*P6₃/mmc*, Vickers hardness 38.4 GPa⁷⁶ or 39.4 GPa⁷⁵) with hexagonal structures. Later theoretical calculations also proposed three stoichiometries of TcB, TcB₃ and TcB₄.^{62,70–75} First-principle DFT calculations by Li *et al.*⁶² suggested that hexagonal TcB (*P6₃/mmc*) could be energetically stable. Structural searches by Wu *et al.*⁷¹ found a thermodynamically stable TcB (*Cmcm*) structure above 8 GPa. Later structural searches by Zhang *et al.*⁷² led to the argument that TcB (*P3m1*, Vickers hardness 30.3 GPa) could be energetically more stable than the above two structures. Structural predictions by Van Der Geest *et al.*⁷⁰ suggest there are two thermodynamically stable structures, TcB (*Pnma*) and TcB₄ (*P6₃/mmc*), at 30 GPa. First-principle DFT calculations by Miao *et al.*⁷⁴ reported a thermodynamically stable TcB₃ structure (*P6₃/mmc*, Vickers hardness 29 GPa) above 4 GPa. Structural searches by Ying *et al.*^{73,75} suggested two structures, TcB₃ (*P6₃/mmc*, Vickers hardness 30.7 GPa) and TcB₄ (*P6₃/mmc*, Vickers hardness 32.4 GPa), that are thermodynamically stable at 0 and 100 GPa, respectively. However, the discussions of possible superconductivity in technetium borides are totally absent.

In this paper, we choose to search the technetium–boron binary system for new superconductors. A comprehensive

phase diagram of all thermodynamically stable technetium borides up to 180 GPa has been derived. We also found five superconducting technetium borides possessing metastable states for the first time, including TcB (*P6₃/mmc*), TcB₂ (*P6₃/mmc*), Tc₂B (*I4/mcm*), Tc₃B (*P4/mmm*) and TcB (*Cmcm*), that remain dynamically stable at low or even ambient pressures. The mechanical properties of these superconducting technetium borides have been investigated as well.

2 Methods

The structure prediction for technetium–boron binary crystals is performed by the CALYPSO package.⁷⁷ The crystal structures and the X-ray diffraction (XRD) patterns are generated by the VESTA package. The electronic structures and the phonon properties are calculated using the QUANTUM-ESPRESSO (QE) package.⁷⁸ The plane-wave kinetic-energy cutoff and the charge density energy cutoff are 100 Ry and 400 Ry, respectively. An optimized norm-conserving pseudopotential with valence electron configurations of Tc-4p⁶ 4d⁵ 5s² and B-2s² 2p¹ and a Methfessel–Paxton smearing⁷⁹ width of 0.02 Ry is used.

The dynamic matrix and the electron–phonon coupling (EPC) constant λ are calculated using the density functional perturbation theory.⁸⁰ The superconducting transition temperature is estimated following the Allen–Dynes modified McMillan equation,⁸¹

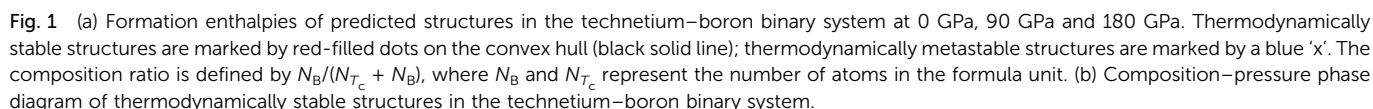
$$T_c = \frac{\omega_{\log}}{1.2} \exp \left[-\frac{1.04(1 + \lambda)}{\lambda - \mu^*(1 + 0.62\lambda)} \right], \quad (1)$$

in which λ is the average EPC parameter, ω_{\log} is the logarithmic average frequency, and the Coulomb pseudopotential⁸² $\mu^* = 0.12$. Mechanical properties including Vickers hardness are estimated following models by Chen *et al.* and Tian *et al.*^{83,84} Calculation details are given in the ESI.†

3 Results and discussion

3.1 Convex hull and phase diagram

We have done variable-composition and fixed-composition structure searches in the Tc–B system at pressures of 0, 90 and 180 GPa. Thermodynamically stable structures and the derived composition–pressure phase diagram are presented in Fig. 1. Three existing technetium borides at ambient pressure, Tc₃B (*Cmcm*), Tc₇B₃ (*P6₃/mmc*) and TcB₂ (*P6₃/mmc*), have been successfully identified. Tc₃B (*Cmcm*) is thermodynamically stable up to 180 GPa in our study. In contrast, Tc₇B₃ (*P6₃/mmc*) and TcB₂ (*P6₃/mmc*) stop being energetically favorable above 60 GPa and 139 GPa, respectively, and a new TcB₂ (*I4₁/amd*) thermodynamically stable phase shows up above 170 GPa. Two previously predicted structures, TcB₃ (*P6₃/mmc*)^{73,74} and TcB₄ (*P6₃/mmc*),^{70,75} also have been found in our calculations, and these structures are thermodynamically stable above 2 and 35 GPa, respectively. We found a TcB (*P2₁*) structure that is thermodynamically stable above 24 GPa, then transfers into a *Pmn2₁* structure at 63 GPa, and finally into the previously predicted *Pnma* structure⁷⁰ at



atom above the hull), Tc_3B ($P4/mmm$, 248 meV per atom above the hull) and TcB ($Cmcm$, 25 meV per atom above the hull). These five superconducting technetium borides stay dynamically stable at decreased pressures. The minimum dynamically stable pressures of TcB_2 ($P6/mmm$) and TcB ($Cmcm$) are 20 and 30 GPa, respectively, while TcB ($P6_3/mmc$), Tc_2B ($I4/mcm$) and Tc_3B ($P4/mmm$) are dynamically stable even at ambient pressure.

The superconducting transition temperatures of the technetium borides are presented in Fig. 2, together with the transition temperatures of other known superconducting metal borides that have been measured experimentally for benchmarking. As shown in Fig. 2b, the superconducting transition temperatures of the technetium borides in our study increase at decreased pressure. Although the superconducting transition temperatures of all five technetium borides are always lower than those of MgB_2 ¹⁵ and MoB_2 ,²⁶ they are higher than the superconducting transition temperatures of other metal borides in Fig. 2a at their lowest dynamically stable pressures. In addition, TcB_2 ($P6/mmm$) and TcB

9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178 179 180 181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 197 198 199 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216 217 218 219 220 221 222 223 224 225 226 227 228 229 230 231 232 233 234 235 236 237 238 239 240 241 242 243 244 245 246 247 248 249 250 251 252 253 254 255 256 257 258 259 260 261 262 263 264 265 266 267 268 269 270 271 272 273 274 275 276 277 278 279 280 281 282 283 284 285 286 287 288 289 290 291 292 293 294 295 296 297 298 299 300 301 302 303 304 305 306 307 308 309 310 311 312 313 314 315 316 317 318 319 320 321 322 323 324 325 326 327 328 329 330 331 332 333 334 335 336 337 338 339 340 341 342 343 344 345 346 347 348 349 350 351 352 353 354 355 356 357 358 359 360 361 362 363 364 365 366 367 368 369 370 371 372 373 374 375 376 377 378 379 380 381 382 383 384 385 386 387 388 389 390 391 392 393 394 395 396 397 398 399 400 401 402 403 404 405 406 407 408 409 410 411 412 413 414 415 416 417 418 419 420 421 422 423 424 425 426 427 428 429 430 431 432 433 434 435 436 437 438 439 440 441 442 443 444 445 446 447 448 449 450 451 452 453 454 455 456 457 458 459 460 461 462 463 464 465 466 467 468 469 470 471 472 473 474 475 476 477 478 479 480 481 482 483 484 485 486 487 488 489 490 491 492 493 494 495 496 497 498 499 500 501 502 503 504 505 506 507 508 509 510 511 512 513 514 515 516 517 518 519 520 521 522 523 524 525 526 527 528 529 530 531 532 533 534 535 536 537 538 539 540 541 542 543 544 545 546 547 548 549 550 551 552 553 554 555 556 557 558 559 560 561 562 563 564 565 566 567 568 569 570 571 572 573 574 575 576 577 578 579 580 581 582 583 584 585 586 587 588 589 590 591 592 593 594 595 596 597 598 599 600 601 602 603 604 605 606 607 608 609 610 611 612 613 614 615 616 617 618 619 620 621 622 623 624 625 626 627 628 629 630 631 632 633 634 635 636 637 638 639 640 641 642 643 644 645 646 647 648 649 650 651 652 653 654 655 656 657 658 659 660 661 662 663 664 665 666 667 668 669 670 671 672 673 674 675 676 677 678 679 680 681 682 683 684 685 686 687 688 689 690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708 709 710 711 712 713 714 715 716 717 718 719 720 721 722 723 724 725 726 727 728 729 730 731 732 733 734 735 736 737 738 739 740 741 742 743 744 745 746 747 748 749 750 751 752 753 754 755 756 757 758 759 760 761 762 763 764 765 766 767 768 769 770 771 772 773 774 775 776 777 778 779 780 781 782 783 784 785 786 787 788 789 790 791 792 793 794 795 796 797 798 799 800 801 802 803 804 805 806 807 808 809 810 811 812 813 814 815 816 817 818 819 820 821 822 823 824 825 826 827 828 829 830 831 832 833 834 835 836 837 838 839 840 841 842 843 844 845 846 847 848 849 850 851 852 853 854 855 856 857 858 859 860 861 862 863 864 865 866 867 868 869 870 871 872 873 874 875 876 877 878 879 880 881 882 883 884 885 886 887 888 889 890 891 892 893 894 895 896 897 898 899 900 901 902 903 904 905 906 907 908 909 910 911 912 913 914 915 916 917 918 919 920 921 922 923 924 925 926 927 928 929 930 931 932 933 934 935 936 937 938 939 940 941 942 943 944 945 946 947 948 949 950 951 952 953 954 955 956 957 958 959 960 961 962 963 964 965 966 967 968 969 970 971 972 973 974 975 976 977 978 979 980 981 982 983 984 985 986 987 988 989 990 991 992 993 994 995 996 997 998 999 1000 1001 1002 1003 1004 1005 1006 1007 1008 1009 1010 1011 1012 1013 1014 1015 1016 1017 1018 1019 1020 1021 1022 1023 1024 1025 1026 1027 1028 1029 1030 1031 1032 1033 1034 1035 1036 1037 1038 1039 1040 1041 1042 1043 10

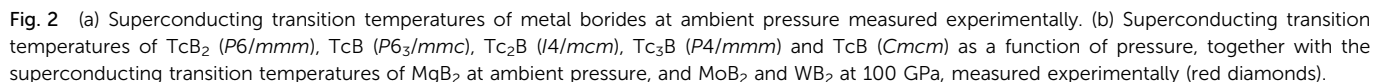


Table 1 Total electronic density of states (DOS) at the Fermi level $N(E_F)$, EPC parameter λ , logarithmic average frequency ω_{\log} , and superconducting transition temperature T_c of the superconducting technetium borides at their lowest dynamically stable pressures

Formula	Space group	P (GPa)	$N(E_F)$ (states per eV per f.u.)	λ	ω_{\log} (cm^{-1})	T_c (K)
TcB ₂	$P6/mmm$	20	1.41	1.85	125.1	23.1
TcB	$P6_3/mmc$	0	1.63	1.56	126.1	20.2
Tc ₂ B	$I4/mcm$	0	1.75	0.85	165.1	10.9
Tc ₃ B	$P4/mmm$	0	2.85	0.92	162.9	12.9
TcB	$Cmcm$	30	1.05	0.96	135.5	11.5

($P6_3/mmc$) have higher superconducting transition temperatures at 100 GPa than WB₂ with $T_c = 15$ K.²³

We also present the superconducting transition temperatures of the five technetium borides at their lowest dynamically stable pressures, together with their total electronic DOS at the Fermi level $N(E_F)$, the EPC parameter λ and the logarithmic average frequency ω_{\log} in Table 1. TcB₂ ($P6/mmm$) has the highest superconducting transition temperature of 23.1 K at 20 GPa, which comes from its largest EPC parameter of $\lambda = 1.85$. In contrast, TcB ($Cmcm$) has a much lower superconducting transition temperature of 11.5 K at 30 GPa due to its small EPC parameter of $\lambda = 0.96$. The superconducting transition temperatures of TcB ($P6_3/mmc$), Tc₂B ($I4/mcm$) and Tc₃B ($P4/mmm$) at 0 GPa are 20.2, 10.9, and 12.9 K, respectively. Although the EPC parameters λ of these metastable technetium borides are not small, their logarithmic average frequencies ω_{\log} are rather low with a maximum of 165.1 cm^{-1} , which limits their superconducting transition temperature. This is in sharp contrast with MgB₂, which has a smaller λ value of 0.87 but a much larger ω_{\log} value of 504 cm^{-1} , and the highest BCS-type superconducting transition temperature of 39 K at ambient pressure.⁸⁵

The thermodynamically metastable nature of the discovered superconducting technetium borides doesn't necessarily exclude their experimental synthesis. Metastable materials have long been synthesized and implemented,⁸⁶ typically like fullerene C₆₀. As for superconductors, DFT calculations predict NdH₉ ($P6_3/mmc$) has a formation enthalpy that is 35 meV per atom above the convex hull at 150 GPa, yet it has been successfully synthesized with $T_c \approx 4.5$ K.⁸⁷ Several metastable borides have been predicted to be superconducting in recent structural searches. Xia *et al.* discovered thermodynamically metastable CB₆ with a superconducting transition temperature of 12.5 K at ambient pressure.³³ Zhang *et al.* also found thermodynamically metastable RbB₆ ($Pm\bar{3}m$) and RbB₈ ($Immm$) with superconducting transition temperatures of 7.3–11.6 and 4.8–7.5 K at ambient pressure, respectively.³⁷ These works further validate the importance and necessity of our discoveries of superconducting technetium borides.

3.3 Crystal structures

The crystal structures of the five superconducting technetium borides in our study are presented in Fig. 3. TcB₂ ($P6/mmm$) shares exactly the same crystal structure with MgB₂ and MoB₂. TcB ($P6_3/mmc$) has a TiAs-type structure, in which the rhombus

Tc-layers are AB-stacking along the c -axis and the rhombus B-layers are sandwiched between the neighbouring Tc-layers. Tc₃B ($P4/mmm$) has square Tc-layers stacking in an ABB-pattern along the c -axis, and the square B-layers are located between the two Tc-layers of the BB-pattern. Tc₂B ($I4/mcm$) consists of square Tc-layers AB-stacking along the c -axis, where the neighbouring Tc-layers are twisted by 37.2 degrees. The B-layers in Tc₂B ($I4/mcm$) are sandwiched between the neighbouring Tc-layers as well. In TcB ($Cmcm$), the square Tc-layers stack in an ABCD-pattern along the b -axis, and the B atoms form zig-zag chains along the c -axis between the AB and CD Tc-layers. The angle of the zig-zag chain of the B atoms is around 108.8 degrees. Crystal structure information and the XRD patterns of the superconducting technetium borides are presented in Table S3 and Fig. S3 of the ESI.†

3.4 Electronic structures

The electronic DOS of superconducting technetium borides at their lowest stabilizing pressure are presented in the left column of Fig. 4. The electronic DOS of all technetium borides share certain features. The total DOS at the Fermi level are dominated by the states of the Tc-4d bands. Although the B-2p DOS have considerable weight away the Fermi level, its contribution is minor at the Fermi level, if not zero. The B-2s DOS almost vanish around the Fermi level, which makes the B-2s bands almost irrelevant for electronic conduction. Our DOS results for technetium borides have a close resemblance to those for the transition-metal boride MoB₂,²⁶ while they are in obvious contrast to results for the alkali-earth-metal boride MgB₂^{46,47} and the alkali-metal boride RbB₆.³⁷ In both MgB₂^{46,47} and RbB₆,³⁷ the major DOS at the Fermi level are contributed by the B-p bands. But in both the superconducting technetium borides of our study and MoB₂,²⁶ the 4d electronic states play dominant roles around the Fermi level.

The electronic band structures, the partial DOS of the Tc-4d orbitals and the Fermi surfaces of the superconducting technetium borides are presented in Fig. S2 of the ESI.† For all five superconducting technetium borides, either their band structure or their Fermi surface show obvious electronic dispersion in three dimensions. Typically, for example, TcB₂, which shares the same crystal structure as MgB₂ and MoB₂, has a three-dimensional Fermi surface like MoB₂,^{26,88} while being distinct from the quasi-two-dimensional Fermi surface of MgB₂.^{47,89}

3.5 Dynamic stability and electron-phonon coupling

The phonon spectra, the PHDOS, the Eliashberg functional $\alpha^2F(\omega)$ and the corresponding integrated EPC constant λ of the superconducting technetium borides at their lowest dynamically stable pressures are presented in the right column of Fig. 4. There is no sign of an imaginary frequency in the phonon spectra of all five superconducting technetium borides, which proves the dynamic stability of these structures at the corresponding pressures. The distribution of the PHDOS and the Eliashberg spectral functional $\alpha^2F(\omega)$ of the superconducting technetium borides show clear separation between the low-frequency phonon modes of the heavier Tc atoms and the high frequency phonon modes of the lighter B atoms. This enables us to separate the integrated

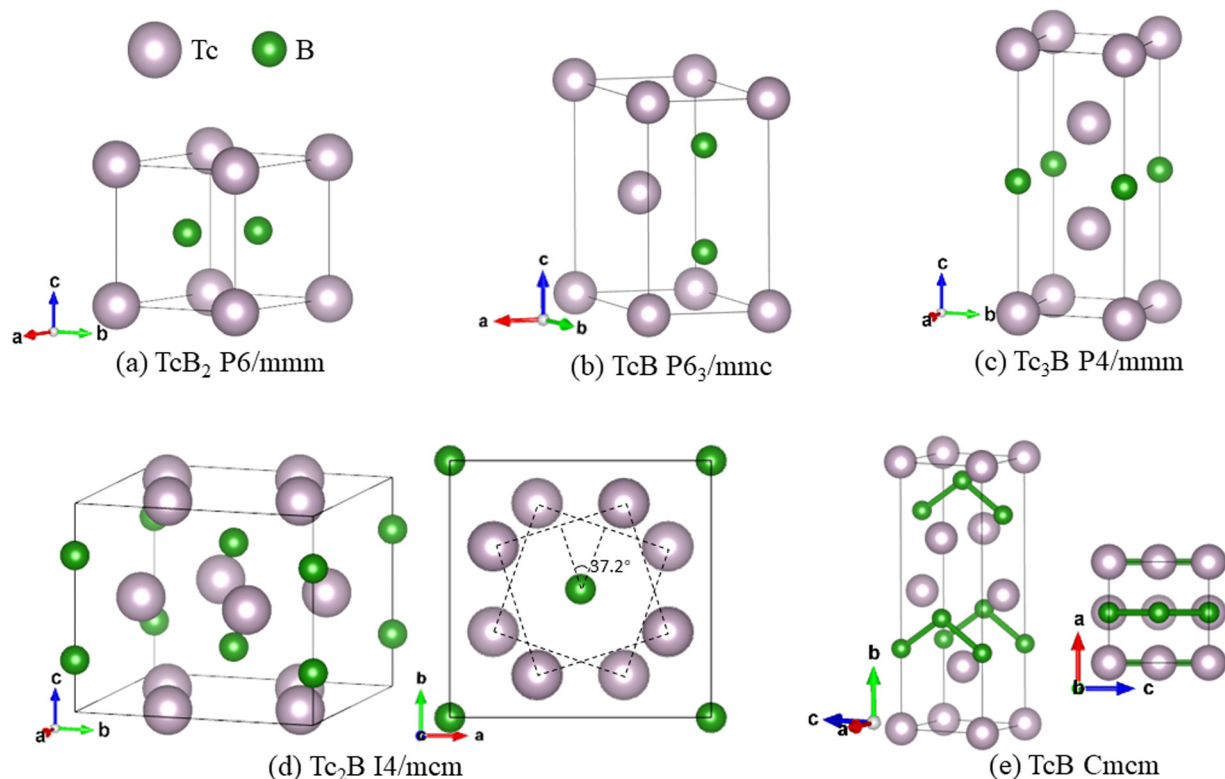


Fig. 3 Crystal structures of superconducting technetium borides. (a) TcB_2 ($P6/mmm$), (b) TcB ($P6_3/mmc$), (c) Tc_3B ($P4/mmm$), (d) Tc_2B ($I4/mcm$) and (e) TcB ($Cmcm$). The technetium and boron atoms are represented by spheres of coral and green colors, respectively.

EPC constant λ into two parts, the EPC from the Tc atoms λ_{Tc} and the EPC from the B atoms λ_{B} . The ratio of EPC from oscillation of the Tc atoms relative to the total EPC, $\lambda_{\text{Tc}}/\lambda$, are 0.883, 0.910, 0.873, 0.907 and 0.911 for TcB_2 ($P6/mmm$), TcB ($P6_3/mmc$), Tc_2B ($I4/mcm$), Tc_3B ($P4/mmm$) and TcB ($Cmcm$), respectively. It indicates that superconductivity in these five technetium borides mainly originates from the coupling between the Tc-4d electrons and the low frequency phonon modes of the Tc atoms.

The superconducting mechanism of our predicted technetium borides is similar to that in the transition-metal boride MoB_2 , whose superconductivity mainly originates from the coupling between the Mo-4d electrons and the low frequency Mo-phonon modes.²⁶ However, the superconducting scenarios in the alkali-earth-metal boride MgB_2 ^{46,47} and the alkali-metal boride RbB_6 ³⁷ are very different in that the couplings between the B-2p electrons and the high-frequency B-phonon modes play dominant roles. At least three isotopes of technetium have reasonably long half-lives (Tc-97, Tc-98 and Tc-99 at 4.2×10^6 , 6.6×10^6 and 2.13×10^5 years, respectively). Therefore, we suggest experiments on the isotope effects of technetium to examine our prediction.

Observations in the phonon spectra, PHDOS and EPC of the superconducting technetium borides are consistent with their relatively smaller logarithmic average frequency ω_{\log} as listed in Table 1, since Tc atoms are much heavier than B atoms. The enhanced λ plus small ω_{\log} characteristics of TcB_2 have also been seen in the iso-structural superconductor TlBi_2 of heavy atomic mass,⁹⁰ with $\lambda = 1.4$, $\omega_{\log} = 37 \text{ cm}^{-1}$ and rather low

$T_c = 5.5 \text{ K}$. Recent work suggests that the introduction of hydrogen atoms into the non-superconducting transition-metal boride Ti_2B_2 will result in superconducting $\text{Ti}_2\text{B}_2\text{H}_4$ ($T_c = 48.6 \text{ K}$ at ambient pressure), through expansion of the frequency range of the phonon spectrum and consequently enlarged electron-phonon coupling.⁹¹ Similar hydrogenation probably helps in elevating the superconducting transition temperatures of technetium borides by the enlarged ω_{\log} .

Another interesting observation on the discovered superconducting technetium borides is that the Fermi levels of TcB_2 and TcB fall closely above the peak positions of their DOS, as shown in Fig. 4. Since the EPC in technetium borides is controlled by the coupling between the Tc-4d electrons and the oscillation of the Tc atoms, slight hole-doping could lower the Fermi level, thus enhancing the effective number of electrons participating in the superconducting pairing and therefore increasing the superconducting transition temperatures.

3.6 Hardness

We also calculated the Vickers hardness of the discovered superconducting technetium borides as presented in Table 2. At ambient pressure, TcB ($P6_3/mmc$), Tc_2B ($I4/mcm$) and Tc_3B ($P4/mmm$) have Vickers hardness values of 2.8–4.8, 11.8–13.0 and 10.0–11.3 GPa, respectively. The Vickers hardness values of TcB_2 ($P6/mmm$) and TcB ($Cmcm$) are 9.8–11.3 GPa and 12.2–13.7 GPa at pressures of 20 and 30 GPa, respectively. The superconducting technetium borides in our study have lower hardness values than

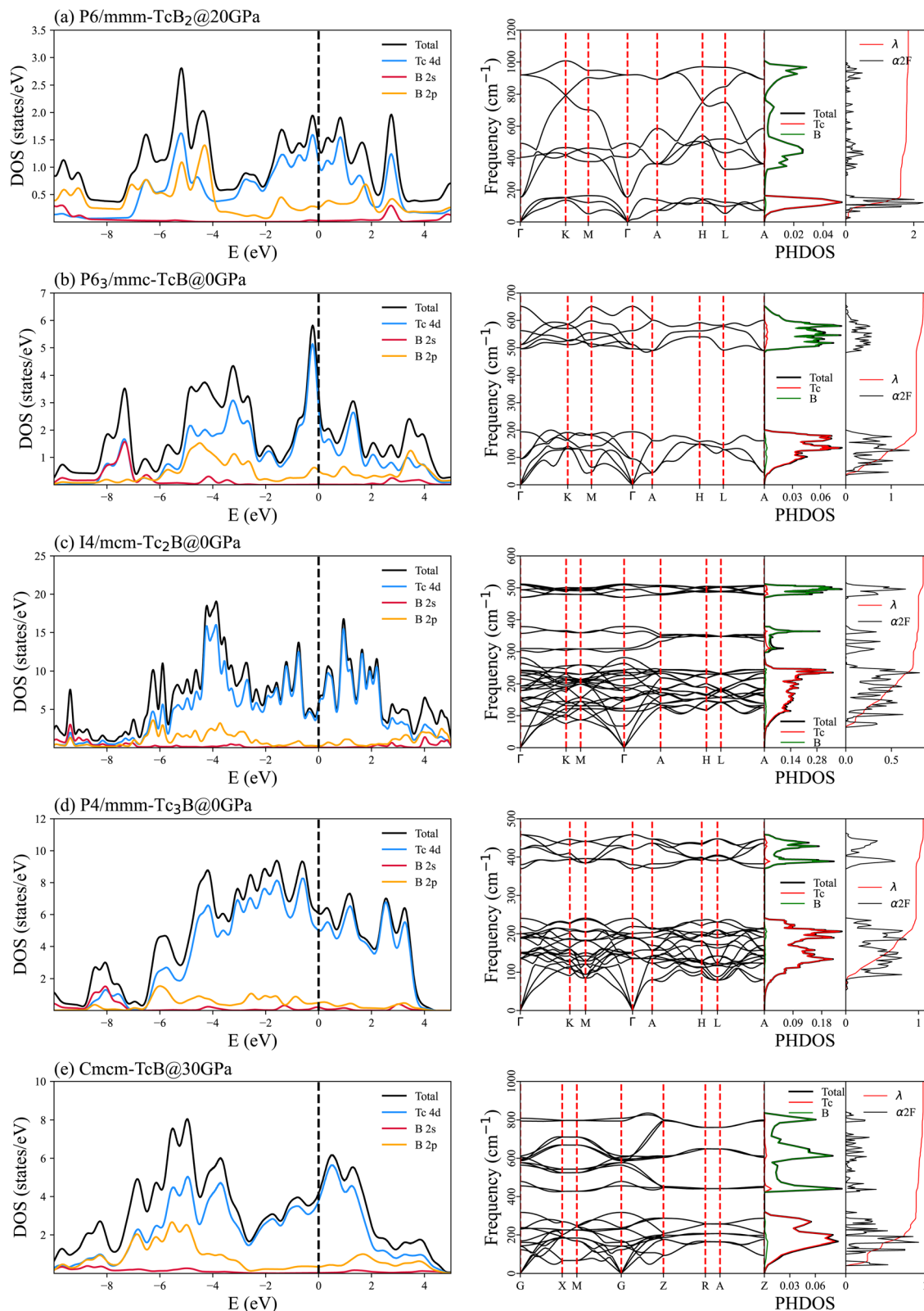


Fig. 4 Total and partial electronic DOS, phonon dispersion relation, phonon density of states (PHDOS), Eliashberg functional $\alpha^2F(\omega)$ and integrated EPC parameter $\lambda(\omega)$ of superconducting technetium borides at their lowest dynamically stable pressures. From top to bottom: (a) TcB_2 ($P6/mmm$, 20 GPa), (b) TcB ($P6_3/mmc$, 0 GPa), (c) Tc_2B ($I4/mcm$, 0 GPa), (d) Tc_3B ($P4/mmm$, 0 GPa) and (e) TcB ($Cmcm$, 30 GPa).

Table 2 Vickers hardness of superconducting technetium borides at their lowest dynamically stable pressures

Formula	Space Group	<i>P</i> (GPa)	<i>H_v</i> ,Chen ⁸³ (GPa)	<i>H_v</i> ,Tian ⁸⁴ (GPa)
TcB ₂	<i>P6₃/mmm</i>	20	10.6	12.0
TcB	<i>P6₃/mmc</i>	0	2.8	4.8
Tc ₂ B	<i>I4/mcm</i>	0	11.8	13.0
Tc ₃ B	<i>P4/mmm</i>	0	10.0	11.3
TcB	<i>Cmcm</i>	30	12.2	13.7

those previously stated for superconducting superhard borides, for example RbB₆ (*Pm3̄m*, Vickers hardness of 19.7 GPa at ambient pressure) and RbB₈ (*Immm*, Vickers hardness of 36.9 GPa at ambient pressure).³⁷ Other mechanical parameters including elastic constants *C_{ij}*, bulk modulus *B*, and shear modulus *G* at their lowest dynamically stable pressures were also calculated. Mechanical stability criteria⁹² related to the elastic constants of these superconducting technetium borides are fulfilled as presented in the ESI.†

4 Conclusions

In summary, we have conducted thorough structural searches in the technetium–boron binary system. An updated composition–pressure phase diagram for technetium borides at up to 180 GPa have been derived, including two new stoichiometries as Tc₃B₄ and Tc₂B. More importantly, we also found five unprecedented superconducting technetium borides that remain dynamically stable at moderate or even ambient pressures. Among these thermodynamically metastable superconducting technetium borides, TcB₂ (*P6₃/mmm*) has the highest superconducting transition temperature of 23.1 K at 20 GPa, and TcB (*P6₃/mmc*) has the highest superconducting transition temperature of 20.2 K at ambient pressure. The superconductivity in these technetium borides mainly originates from the coupling between the dominant presence of Tc-4d electronic states around the Fermi level and the low-frequency vibrational modes of the technetium atoms, which are closely analogous to another transition-metal-boride MoB₂. Our calculations not only identified that superconducting TcB₂ (*P6₃/mmm*) has the same crystal structure as MgB₂ and MoB₂, but also led to the discovery of a series of superconducting technetium borides with diversified crystal structures. This work proves the rich structures and stoichiometries in superconducting technetium borides at high pressures, thus indicating the necessity for extended research in the discovery of new superconducting transition-metal borides.

Conflicts of interest

There are no conflicts of interest to declare.

Acknowledgements

P. Z., Y. D. Q. and S. X. Y. designed the project; X. R. T. conducted the structure searches; P. Z. and A. Q. Y. calculated the electronic structures, the phonon spectra and the superconducting

transition temperatures; all authors prepared the manuscript together. We would like to thank Jianjun Ying, Defang Duan and Zihao Huo for the important discussions in preparing this manuscript. This work is supported by the National Natural Science Foundation of China (Grants No. 11604255), the Fundamental Research Funds for the Central Universities (Grants No. xzy022023011 and xhj032021014-04), and the Natural Science Basic Research Program of Shaanxi (Grants No. 2021JM-001). Shuxiang Yang is supported by the Key Research Projects of Zhejiang Lab (Grant No. 2021PB0AC02). The computations were performed at the TianHe-2 national supercomputing center in Guangzhou and the HPC platform of Xian Jiaotong University.

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