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A review of recent advances and applications of machine learning in tribology†

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In tribology, a considerable number of computational and experimental approaches to understand the interfacial characteristics of material surfaces in motion and tribological behaviors of materials have been considered to date. Despite being useful in providing important insights on the tribological properties of a system, at different length scales, a vast amount of data generated from these state-of-the-art techniques remains underutilized due to lack of analysis methods or limitations of existing analysis techniques. In principle, this data can be used to address intractable tribological problems including structure–property relationships in tribological systems and efficient lubricant design in a cost and time effective manner with the aid of machine learning. Specifically, data-driven machine learning methods have shown potential in unraveling complicated processes through the development of structure–property/functionality relationships based on the collected data. For example, neural networks are incredibly effective in modeling non-linear correlations and identifying primary hidden patterns associated with these phenomena. Here we present several exemplary studies that have demonstrated the proficiency of machine learning in understanding these critical factors. A successful implementation of neural networks, supervised, and stochastic learning approaches in identifying structure–property relationships have shed light on how machine learning may be used in certain tribological applications. Moreover, ranging from the design of lubricants, composites, and experimental processes to studying fretting wear and frictional mechanism, machine learning has been embraced either independently or integrated with optimization algorithms by scientists to study tribology. Accordingly, this review aims at providing a perspective on the recent advances in the applications of machine learning in tribology. The review on referenced simulation approaches and subsequent applications of machine learning in experimental and computational tribology shall motivate researchers to introduce the revolutionary approach of machine learning in efficiently studying tribology.

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1. Introduction

Tribology – the fundamental science of interacting surfaces in relative motion – has fascinated researchers due to its applications in different fields including energy,[1,2] biomedicine,[3] biology,[4] food,[5] automobiles,[6] and aerospace.[7,8] Thus, it is no surprise that key elements in tribology, such as motion dynamics and interfacial mechanism as well as attributes of surfaces in motion, such as friction, wear, adhesion, indentation, lubrication, and so on, have been extensively studied.[9–12] For example, high energy consumption, failure of industrial processes, mechanical equipment, and increased transportation cost caused by unavoidable friction and wear have motivated researchers to understand the tribological phenomenon at different time and length scales.[13–16] In recent years, a majority of these studies have developed and employed state-of-the-art experimental methods with the intention of reducing friction and wear, which account for one-fifth of all annual energy consumption.[17] Specifically, advanced experimental techniques such as nanoindentation, atomic force microscopy and imaging,[18] digital image correlation,[19] and *in situ* spectroscopy, have been developed with the aim of studying tribological systems. Significant progress has been made in studying tribology at nano- and micro-scales through quantum *ab initio* simulations, as well as empirical, and mathematical approaches such as continuum mechanics,[20,21] multi-scale,[22] atomistic,[23] and coarse-grained molecular dynamics (CG MD) simulations,[24] non-equilibrium molecular dynamics (NEMD) simulations,[25] reactive molecular dynamics (RMD) simulations,[26] probabilistic and stochastic modeling,[27–29] finite element method,[30] and fractal methodology.[31,32]

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One of the effective ways to overcome and control friction and wear is through lubrication.[33] In recent decades, numerous studies have been conducted to enhance lubrication in moving components of machinery by developing novel lubricants. These include novel varieties of solid-based lubricants including ball-bearings, diamond-like carbon (DLC), *etc.* or liquid-based lubricants like composites of gels, mineral or vegetable oils, among others. Moreover, the reinforcement of solid-state materials like short carbon fibers (SCFs), graphite, titanium oxide (TiO_2) particles, boron carbide (B_4C), titanium carbide (TiC), silicon carbide (SiC), and/or fly ash in oil/polymer-based liquids have enhanced lubrication.[34–36] However, due to limited knowledge on the individual contributions of functionalities of each component and uncertainty associated with it, the development of new hybrid materials remains challenging. Moreover, the traditional methods to create these hybrid materials mainly rely on a highly inefficient, trial and error approach. Modern-day data-driven techniques of ML have emerged as new approaches for understanding and advancing complex processes in tribological studies. This is because, with the aid of ML, higher-dimensional problems and datasets can be modeled with ease and at a minimal cost, with better adaptive abilities to changing conditions.[37] Several studies have combined the design of experiments (DOE) and modeling techniques with ML to accelerate the design of tribological materials with the desired characteristics/properties.[38,39] This, in turn, has enabled researchers to analyze, predict, optimize, and accelerate the discovery of tribological materials by successfully establishing structure–property or structure–functionality relations in the existing available data.[40,41] Thus, it is no surprise that there has been a surge in the use of ML for tribological applications recently (2010-today) as compared to that until 2010.

The field of tribology has been explored in recent years by reviewing applications of artificial neural networks (ANNs), as well as other machine learning (ML) techniques.[37,42,43] Most of these reviews are focused on models developed using experimental data, with relatively low emphasis on computationally modeled tribological studies.[38,44] This is because, in spite of the enormous amounts of data generated using computational approaches, the use of ML to solve tribological problems has been scarce. To the best of our knowledge, this is the first comprehensive review article with a focus on applications of ML with experimental and molecular simulations studies in tribology. Specifically, we provide details of different ML methods used to perform tribological studies as well as their applications in predicting and/or studying properties and performance of tribological systems and designing novel lubricants. Thus, making this review more appealing to all the relevant scientific communities. We highlight a detailed procedure used for data-generation, including description on design of experiments (DOE), as well as the pre-processing of the experimental and/or computational data for ML methods.[38] Consequently, the importance of having the appropriate data for pre-processing tools and methods is demonstrated in improving the predictive accuracy of models based on the available data. There is a particular emphasis on integrating machine learning with optimization algorithms to resolve an important task of tuning hyperparameters during model training and the use of ML models as surrogates or objective functions during optimization. Thus, the goal of this comprehensive review is to provide insights into tribology obtained from the molecular modeling techniques and discuss recent trends of ML in the field of tribology.

We have divided this review article into six sections as presented in Fig. 1 as the contents and Table S1 of ESI.† According to different ML algorithms applied, Section 3 is divided into the 9 subsections in the subsequent order of the material formulation of (i) lubricants and (ii) composites material formulation, including (a) polymer matrix composites (PMCs), (b) metal matrix composites (MMCs), and (c) ceramic matrix composites (CMCs). Following the section on emerging, new and unexplored tribological materials, the challenges and our perspective on the applications of ML are also presented.

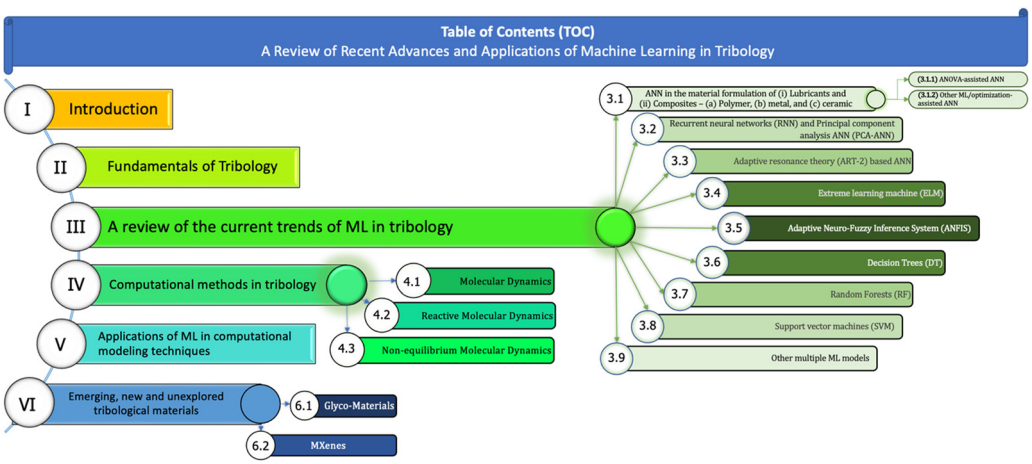

Fig. 1 The visual representation of the table of contents (overall flow) of the review is presented.

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2. Fundamentals of tribology

2.1 Experimental studies of tribology

Experimentally, tribological materials, either pure or composite, are generally assessed through a number of test rigs including pin-on-disk (POD), four-ball tester, rub shoe, *etc.* to determine physical bulk or chemical tribological properties including interfacial friction, wear, and surface energy. Here, two of the widely used test rigs to generate training data for ML models are discussed:

(i) Pin-on-disk. The friction and wear between two materials can be characterized using POD experiments. The experimental setup of materials, pin, and disk, sliding against each other is shown in Fig. 2(a). During the test, the dynamometric responses, including applied load (N), linear speed (L_s), track radii (R), and the turning speed (ω), can be varied in addition to the environmental conditions like external temperature, pressure, and humidity, as well as the lubricant additives. Here, the fixed pin holder is allowed to deflect minimally while the transducer takes care of the forces such as the applied normal force and the frictional force. The performance of the material is generally characterized by the coefficient of friction (CoF), specific wear rate (SWR), and/or wear scar diameter (WSD), determined by the mass (or volume) loss during the sliding experiment. The relative simplicity and abundance of tribological contacts make this a popular experiment for tribological tests.

(ii) Four-ball tester. The Four-ball tester as shown in Fig. 2(b) is used for analyzing lubricants for wear, extreme pressures, and frictional properties. An experimental setup involves rubbing a rotating ball against three stationary lubricated balls in order to develop and measure wear scars. The applied load, rotating speed, the temperature of contact, and time of experimental run are specified as per the American Society for Testing and Materials (ASTM) standards. The volume of wear given by its size, on the rotating ball, is indicative of the performance of the lubricant. The primary objective of this test is to evaluate the wear-prevention abilities of a lubricant.

In general, the evaluation metric for a given tribological material is through their wear characteristics like the CoF, SWR, WSD, and/or mechanical properties like compressive and tensile moduli, and strength. Typically, these properties are used to train the ML models and the following subsection describes these properties:

(i) Coefficient of friction (CoF). The CoF can be quantified as the amount of friction occurring between two surfaces. The expression for CoF can be given by eqn (1):

$$\mu(\mathrm{COF}) = \frac{\text{Frictional force } (F)}{\text{Normal force } (N)} \tag{1}$$

In the case of a low CoF, the force required for a sliding action to occur is substantially less than in the case of a high CoF.

(ii) Specific wear rate. Wear is defined as the irreversible material loss resulting from sliding of the interacting surfaces. The SWR (W_s) is calculated by the following eqn (2):

$$W_s = \frac{\Delta m}{\rho \cdot v \cdot t \cdot F_N} (\mathrm{mm^3\ N^{-1}\ m^{-1}}) \tag{2}$$

where, Δm is the mass loss, ρ is the density of the material, v is the sliding speed and t is the duration of the test. Note, here $v{\cdot}t$ can be shown as sliding distance (d). F_N represents the normal applied force imposed on that substance while sliding. However, in order to simplify and reduce testing parameters, a time-dependent depth wear rate (W_t) given in eqn (3), where Δh is the height reduction of the substance after the test, is defined to evaluate wear behavior under pv-conditions.

$$W_t = W_s \cdot p \cdot v = \frac{\Delta h}{t} (\mathrm{mm\ s^{-1}}) \tag{3}$$

2.2 Introduction to machine learning algorithms and their applications

ML has been demonstrated in numerous studies to develop a thorough understanding of structure–property relationships in complex higher dimensional tribological problems.[47–50] In addition to quantifying frictional and wear behavior, ML has

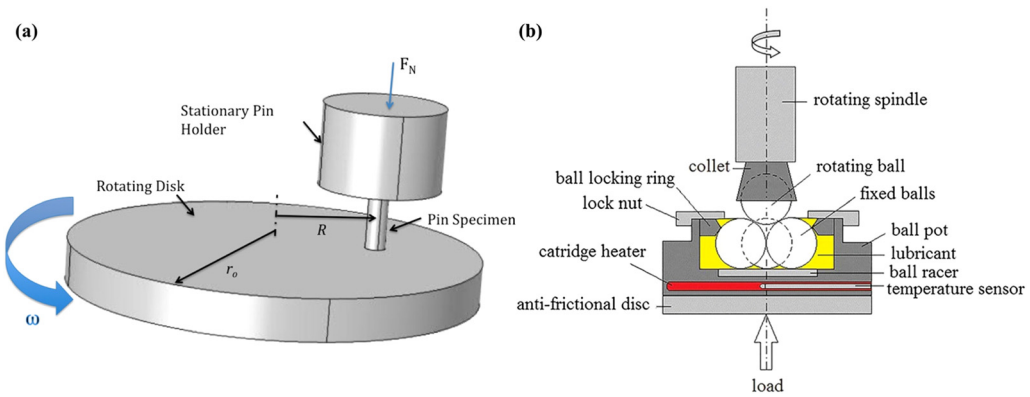

Fig. 2 (a) Schematic diagram of POD tribometer. Reproduced from ref. 45 with permission from Elsevier, copyright 2015. (b) Four ball tester schematic diagram. Reproduced from ref. 46 with permission from Springer Nature, copyright 2019.

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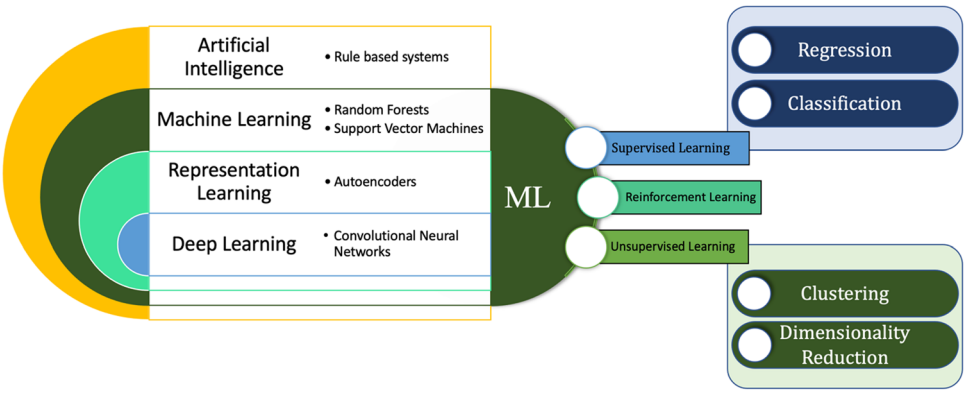

Fig. 3 The visual representation of the hierarchical methods of artificial intelligence. In addition, the classification of machine learning into supervised, unsupervised, and reinforcement learning is also presented.

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proven to be effective in the design of new lubricant materials for desired tribological applications such as ball-bearing, shaft seals, piston rings, spacecrafts, *etc.*[12,37,38,43,51] In light of the fact that the impact of multiple complex factors on a system remains uncertain in tribology, the potential of ML also goes beyond purely academic perspectives into actual industrial applications.[52,53] In general, the formulation of ML models is driven either by the deterministic approach of logic and algorithmic theory or the stochastic way of probability theory. Data preprocessing followed by an appropriate choice of the algorithm and hyperparameter tuning, constitutes the training phase of ML models. The constructed and trained ML system can thereby be used to model, analyze, and predict solutions to that problem. Given a myriad of formulated algorithms, they can be broadly classified as either 'supervised', 'unsupervised' and 'reinforcement' learning techniques as shown in Fig. 3.[54] The supervised learning approach is designed to learn through a feature-property relationship, such that the model learns over time by evaluating and improving the labeled output for a given input vector. A supervised learning model can be successfully constructed by identifying and defining a vector of unique features that are anticipated to significantly affect the outcome. Examples of supervised learning techniques include SVM, DT, RF, the Naive-Bayes model, and so on.[55] An unsupervised learning approach, on the other hand, uses an unlabeled dataset for analyzing and clustering data based on its common characteristics.[56] *K*-means clustering algorithm, hierarchical clustering, density-based spatial clustering of applications with noise (DBSCAN), *etc.* constitute the examples for unsupervised learning method. Another important category of ML models is 'reinforcement learning', which may be classified as supervised learning, employing an approach of a reward-punishment mechanism.[57] These ML models can be multi-layered feedforward NN, convolutional NN (CNN), RNN, modular NN (MNN), radial basis function NN (RBFNN), *etc.*[58]

In the field of tribology, the tribological performance of materials are not only related to their material composition or physical/chemical properties, but also on the experimental testing conditions such as external temperature, pressure, humidity, *etc.* Thus, it is crucial to understand how the performance of a material is influenced by different experimental parameters. A systematic approach of determining the important factors affecting friction and wear in complex problems can be challenging as it may require running plenty of experiments. The design of experiments (DOE) including full and fractional DOE, as well as Taguchi method can be effective as they allow a systematic study of the effect of input parameters on outcome in addition to a simple, robust, efficient, and systematic way of designing experiments.[59] The orthogonality of this DOE allows the effects of each variable to be separated from one another. Taguchi's method of DOE, in addition to the reduced number of experiments, is one of the most robust, efficient, and systematic methods to provide a parameters design for the experiments. Taguchi's method is particularly useful when operating on a set of 3 to 50 variables in which only a few variables have significant contributions and interactions are relatively minor.[60] Several studies have successfully demonstrated the use of orthogonal arrays generated by the Taguchi methodology to reduce the number of experiments.[61,62] Data obtained from these experiments are employed to model, analyze, and predict/answer the required questions, through ML/AI models. This is reviewed and discussed in-depth in the following sections, which are divided into subsections according to the aforementioned ML algorithms implemented in their studies.

3. Applications of ML algorithms in tribological experiments

3.1 Artificial neural networks (ANN)

ANNs, due to their adaptive learning, generalization, model independence, and analytical capabilities have proven vital in studying, designing, and predicting material formulations with enhanced properties in various fields of research.[63–69] Particularly, ANNs have been broadly used for optimizing minimum wear rate, high lubrication, and/or the minimum CoF. Initial successful research on the implementation of ANN includes fretting wear damage prediction,[70] tool wear,[71] faulty rolling bearings diagnosis,[72] composites' tribological properties

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prediction, surface roughness, and disk brake performance. In general, the application of ANNs to lubricant design has not only led to the discovery of novel lubricants with different additives, but has also provided physical insights into the formulation and correlation between inputs of new lubricants and resulting outputs. The recent articles on the applications of ML in the design and development of triboinformatics,[38] lubricants,[37] MMCs,[73] and structural materials[74] further shed light on the current advances in the field of tribology using ML methods. The following sections provide a review of the formulation of lubricants and composites through the utilization of ANNs.

(i) Oil-based lubricants. Friction and wear can be reduced by lubrication, which ensures a smooth relative motion between two surfaces of two bodies, resulting in reduced energy loss. Lubricants are heavily used in the manufacturing and transportation sectors.[75,76] The current focus of research on lubricants encompasses petroleum-based, composite-based, and carbon-based lubricants.[77–79] However, due to their enhanced viscosity, volatility variation with temperature, additive susceptibility, and high thermal stability, petroleum-based lubricants have gained much attention over the years.[78,79]

Jones *et al.* were the first to endeavor to model an ANN on finite available data from POD, four-ball, and rub shoe rig experiments on perfluoropolyether (PFPE) lubricant.[80] They showed that the ANN model accurately predicted the wear rate while also emphasizing on the influence of 6 input variables and specifications of material systems like sliding speed, distance, viscosity, applied load, CoF, and temperature on their tribological properties. They reported that the input layer dampened with a feedback loop (RNN architecture) was most suitable to predict the wear behavior. Because RNNs recirculate previous outputs along with new inputs from the input layer, they are able to learn better from past instances.[80] Bhaumik and Kamaraj studied for the first time, a blend of 60% glycerol and 40% castor oil (NCO), which produced a 37% reduced CoF compared to NCO and cashew nut shell liquid (CNSL) and 50% less CoF to commercial mineral oil (CMO). A total of 60 data points collected from experiments from four-ball tester rigs on the lubricant developed by varying volumetric levels of mentioned three oils were used to train an ANN model. Ignoring the testing conditions, only the significance of the content of oil (in vol%) was studied on CoF and WSD.[81] Humelnicu *et al.* used ANN to predict the low CoF composite of the diesel oil combined with two vegetable oils, namely, sunflower oil and rapeseed oil. The resulting mixture comprising 4% sunflower oil and 0% rapeseed oil indicated lower CoF compared to 0% sunflower oil and 20% rapeseed oil. In addition, ANN successfully predicted reduced CoF for 6.5% sunflower oil and 0% rapeseed oil compared to pure diesel oil, which was in good agreement with the experimental observation.[82]

Durak *et al.* successfully illustrated the use of feed-forward back-propagation neural network (BPNN) to explore the frictional behavior of the polytetrafluoroethylene (PTFE)-based additives in mineral oil under different loads and rotating speeds of the journal bearings.[83] A 3-5-3-1 BPNN architecture was implemented with load, velocity, and additive concentration as input to predict CoF as output with 98% accuracy. Their study reported the successful experimental validation of ANN predicted PTFE loadings for different forces in the optimal hydrodynamic lubrication regime. Particularly, in experiments, 10–15% of PTFE at 153 N load, and 3–5% of PTFE at 253 N yielded maximum reduction CoF, while the same was observed in ANN for 15% of PTFE at 153 N, and 10–15% of PTFE at 253 N. These four articles, as summarized in Table S2 (ESI†), successfully operated on determining a perfect blend of different oils including mineral, vegetable, and commercial oils using ANN.

(ii) Composite-based materials design for tribology. Composites, which consist of multiple heterogeneous components with the aim of achieving diverse chemical or physical characteristics, are promising candidates in engineered materials. Because of their unique properties, including higher mechanical strength, lower density and cost, as well as longer life cycles, composites may be distinguished from their individual elements. Composites can be broadly classified into three major categories: (a) PMC, (b) MMC, and (c) CMC.

(a) Polymer matrix composites (PMC). Polymers, when combined with additives/fillers like carbon (CF) or glass fibers (GF) form PMC, which generally have improved thermal conductivity, mechanical, and tribological properties compared to the pure polymer.[84,85] PMCs exhibit interesting tribological properties, including their chemical stability, extreme temperature, and wear resistance.[11,84,86,87] Owing to these properties, PMCs are applied as lubricants in spacecrafts, automobile engines and under high vacuum conditions.[88–92] For example, poly (ether ether ketone) (PEEK) composites have been examined largely for their low CoFs and high wear resistance.[93–97] It has also been reported that the wear resistance of higher molecular weight PEEK was more than that of lower molecular weight PEEK.[93]

PTFE, a material possessing a high wear rate but with a low CoF,[98] when blended with PEEK forms a PMC displaying a blend of both, low CoF and low wear rates.[93] Lu and Friedrich, in their study, reported the value of the lowest CoF for a PEEK blend with 15% PTFE, as it formed a lubricating transfer film on the steel interface.[93] Furthermore, a reinforcement of CF with PEEK polymer decreased the wear CoF at high temperatures ($>$493 K).[94] At higher temperatures ($>$493 K), local surface heating of the contact area was observed, which led to a decrease in the specific shear stress and thus, also the CoF.[94] PEEK matrix reinforced with CF matrix exhibited a low CoF compared to aramid fiber matrix.[96] A higher enhancement in the reduction of abrasive wear was observed when PEEK was reinforced with CF compared to glass fiber.[97] SEM images of CF reinforced PEEK (CF-PEEK) have shown that the surface of CF-PEEK was smoother as compared to aramid fiber matrix.[95] The time required to remove a fiber from the surface was shorter in the case of aramid fiber matrix than CF-PEEK as the fiber had to be broken into many pieces before final removal could take place in CF-PEEK.[96] Additionally, a higher degree of crystallinity of PEEK reduced the abrasive and sliding wear of the matrix.[99]

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Owing to these advantages, it becomes imperative to determine a precise blend of PMCs in order to achieve enhanced tribological performance. However, in light of the large design space for exploration, the design of an optimal PMC for the desired applications continues to be a challenge. Therefore, in recent years, researchers have circumvented this issue through various data-driven techniques like ANN.[100] We list these papers used to predict the properties of PMCs in Table S3 (ESI†) and discuss them here.

Friedrich and coworkers were pioneers in successfully implementing the ANN technique for predicting the mechanical and wear properties of PMCs.[67,101–107] The early work of Jones *et al.* was followed by the work of Velten *et al.* as they modeled ANN for wear volume prediction in short fiber reinforced polymeric bearing when in contact with a steel ball. In Velten *et al.*'s ANN model, 10 input variables were utilized and pre-processing through PCA was applied for dimensionality reduction, and to identify the correlations between input variables.[108] Subsequently, Zhang, Friedrich, and Velten predicted the SWR and CoF using multi-layer feed-forward ANN on composites of polyamide reinforced by short fibers. Particularly, they reported the influence of learning rules including bayesian regularization, Powell–Beale conjugate gradient algorithm (CGB), BFGS quasi-Newton method, Adaptive learning rate (GDX), and Levenberg–Marquardt algorithm (LM) on the coefficient of determination (B). In addition, the influence of altering ANN architectures *i.e.*, 9-25-1, 9-50-1, 9-20-10-1, 9-15-10-5-1, and 9-12-8-5-5-1 and varying number of training data sets on B, which is formulated as shown in eqn (4), was also investigated.[109]

$$B = 1 - \frac{\sum_{i=1}^{M} [O(p^{(i)}) - O^{(i)}]^2}{\sum_{i=1}^{M} [O^{(i)} - O]^2} \quad (4)$$

where, $O(p^{(i)})$ represents the ith predicted wear characteristic, $O^{(i)}$ represents the ith measured value, and O represents the mean value of $O^{(i)}$.

A survey by Frangu and Ripa[110] revealed the applications of neural networks (NN) for modeling and predictions in continuous nonlinear approximation and classification data.[110] Later, Zhang *et al.*, who focused on the erosive wear of three polymers, *i.e.*, polyethylene (PE), polyurethane (PUR), and epoxy modified by hydrothermally decomposed polyurethane (EP-PUR), introduced the compelling potential of ANNs to study polymer composites.[67,101] Jiang *et al.* followed up this work by investigating the wear properties like SWR, CoF, and mechanical properties such as compressive strength and modulus, tensile strength (T_s) and flexural strength (F_s) in polyamide 4.6 (PA 4.6: synthesized with diaminobutane (C4 diamine) and adipic acid (C6 diacid)), and 6.6 (PA 6.6: synthesized with hexamethylenediamine (C6 diamine) and adipic acid (C6 diacid)) composites. They varied material compositions, including PA 4.6 matrix content with GF, PTFE filler and graphite filler, at different surrounding conditions like temperature, normal force, and sliding speed to train their ANN model.[102,104] In another study, Jiang *et al.* shifted their focus to polyphenylene sulfide (PPS) composites reinforced with SCFs and TiO_2 particles. An excellent agreement of their ANN model with their experimental validation confirmed that introducing fillers to PPS improved the wear resistance (4.0×10^{-7} mm^3 N^{-1} m^{-1}) for a specific composition (PPS with 15 vol% SCF and 5 vol% TiO_2). ANN-based models are also efficient at modeling nonlinear relationships between material compositions and testing conditions with wear characteristics, so estimating optimal compositions is simplified.[103] This study by Jiang *et al.* was further accelerated by Gyurova by incorporating the graphite and PTFE in PPS composites blended with SCF and TiO_2 fillers. A set of 90 data obtained from a POD experiment by varying loads and sliding velocities was used to train the ANN model. The inputs also included material composition and thermo-mechanical properties like tensile and compressive properties of materials to predict the SWR and CoF as outputs. To minimize the mean relative error and predict the CoF, ANNs were trained separately on gradient descent back-propagation algorithm with momentum and adaptive learning rate. Uniquely, the efficiency and performance of the ANNs were improved by removing irrelevant network nodes through a network optimization technique called the optimal brain surgeon (OBS) algorithm.[111–113] The predictions on pruned data showed a good agreement with experimental data while portraying better accuracy than the ANN model trained on unpruned data.[105] Further, in their second study, they suggested that the tribological characteristics predicted by ANNs were primarily altered by the material type, applied pressure, and sliding speed in the POD experiment. The composite data, predicted using their ANN models and experimental data were in fair agreement, resulting in the best wear resistance (*i.e.*, lowest SWR) for the composition of PPS with 15 vol% SCF and 8 vol% submicron TiO_2.[106] Effectively enough, the model was able to predict the SWR and CoF with reduced mean relative errors (0.55 for SWR and 0.1 for CoF) compared to their previous study.[104,105] Busse and Schlarb further improved this wear rate prediction efficiency (six times higher than their previous studies) by using the LM training algorithm with mean squared error regularization as a performance function.[114] The aforementioned study by Gyurova[106] also evaluated the effect of the size of the data set (of composites of PPS with TiO_2 and SCF) used to train the ANN model.[114]

Zhu *et al.* showed that an increase in the number of training data points can further improve the accuracy of ANN prediction. The tribological properties of the composites of PTFE reinforced by the CF and TiO_2 particle were predicted by an ANN model. 12 compositions of PTFE reinforced with CF (ranging 5–25 wt%), and TiO_2 particles (ranging from 3–15 wt%) were utilized. The varying sliding velocities, applied normal loads, and the material composition along with corresponding mechanical properties, were used as input to predict the wear volume loss and CoF. Interestingly, the least mean squared errors were shown in a multi-layered model (with an architecture of 7-[15-10-5]$_3$-1) by the scaled conjugate gradient (SCG) algorithm with tan-sigmoid transfer functions between input and hidden layers and linear

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transfer functions between hidden and output layers. For the case of moderate-level testing conditions, they concluded that the exhibited best wear resistance for PTFE (79 vol%) was due to a synergistic effect of CF (15 vol%) and TiO_2 (6 vol%), while the lowest CoF for PTFE/CF/TiO_2 content at 69/25/6%.[115]

A study on the CoF and weight loss of the composites of PEEK reinforced by using 30 wt% CF (PEEK-CF30) was performed by LiuJie *et al.*[116] Using a non-linear ANN model through BPNN; they determined that *pv* factor (a mechanical factor *i.e.* product of applied pressure and sliding speed) significantly influenced CoF whereas contact temperature affected the weight loss. Kranthi and Satapathy investigated epoxy resin (Araldite LY 556) composites reinforced with pine wood dust (PWD) using POD experiments.[117] Employing ANN on the data obtained from full-factorial DOE experiments ($L_9(3^4)$ orthogonal array), they constructed a 3-10-1 topology with sliding velocity, PWD content, and applied load as inputs. The experimental validation of ANN predictions was in good accordance with SWR errors $<8\%$. They also rank PWD content, sliding velocity, and normal load in the order of most influential parameters for SWR.[117] Following up, Rout and Satapathy investigated the epoxy composites blended with (5–20 wt%) rice husk (RH) for their SWR calculation using POD setup. They utilized an L16 orthogonal array determined from Taguchi DOE to obtain the experimental parameters. ANN model with 3-6-1 architecture, including RH content (wt%), sliding velocity and applied load as inputs for SWR as output was developed. In the 16 data points that were used, ANN predictions were in reasonable agreement with experiments since the errors were $\leq 9.64\%$.[118] Additionally, the work by Padhi and Satapathy illustrated the use of a BPNN on the experimental data obtained from Taguchi's experimental design on epoxy composites with SGF and blast furnaces slag (BFS). A data set of 16 parameters were run experimentally using a POD setup, and a SWR was determined. An ANN-trained model was used to estimate the SWR for composites with BFS (errors between 0.9% and 5.1%) and without BFS (errors between 2.5% and 6.9%).[119] Dai *et al.* designed novel antiwear additives by applying the BPNN-assisted quantitative structure tribo-ability relationship (QSTR) model.[120] This study investigated 90 structural descriptors, including octanol-water partition coefficient, 3D Jurs descriptors, and topological and quantum indices for 36 additives, to determine their WSD area under three loads.

Umar Nirmal investigated the frictional performance of polyester (T-BFRP) composite reinforced by treated betelnut fiber.[121] They trained an ANN model on 492 experimental sets of a block-on-disk experiment with normal load, sliding distance, and fiber orientation as inputs, used to predict the CoF. ANN trained with LM training function, and Logsig transfer function yielded the lowest errors compared to other training algorithms.[121] The work by Nasir *et al.* also highlighted the good accuracy of the LM training function in training ANN to predict the frictional performance of a polymeric composite of polyester resin reinforced by multi-layered GF. Here, a large dataset of 7389 parameters of experimental disk-on-flat tribometer setup was utilized with different fiber orientations, applied normal load, sliding speed, and test duration as the input. Interestingly, higher accuracy was shown by a single-layered model with a large number of neurons (90% in prediction) as compared to a multi-layered model with fewer neurons.[122] Parikh and Gohil investigated polyester composites reinforced with cotton fibers and fly ash to study composites' wear responses. Experiments were conducted on the POD setup to evaluate a devised composite. A Box Behnken DOE was utilized to determine the experimental operating parameters with sliding velocity, applied load, and sliding distance as three inputs. An ANN model was trained with a total of 7 inputs including above three operating parameters and four composites specifications (polyester, cotton fiber polyester composite, 3 wt% fly ash filled CFPC, and 5 wt% fly ash filled CFPC). An ANN architecture of 7-10-1 was generated to achieve excellent agreement of predictions with experiments with R^2 value of 0.90916.[123] Another prime example of determining an optimum composition with reduced SWR using ANN on the polyester (epoxy thermoset) composites generated by utilizing waste marble dust as the fillers was demonstrated by Nayak and Satapathy.[124] In their study, wear trials using POD tests were performed on 25 test parameters generated by varying sliding velocity, sliding distance, normal load, and marble dust content with the assistance of the Taguchi L_{25} orthogonal array.

Zakaulla *et al.* formulated and designed polycarbonate composites blended with graphene (GR) and B_4C particles through an injection molding process. They demonstrated the proficient use of ANN on the database collected through POD experiments. Employing material compositions (volume content of polycarbonate, GR, and B_4C) and operating conditions (applied load and sliding speed) as inputs, and SWR and CoF as outputs. The effect of the number of hidden layers and the number of neurons in hidden layers on the training ANN model was shown. A topology of 5-10-5-2 yielded the best results with CoD for SWR and CoF were 0.9375 and 0.9853 respectively. A polycarbonate composite with 10 vol% GR and 5 vol% B_4C produced the lowest CoF (0.13) and SWR (35 μm). They attribute their decrease in wear with increasing GR content to the interlocking with polycarbonate which aids in enhanced load transfer.[125] Yet another study exemplifies the successful use of ANN on polypropylene composite reinforced by blast furnace glass by Padhi and coworkers.[126] Both above studies used the Taguchi method to perform experiments on distinct arrays of parameters to generate input for the ANN model. Particularly, this study emphasizes the significant influence of sliding velocity and BFS filler content on the minimization of SWR.[126]

Kurt and Oduncuoglu magnificently illustrated that sliding speed and normal load significantly affected the wear volume losses. Their study comprised an ANN model trained on 125 datasets extracted from established literature on ultrahigh molecular weight polyethylene (UHMWPE) composites reinforced with zinc oxide (ZnO), zeolites, carbon nanotubes (CNT), CF, graphene oxide (GO), and wollastonite. A total of 11 inputs as shown in Fig. 4(a), including the weight% of each component, in addition to ZnO and zeolite sizes as well as

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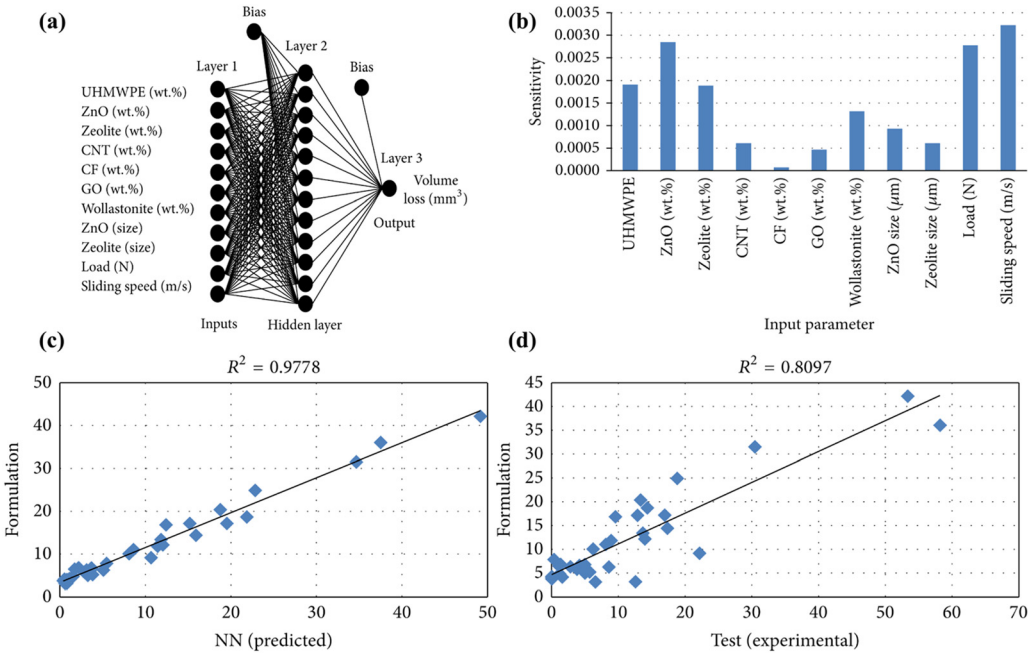

Fig. 4 (a) A schematic diagram representing ANN structure with an architecture of 11-12-1 is shown. (b) Sensitivity analysis of wear volume loss w.r.t. the 11 input parameters. A plot of formulated value of wear loss plotted against (c) ANN predicted volume loss values and (d) experimental results. Reproduced from ref. 127 with permission from Hindawi, copyright 2015.

sliding speeds and applied load, were used to train conventional feed-forward BPNN (with LM training function and logistic sigmoid transfer function) to predict the wear volume loss. A sensitivity analysis shown in Fig. 4(b) indicates that wear volume loss is significantly affected by the sliding speed, followed by the applied load, ZnO wt%, UHMWPE wt% and zeolite wt%. This study also involved volume loss calculation through a theoretical formulation, of which the volume loss is plotted against ANN predicted losses and experimental testing results as shown in Fig. 4(c) and (d) respectively.[127] Zhang *et al.* studied PEEK-based composite with SiC filler materials using ANN.[128] The model was successfully trained using applied load and sliding velocity as input variables to predict CoF and wear accurately. They observed that both outputs were significantly influenced by sliding conditions when the applied load was larger than 9N. On the other hand, for applied load <9N, they reported that the relationship between CoF and sliding velocity was parabolic.[128] Overall, Zhang *et al.* conclude their work by attributing the effect of testing conditions that affected the contact temperature in the experiments.

(b) Metal matrix composites. Metals, primarily aluminum, magnesium, and titanium, reinforced with other materials such as ceramic, other alloys, and organic compounds can be classified as MMCs.[129] MMCs are characterized by high specific strength, low density, controlled thermal expansion, high fatigue resistance, good corrosion resistance, thermal stability, enhanced electrical performance, and remarkable tribological behavior.[130] Therefore, they have been utilized in aerospace, automobile, electronics, petrochemical, and biomedical sectors.[131–134] The tribological performance of MMCs was successfully enhanced by the variation of the composition of fillers and reinforcement with materials such as alumina, SiC, and B_4C.[134–137] Moreover, an increase in their tribological performances was shown by reinforcement of these MMCs with CNT.[138–140] For example, a study by Zhou *et al.* showed a maximum decrease in the CoF at 20 wt% of CNT, which was attributed to increased surface fraction of CNTs, resulting in the reduced contact area between Al matrix and steel pin.[138] On the other hand, several studies show that excessive addition of nanoparticles led to their agglomeration on the surface of MMCs, which adversely affected the tribological properties of MMC.[139,140] Thus, the ability to *a priori* design MMCs with desired tribological performance under different conditions remains an open challenge. In principle, ANN models, which are capable of modeling and handling nonlinear, complex relationships can be used to address this challenge.[141] Indeed, several studies have exemplified the utilization of ANN for designing MMCs to minimize the tribological properties such as SWR, CoF, wear loss, *etc.*[142–149] Table S4 (ESI†) and text below summarizes the studies on MMCs that apply ANN approach.

A study by Saravanan *et al.* splendidly demonstrated the use of ANN on the prediction of wear behavior and CoF of composites of aluminum alloys reinforced with rice husk ash (RHA).[150] The POD experiments were performed on the parameters generated by an orthogonal array (L_{27}) based on the Taguchi technique. Specifically, the input parameters, applied load, sliding speed, RHA particle size, the weighted content of RHA and wear rate, and CoF as outputs were used to train a four-layered feed-forward BPNN. The LM training function yielded the best prediction results ($\sim$95% for both CoF and SWR). The morphological study showed that aluminum reinforced

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with RHA particles exhibited a lower wear rate due to their slightly plastic deformation.[150] Satyanarayana *et al.* successfully demonstrated the use of ANN to model the wear behavior of aluminum MMCs blended with red mud nanoparticles. In this study, POD experiments were performed on the devised composite of different compositions and deformation by varying applied load, and sliding velocity. A regression model and an ANN model were trained on these experimental results with a goal to predict the volumetric rate. Their results indicate that the composite with 10% red mud fraction and 30% deformation yielded minimum volumetric wear. Further, their ANN model (MAPE: 7.3% and R^2: 0.989) with 4-7-6-1 topology exhibited superior modeling performance compared to their regression model (MAPE: 12.96% and R^2: 0.9775) assumably due to its excellent ability to model non-linear relationship.[151]

In addition, a study by Genel *et al.* showed that the wear resistance of zinc–aluminum alloy could be significantly improved by alumina fiber reinforcement. An ANN model trained on sliding speed, applied loads, alumina fiber fraction, and orientation as input parameters were used to predict the wear performance of the composites. ANN model with the prediction of 94.2% and 99.4% for SWR and CoF, respectively, with a mean relative error (MRE) between experimental and predicted values of 2.4% and 0.43%, respectively, were reported.[152] Furthermore, Kumar *et al.* predicted the wear rate and CoF of aluminum-fly ash composites with 95% accuracy using an ANN model.[153] Particularly, a 4-6-2 architecture, with load, sliding speed, fly ash particle size, and their wt% as inputs were utilized with 98 training and 10 testing data sets. These studies further showed that the time and cost of the experimental process of designing an optimal material composition could be averted through the ANN models.[153]

Hayajneh *et al.* investigated the wear mass loss for composites of aluminum–copper alloy reinforced with SiC using ANN. Specifically, the weight content of copper and SiC in addition to the time of the POD test was used as an input for ANN to predict mass loss. A Neuralware's rule of thumb was used to determine the optimal number of neurons in the hidden layer as shown in eqn (5) to form the ANN architecture of 3-6-6-1 with the normalized squared error of 8.5×10^{-5}.

$$h = \frac{\text{Number of training cases}}{5(m+n)} \tag{5}$$

where, h, m, and n are the number of neurons in the hidden layer, output, and input layer, respectively. The sensitivity analysis suggested that cumulative time (Rel. sensitivity = 0.7796) was the dominating input parameter as compared to Cu (Rel. sensitivity = 0.2441) and SiC (Rel. sensitivity = 0.1805) weight contents.[154]

A356, another aluminum silicon alloy was investigated by Özyürek *et al.* to fabricate MMCs with SiC reinforcements by thixomoulding method to study their wear behavior.[155] A 64 experimental (POD) data sets with manufacturing temperature, applied load, sliding distance, and weight content of SiC as inputs and resulting weight loss, as an output, were used to train the ANN model. A topology of 4-5-3-2-1 was used along with the Fermi transfer function to achieve excellent agreement between experiments and predictions with R^2 value of 0.9985.[155] Another study by Shabani and Mazahery illustrated the use of a combination of ANN and finite element method (FEM) to model the wear properties of A356 alloy MMCs blended with B_4C. FEM was utilized to determine the temperature gradient and cooling rate as two input parameters for the ANN model in addition to the sliding distance of POD experiments, and boron nitride's particle size and volume content. The ANN model with 5-4-2 architecture and sigmoid activation function for their neurons was utilized to determine SWR and variation of porosity. An ANN model with MSE values of approximately 0.2 suggested that predictions were in excellent agreement with experimental results.[156] Rashed and Mahmoud were successful in modeling the wear behavior of A356 MMCs with SiC using ANN. Applied load, weight content and particle size of SiC, and the testing temperature were used as inputs, with 7 neurons in hidden layers to determine SWR as one output neuron was established to form 4-7-1 topology. The predictions of ANN were in good agreement with experimental observations with R-value of $\sim$0.99, and MRE $\sim$6%.[157]

Pramod *et al.* employed ANN to model the prediction behavior of aluminum alloy (Al7075) MMCs reinforced with aluminum oxide (Al_2O_3) particulates. The weight content of Al_2O_3, applied load, sliding distance, and density were used as inputs to predict SWR. The L_{27} orthogonal array obtained from Taguchi DOE to determine the experimental parameters. A topology of 4-5-7-1 was exercised to model this non-linear relationship with an average value of regression $R^2 = \sim 0.99$ and errors within 5%.[158] Veeresh Kumar *et al.* exemplified the superior tribological performance of aluminum 6061 alloy when it was reinforced with Al_2O_3. Their study demonstrated the use of BPNN to model these composites on the data obtained from POD experiments. The process/experimental design parameters were determined from the L_{27} orthogonal array of Taguchi DOE. Similar to the aforementioned paper, ANN model with 4-5-7-1 was constructed to determine wear tallness loss (output) with sliding distance, applied load, weight content of Al_2O_3, and density as inputs. A prediction error within 5% and correlation R^2 value of 0.999 suggested a good agreement of ANN predictions with experiments.[158]

Mehra *et al.* investigated the fabrication process of RZ-5 magnesium alloy MMCs blended with TiC to reduce their wear properties. The experiments showed that the introduction of TiC improved the hardness of the RZ5 alloy. Moreover, the ANN model with Broyden–Fletcher–Goldfarb–Shanno (BFGS) algorithm was trained on the experimental data with sliding distance and applied load as inputs to predict CoF. A topology of 2-2-1-1 was utilized to achieve the errors that were within 3.5% compared to their experimental results, which suggested the high-quality proficiency of NNs in the least possible time.[159]

Younesi *et al.* exercised application of ANN in designing nickel-free stainless-steel composites (NFSS) reinforced with hydroxyapatite (HA). The composites were characterized through POD experiments to estimate appropriate HA content in NFSS, applied load, and sliding distance for reduced wear loss. BPNN was employed with LM training algorithm, and with 3-5-5-1 topology and R^2-value of 0.999, while the prediction errors

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<12% for the volume loss. Owing to the higher accuracy of their ML model, they employed it as a surrogate for determining the volume loss of different composite for varying applied loads and sliding distances (0–1000 m).[160]

(c) Ceramic matrix composites. CMCs are ceramic fiber-reinforced materials that are formed by embedding ceramic fibers in a ceramic matrix and they possess high oxidation and corrosion resistance and are stable at elevated temperatures.[161] C/SiC matrix composites are widely used in vehicle braking systems.[162] Compared to C/C, composites of C/SiC have higher oxidation and wear resistance.[162] But the problem with CMCs is that they are brittle and possess low fracture resistance.[163] Hence research on CMCs is primarily focused on the enhancement of their toughness and ductility. CMCs are mostly applied while sliding against metal counterparts.[164] Reduction in the wear and increase in the tribological compatibility with the iron surface by reducing the adhesion of Si_3N_4 composites has been observed by the addition of SiC whiskers.[165,166] The maximum reduction of wear in Si_3N_4 composites has been observed at a composition of 30 wt% SiC whisker.[164] The addition of TiC particles to Al_2O_3 composite ceramic has been shown to enhance the tribological performance of Al_2O_3 composite when sliding on an iron surface.[166] Reinforcement of alumina matrix composite with GR also leads to a significant reduction in the CoF, with the lowest values observed at 0.3 wt% GR in Gr/Al composite.[167,168] The CoF for Gr/Al increases with an increase in the applied load and decreases with the sliding speed.[168]

In the context of this review article, the application of ANN in designing CMCs remains limited.[169,170] Malazdrewicz and Sadowski were the first to venture in predictions of wear for CMCs through ANN.[169] Specifically their study included curation of data for cementitious composites blended with high-calcium fly ash. Their ANN model constituted 9 input parameters including content of cement, fly ash, water, fine aggregate, coarse aggregate, superplasticizer, air entraining agent, age of concrete, and time of testing to predict the depth of wear as an output using a model with topology 9-18-1. This study successfully demonstrated the use of ANN in CMCs design by predicting wear with linear coefficient R^2 value or 0.998 and 0.997 for training and testing w.r.t. experimental results.[169] Another successful work has been reported by Bucholz *et al.* for design of CMCs.[170] Since their work includes the integration of other ML methods (DT and principal component analysis) with ANN, it is discussed in Section 3.7.

3.1.1 Analysis of variance (ANOVA) based ANN. ANOVA, initially introduced by Fischer, is a widely used statistical test to evaluate the differences among the means of population of two samples by measuring the variation within them.[171] ANOVA has been used to describe the complex relations among variables as well as to investigate the impact of independent variables on the dependent variables. Ongoing recent studies have reported the use of ANOVA to aid in determining the process variables, which are unique and have a significant impact on the results. Subsequently, the number of experiments have reduced and the data on which ML models are trained is efficiently pre-processed. The following sections guide through the use of ANOVA in generating data for ML models for diverse applications. Table S5 (ESI†) tabulates the research work that involves ANN approach assisted by ANOVA statistical analysis for all composite investigations.

(a) PMC. Siddhartha and Singh exercised ANN and ANOVA to formulate and fabricate polyester composites and their functionally graded materials (FGMs) reinforced with SGF. Taguchi DOE was employed to design the POD process parameters like applied load, sliding velocities, sliding distances, and the fiber content in composite. ANOVA results suggested that applied normal load (p = 34.54%) significantly affected both SWR and CoF, followed by the SCF content, and others. ANN model with 4-10-1 topology showed errors <14% for SWR and <10% for CoF. They concluded their study of PMC design with a finding of 6% SCF reinforced polyester exhibited lowest SWR. Moreover, SCFs show incisive effect on T_s and F_s on FGMs than their homogenous counterparts.[172]

Egala *et al.* attempted the work of the composites of epoxy resins blended with castor oil fibers (*Ricinus communis*).[173] Additionally, they also employed an ANOVA model to investigate the effect of these individual parameters on the output. ANOVA predicted that the applied load followed by fiber length and sliding distance were highly influential on gravimetric wear, CoF, and interfacial temperature. In this study, a regression model, single hidden layer ANN model and multiple hidden layer ANN models were developed and compared. These models were trained with input parameters *viz.* fiber length, normal applied load, and sliding distance of the POD experiments designed through a full-factorial approach to predict outputs. They reported that multiple hidden layer ANN performed best followed by single hidden layer ANN and regression analysis. Uniquely, this study utilized 73 different ANN models with varying algorithms, including cascade forward BPNN, feed-forward BPNN, and layer recurrent algorithm. Additionally, they conducted a study on varying hidden layers and number of neurons, and different transfer functions like Logsig and Purelin with constant LM training function.[174–176] Here, the predictions by cascades forward BPNN and feed-forward BPNN (errors ±5% and ±4.5%) were efficient and reliable compared to linear regression models (errors ±8%). They predicted epoxy reinforcement with 40% unidirectional short five mm-fiber length castor oil fiber improved wear by 65% to 70%, CoF by 31% to 40%, and interfacial temperature by 19% to 24%.[173]

(b) MMC. The study by Vettivel *et al.* exhibited the numerical modeling approach of ANOVA to predict the SWR and CoF with a 99% confidence level for the copper–tungsten (Cu–W) powder composites.[177] In their follow up study, Vettivel *et al.* employed ANN to predict the hardness, CoF, and SWR for Cu–W composite powder. A total of 4 inputs *i.e.* sliding distance, applied load, sintering temperature, and weight content of tungsten was employed to train the model. In particular, 10 different ANN architectures with LM training algorithms were designed.

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Specifically, an architecture 4-7-4-3 yielded best train-test-validation performance with a total MSE values <0.05, and R^2 values of 1, 0.99624, and 0.99046 for hardness, CoF, and SWR, respectively.[178] Furthermore, Leema *et al.* investigated the copper–tungsten composites using a radial basis function neural network (RBFNN) to predict hardness, CoF and SWR. An architecture of 4-140-3 was employed such that tungsten weight content, applied load, sliding distance, and sintering temperature (while preparing samples) were used as inputs. The accuracy in terms of *R*-value of $\sim$0.97 (SWR) and $\sim$0.99 (CoF) for training, while $\sim$0.976 and $\sim$0.965 in testing was achieved. This validated a good agreement of experiments with RBFNN predictions.[179] Moreover, Arif *et al.* exercised the powerful approach of feed-forward BPNN integrated with statistics (ANOVA) to investigate the tribological performance of aluminum hybrid composites reinforced with SiC and zirconia. It was determined that the most influential parameters were sliding speed, zirconia content, and applied load based on the full factorial analysis. However, the effect of each parameter in the exact amount of percentage *i.e.* sliding distance (79.47%), zirconia wt% (10.35%), and applied load (6.7%) on the wear loss performance of each composite was reported through ANOVA. The ANN model with the aforementioned three variables in addition to sliding speed was developed with a topology of 4-10-1, to accurately predict the wear loss as compared to experiments.[180]

Thankachan *et al.* demonstrated the use of ANOVA combined with BPNN to predict the tribological behavior of copper surface strengthened by a mixture of aluminum nitride and boron nitride particles. The experimental set of parameters was designed by L_{27} Taguchi's orthogonal array with varying volumetric fractions of particles, sliding speed, applied load, and sliding distances as the input parameters.[181] Stojanovic *et al.* investigated the aluminum hybrid composites mixed with A356 alloy, which was further reinforced with SiC and graphite. In this study, the L_{27} orthogonal array of experimental parameters was generated using the Taguchi method to design experiments. ANOVA technique was performed to determine that GR composites with 3 wt% exhibited the lowest wear and friction. Additionally, an ANN model was trained with 3-20-30-2 architecture trained on LM function and logarithmic sigmoid and linear transfer functions. The comparison of predictions by ANN with ANOVA illustrated that ML algorithms perform precisely better than statistical methods. An ANN model with one hidden layer of 7 neurons and LM training function successfully predicted the optimized SWR with higher accuracy compared to the referenced regression model.[182]

Agarwal *et al.* investigated the effect of powder-chip reinforcement for LM6 aluminum alloy to reduce SWRs using BPNN. While maintaining the sliding speed at 300 rpm at an applied load of 15 N, only sliding distances (varied from 125 m to 750 m) and reinforcement content (10 to 25%) were used as input for training the ANN model. With an architecture of 2-5-1, the total mean squared error (MSE) of 1.11% was reported. In addition, ANOVA was used to determine the interaction effects between the input parameters. Particularly, reinforcement incorporation (adjusted sum of squares (Adj SS) = 11.225) showed a dominant effect on the wear rate compared to sliding distance (Adj SS = 8.475).[183] Ritapure and Kharde developed an ANN model to examine and predict the SWR for Al–25Zn alloy based MMCs blended with SiC. Taguchi's L_{16} orthogonal array was determined and accordingly experiments were performed on POD setup. With sliding speed, temperature, applied load and filler (SiC) content as input, ANOVA, regression and ANN models were developed to calculate SWR. Through ANOVA, the dominance of testing temperature was evident followed by applied load, SiC content and sliding velocity. An ANN model with $R^2 = \sim 0.99$ outperformed the regression model with $R^2 = \sim 0.98$ by a fine margin, while both models showed reasonable agreement with experimental validation. Their results suggested that highest wear resistance and hardness was observed for 15 wt% SiC reinforcement with an increase in its T_s.[184]

Prakash *et al.* investigated the copper MMCs reinforced with MWCNTs with POD experiments. The obtained results were analyzed through statistical (ANOVA) and ML (ANN) algorithms to determine the wear loss. Taguchi's DOE was used to obtain an L_{16} orthogonal array to optimize the experimental parameters such as volume fraction of MWCNTs, applied load and sliding distance. In the ANOVA, MWCNT content (76.48%) was found to be the most influential factor, followed by the applied load (12.18%) and the sliding distance (9.91%). The ANN model was constructed with these 3 inputs and 1 hidden layer with 7 neurons and 1 output *i.e.* wear loss. This model with R^2 value of 99.5% was in excellent agreement with experiments and exhibited superior predictability than ANOVA predictions.[185]

Kavimani and Prakash employed ANN and ANOVA to study and analyze the magnesium (AZ31 alloy) MMCs with varying reinforcements of reduced graphene oxide (r-GO). Four input parameters, namely, applied load, r-GO weight content, sliding distance, and sliding velocity were determined to be influential in training of the ANN model. Using the Taguchi method of DOE, an L_{27} orthogonal array with three levels of variation of input parameters was determined. The mean-effective plot describing the signal-to-noise ratio of each individual parameter is shown Fig. 5(a). Their ANN model development involved studying the variation of the number of neurons in the hidden layer. The corresponding MAE results are shown in Fig. 5(b). An architecture of 4-7-1 yielded 98.4% accuracy (R^2 = 0.984) for the prediction of SWR as shown in Fig. 5(c). ANOVA results suggested that applied load (38.85%) is the most influential parameter determining MMC's SWR, while sliding distance was the least (12.33%).[186] In their follow-up study, Kavimani *et al.* investigated the wear and friction behavior of Mg MMC reinforced with r-GO now doped with SiC. Similar to their previous study, the L_{27} orthogonal array for varying the applied load, sliding distance, sliding speed, and the weight contents of r-GO and SiC were determined through the Taguchi DOE method. The ANN model with an R^2-value of 0.998 was shown for an architecture 5-8-1, while ANOVA predicted that the weight content of r-GO and applied load were the most influential parameters determining the SWR.[187]

3.1.2 ML/optimization assisted ANN and ANN assisted optimization. An attribute-property relation of any multivariate

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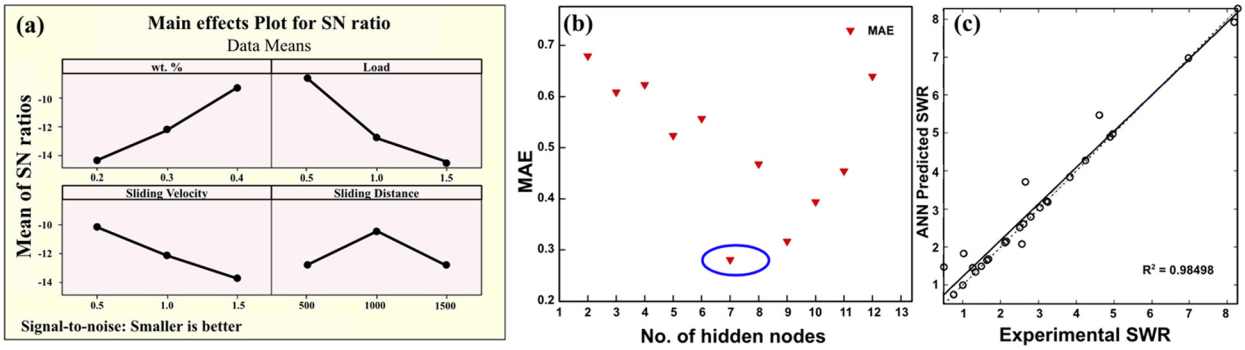

Fig. 5 (a) The mean-effective plots show the signal-to-noise ratio of each individual parameter. (b) The variation of MAE with the changing number of neurons in the hidden layer. Highlighted point with 7 neurons shows the lowest MAE error. (c) The results for the predictions of ANN validated against experiments for wear rate. Reproduced from ref. 186 with permission from Elsevier, copyright 2017.

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system of ANN can be developed, however at the cost of appropriate choice of hyperparameters. Studies have developed some interesting strategies to tailor these multiple variables, but may be focused on that specific dataset. To that rescue, some studies have incorporated optimization algorithms like monte-carlo (MC),[188] improved bat algorithm (IBA)[189] or other ML techniques to develop ANN models. These optimization techniques have enabled researchers to overcome drawbacks of slower convergence and compromised accuracy in development of traditional BPNN. In the case of ANN assisted optimization, an ANN model is used as a surrogate where optimization algorithms use ANN as an objective function. These include evolution algorithms like non-sorting genetic algorithm (NSGA-II)[190] and genetic algorithm (GA)[191–193] to optimize the input variables. As a result, multi-objective optimization can be conducted with a high degree of efficiency. Table S6 (ESI†) tabulates applications of ANN combined with other ML/optimization algorithms to investigate tribological properties of composite materials.

(i) Monte-Carlo-based ANN. In Monte Carlo simulations, stochastic processes are modeled and their outcomes are estimated using probabilistic numerical techniques.[194] In regards to any mathematical problem, repeated sampling of the parameter space can enable equilibrium to be reached faster than analytical deterministic methods, depending on the complexity of the problem. Monte-Carlo's theory has exhibited proficiency in modeling a variety of real-world probabilistic processes.[194] Compared to this traditional deterministic method, a probabilistic approach of the Monte-Carlo (MC) method, which can generate random scenarios (variables), may help in developing/modeling ANN faster with efficient computational usage.

A few studies have demonstrated the successful use of MC in sensitivity analysis, uncertainty quantification, and so on.[195,196] An appropriate choice of hyperparameters and as such determining the weights of neurons remains challenging. Therefore, MC-ANN, introduced by Li *et al.* exercises the MC approach to estimate the weights of each neuron in a probabilistic manner.[188] A faster and more accurate MC-ANN aids in better non-linear mapping ability and improved fitting effect of samples. The comparison of the workflow of MC-ANN that is featured in the work of Li *et al.* is shown in Fig. 6(a) and (b). They trained and compared MC-based ANN (MC-ANN) and BPNN, exhibiting a better accuracy of MC-ANN (RMSE 0.97 and 0.007) compared to BPNN (RMSE 2.08 and 0.019) for SWR and CoF, respectively as shown in Fig. 6(c) and (d). This study investigated the tribological behavior of PTFE resin composites reinforced with aramid pulp, mica, copper (Cu), nano-SiO_2, and potassium titanate whisker (PTW). 18 different compositions were formulated using orthogonal table L_{18} (3^7), and the experimental data conducted in triplicate on a quasi-static test rig were used to train the ANN model. The gray relational analysis (GRA) was employed to optimize formulation design and determine weight factors and non-linear dependency of the ingredients. In the context of variation and volatility of the data, MC-ANN performs better than conventional ANN because it uses repeated random sampling and a variety of transfer functions like sigmoid, polynomial, tanh, and Gauss functions.[188]

(ii) Improved bat algorithm (IBA). A meta-heuristic global optimization algorithm, improved bat algorithm (IBA) is based on the echolocation characteristics of the bat.[197,198] With the improved exploration and local search capability, IBA exhibits superior performance compared to the original bat algorithm (BA). In search of prey, bats (explorers) fly randomly with certain velocity and emitting (adjustable) frequency, depending on the distance from the target.

A novel work by Gangwar and Pathak integrating an IBA optimization with ANN that overwhelms the challenges of the training process of complex and non-linear ANN models.[189] This work exemplifies the efficient and effective training of ANN models to evaluate and predict the wear characteristics of ZA-27 alloy reinforced with marble dust particles (MDp). Taguchi design of the experiment was utilized to generate an L_{25} orthogonal array for unique parameters (applied normal load, sliding distance, velocity, marble dust composition, *etc.*) for POD setup. Compared to other training algorithms like backpropagation, genetic algorithms, particle swarm optimization, and so on, the flexibility and stability in the tuning of IBA

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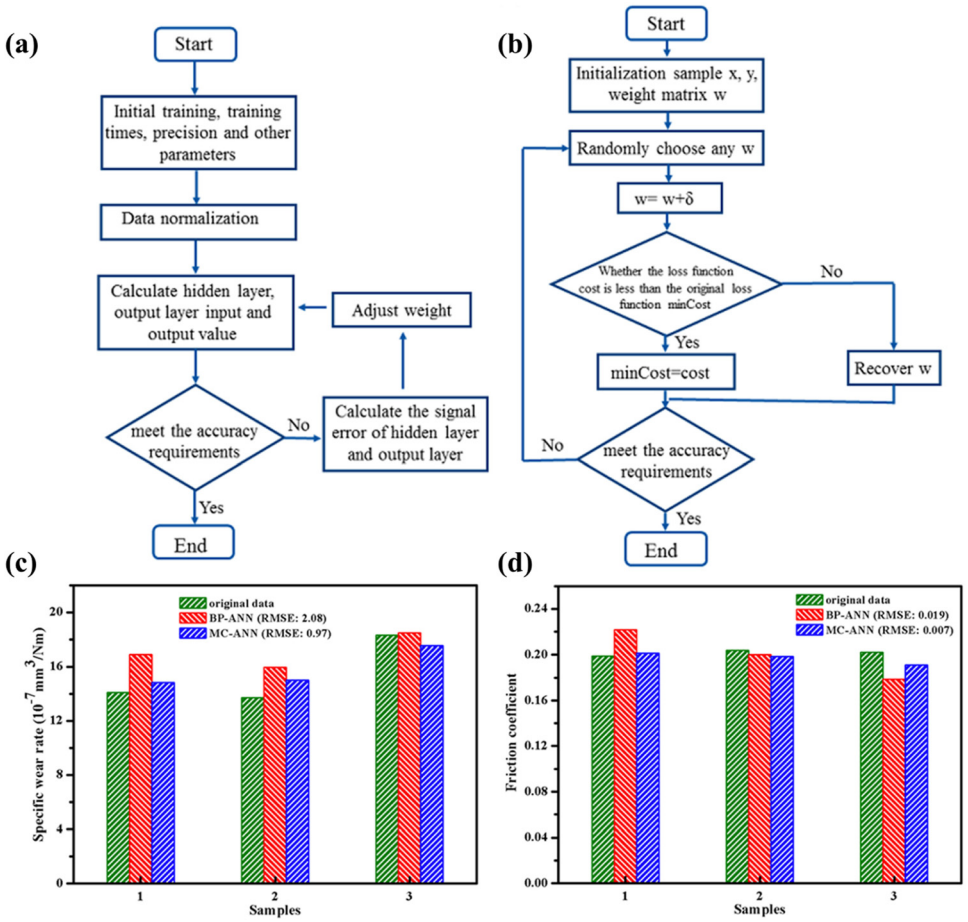

Fig. 6 The schematic representation of the workflow of (a) BPNN and (b) MC-ANN. The results for (c) SWR and (d) CoF are also shown in bar graphs. Reproduced from ref. 188 with permission from Wiley Online Library, copyright 2019.

allow us to attain convergence faster by introducing a new velocity, position search equation, and Sugeno inertia weights.[199,200] As a result, the local optima stagnation was overcome, and prediction accuracy for SWR of 97% with a mean squared error of 0.26 was obtained for this study. Employing optimization-assisted ANN, one can save the tedious task of brute-force training a complex NN model, and accelerate the process of optimization and prediction.[189]

(iii) Non-dominated sorting genetic algorithm (NSGA-II). One of the most popular multi-objective optimization evolutionary algorithms, NSGA-II, exhibits three main features: (i) a fast nondominated sorting process, (ii) a fast crowded distance estimation procedure, and (iii) a simple crowded comparison procedure.[201,202] As a part of multi-objective optimization (MoGA), NSGA-II has shown its reliability in optimizing machining process parameters. Compared to the Pareto-archived evolution strategy (PAES) and the Strength Pareto EA (SPEA), NSGA-II is able to maintain a better spread of solutions and convergence on the Pareto-optimal front.

A recent work by Vinoth and Datta also exemplifies the usage of ANN to predict the mechanical properties of UHMWPE composites reinforced with CNT and GR.[190] ANN model was trained on previously reported 153 experimental data with varying composition within composites, particle size, and mechanical properties as input (7 no.). Here, two ANN models were trained to determine Young's modulus (Y) and T_s, with 3 and 5 hidden layers, respectively. A feed-forward ANN with scaled conjugate gradient backpropagation with hyperbolic tangent transfer function assisted in achieving correlation coefficients of 0.93 and 0.97 for Y and T_s, respectively. A multi-objective function to attain optimum values of Y and T_s were executed by employing a non-dominated sorting genetic algorithm (NSGA) based on Pareto-optimality theory.[201,203] The optimized composites were further experimentally subjected to tribological and mechanical characterization. This process successfully demonstrated the use of ML integrated with optimization to improve the properties, specifically the excellent wear rate of the predicted composites compared to the literature available 153 datasets.[190]

(iv) Genetic algorithm (GA). In the theory of Darwin's natural selection, GAs are iterative processes that evaluate the fit between data over multiple generations in an iterative manner.[204] There have been successful applications of GAs for material development in recent years, including metal–organic frameworks,

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metals, and their oxides, and composites, to optimize large and complex design spaces to develop materials that are tailored for specific applications.[205] They are developed by following a set of rational design principles that produce material structures that can be synthesized for various applications.[206–208]

Given the large design space spanning through varying content of different vegetable oils and nano friction modifiers (FMs), Bhaumik *et al.* successfully employed GA assisted by ANN.[191] They successfully trained an ANN model with 80 and 120 data available on four-ball tester and POD experiments, respectively. Their study aimed to design an optimal blend of different vegetable oils (*viz.* coconut oil, castor oil, and palm oil) with nano FMs, including MWCNT and GR. Two three-layered ANN models were trained, each for POD and four-ball tester experiments, with CoF as the output parameter. Particularly, the data on the amounts of three vegetable oils, dimensions, and amounts of nano FMs, in addition to their respective experimental setup parameters, were used. Further, these two ANN models integrated with a GA were operated to optimize the output constraint CoF and design two lubricants: Lube A: 40% castor oil, 40% palm oil, and 20% coconut oil with 0.7% MWCNT and 0% GR and Lube B: 33.3% castor oil, 33.3% palm oil and 33.3% coconut oil with 1% MWCNT and 1% GR for four-ball tester and POD setup, respectively. Contrary to the work by Li *et al.* where an MC optimization algorithm was used to tune the weights of neurons, here, the ANN surrogate model is used as an objective function to optimize input variables.[188] This study showed a fair agreement of ANN predictions with their experimental results. This study was further extended in developing a quintessential combination of multiple FMs including GR, graphite, MWCNT, and ZnO nanoparticles blended with castor oil.[192] The data generated from POD experiments performed on lubricants designed by varying above components were used to train the ANN model. The GA optimization with ANN models as an objective function was employed to successfully predict a novel lubricant that comprised 0.66 wt% each of graphite, MWCNTs, and ZnO in castor oil. This lubricant yielded a reduction of 50% and 87% in the CoF and WSD, respectively. Their study highlights the contributions of different FMs on CoF, as illustrated in Fig. 7(a), particularly the surface plots (Fig. 7(b)) for the CoF shed the light on varying concentrations of FMs. Moreover, the lubrication mechanism emphasizes the use of FMs in reducing friction as shown in Fig. 7(c).[192]

Mahapatra *et al.* developed polyester composites reinforced with e-glass fiber and ceramic particulates including cement by-pass dust (CBPD), Al_2O_3, and SiC. An L_{27} orthogonal array from Taguchi DOE was utilized to determine the initial input parameters, namely, impact velocity, filler content, stand-off distance, impingement angle and erodent size in an air jet type erosion test rig. An architecture of 5-12-1 yielded errors less than 14% for the ANN predictions compared to experimental results. In addition, an ANOVA indicated that CBPD exhibited superior filler properties compared to alumina and SiC fillers. Subsequently, GA was employed to determine and report the optimal test factors for all three fillers.[193]

Table S7 (ESI†) tabulates applications of other ML algorithms to investigate the process variables or tribological behavior. These other ML algorithms include RNN, PCA, ART-2 ANN, ELM, ANFIS, DT, RF, SVM, regression, KNN, GBM, and so on. Detailed information on these models, including their development and advantages, follows the table.

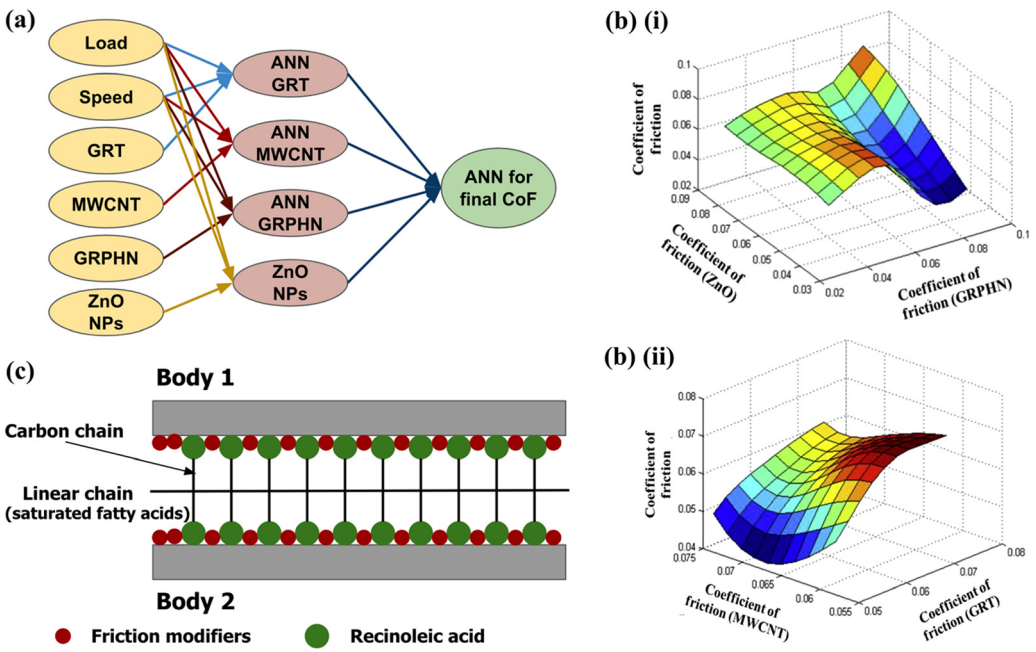

Fig. 7 (a) The schematic representation of ANN used in this study. (b) The surface plots for the variation of CoF with varying (i) ZnO and GR, (ii) MWCNT and graphite content. (c) Representation of the nano-fillers aiding the lubrication regime. Reproduced from ref. 192 with permission from Elsevier, copyright 2019.

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3.2 Recurrent NN (RNN) and principal component analysis (PCA) based ANN

PCA is a dimensionality reduction technique, transforming such a large set of variables into a total lower number of dimensions, representing the information from a larger set.[209,210] A study by Kolodziejczyk delineated the dynamical frictional behavior using the model on wear resulting from dry fretting.[70] Specifically they trained two ANN models *i.e.* static ANN and dynamic RNN for solving static and dynamic problems, respectively. (i) Static ANN: Firstly, their study utilized the PCA to exhibit the dimensional reductionality employed in high dimensional and complex models, which could further be used in training an ANN model. Taking 6 input factors, PCA successfully identified only four parameters, *viz.* number of cycles (NoC), the amplitude of displacement, pressure, and roughness, had the least correlation factor to be utilized for ANN model training. Therefore, a static ANN model with 4-3-1 architecture was trained on tansig transfer functions for input and hidden layers. In contrast, the purelin transfer function was applied for the output layer to achieve a 1.8% mean relative error. Comparing the results of the ANN model with their multiple regression analyses (MRA), they concluded that ANN successfully mapped the non-linear region of the data – particularly, the physical interpretation of input mechanical properties and their response in their ANN model. (ii) Dynamic RNN: The preprocessing of this real-time data involved normalization and bisection, and therefore, one extra input *i.e.* CoF was added to train the model. An algorithm similar to static ANN was used to train RNN with an architecture of 5-12-1. Despite 95.9% accuracy, the authors concluded this work by reporting more data was required for better modeling.[70]

3.3 Adaptive resonance theory (ART-2) based neural network and BPNN

An adaptive resonance model is an unsupervised learning approach that mimics the brain's ability to recognize patterns in environments that are constantly changing.[211] This algorithm relies on a recurrence (feedback) approach in order to regulate learning ability, so that the neurons' weights converge faster. ART-2 model not only solves the problem of pattern and situation recognition but also can be used to study and predict the structure and values of time series.[212] An ART-2 model was employed by Subrahmanyam and Sujatha, which was further compared with conventional multilayered feed-forward ANN with error backpropagation (EBP).[213] These ML models were trained for the diagnosis/detection of localized defects in ball bearings. The experimental data of vibration acceleration signals for normal bearing and two different defective bearings was used to train models. Compared to BPNN, the learning of the ART-2 algorithm was found to be about 100 times faster, with a 100% reliability in detection of faulty bearing in comparison to the normal bearing. However, ART-2 was inefficient in distinguishing localized defects in different ball bearing states. Moreover, BPNN was capable of diagnosing localized defects with 95% success rate. However, while BPNN showed 100% success in identifying defective ball bearings, it exhibited a slower learning rate.[213]

3.4 Extreme learning machine (ELM)

ELM is an ML model with a single hidden feedforward NN.[214] However, unlike gradient-based back propagation, it uses Moore–Penrose generalized inverse method to estimate the output weights. Consequently, they converge faster than conventional methods and produce promising results.[215] Mujtaba *et al.* recently utilized ELM as well as integrated the Cuckoo search optimization process with response surface methodology (RSM) (Box–Behnken DOE).[216] The tribological behavior of biodiesel produced from optimizing process variables of ultrasound-assisted transesterification of palm-sesame oil was examined. The process variables such as time, catalyst amount, methanol to oil ratio, and duty cycle were optimized to improve the cold flow characteristics and average CoF of produced biodiesel. This study also highlighted that CoF prediction using ELM model is computationally less intensive and more accurate as compared to DOE model. The predicted average CoF for P50S50 biodiesel was lower than palm biodiesel and B10 commercial diesel by 2.29% and 12.37%, respectively.

3.5 Adaptive neuro fuzzy inference system (ANFIS)

A hybrid predictive model that uses both NNs and Takagi-Sugeno fuzzy inference system[217] logic to provide mapping relationships between input and output is called ANFIS. This approach allows us to train the non-linear models with rapid learning and adaptive capability.[218] Babajanzade Roshan *et al.* exercised ANFIS modeling and optimization approach to maximize mechanical properties of friction stir welding (FSW).[219] ANFIS model with generalized bell type of membership function was developed to map relationships between inputs (welding speed, pin profile and rotary speed of tool) and outputs (T_s, yield strength, and hardness of welded joints). By the virtue of both single response and multi-response problems, the highest mechanical properties were observed at a welding speed of 1.75 mm s^{-1}, and square pin tool with the rotary speed of 1400 rotations per minute (RPM), axial force of 7.5 kN, which were further validated in their experiments. They mentioned that the axial force plays a critical role in determining CoF due to the frictional heat generation between the tool shoulder and plate surface. A subsequent increase in axial force from 5 kN to 7.5 kN saw a rise in hardness due to improved joint efficiency and increased tensile properties, which saw defects and tunnels if the force was further increased. Moreover, the effects of rotary speed and welding speed emphasize their significant role due to heat generation, cooling rates, and/or welding efficiency.[219]

Dewan *et al.* investigated the effects of process variables including, spindle speed, plunge force, and welding speed for the FSW process through ANFIS and ANN.[218] A small data set of 73 welds were used to train models to predict the ultimate tensile strength (UTS) of FSW joints. Overall, 1200 ANFIS models were generated by varying the number and types of membership functions (MFs), a combination of above mentioned three input variables and empirical force index (EFI)

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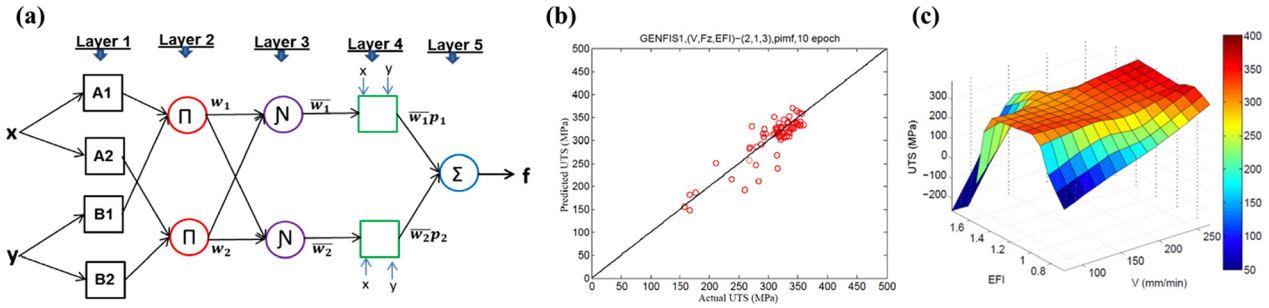

Fig. 8 (a) The schematic representation of ANFIS used in this study. (b) Comparison of ANFIS predictions of UTS w.r.t. experimental values. (c) The surface plots for the variation of UTS with varying (i) EFI, and (ii) welding speed. Reproduced from ref. 220 with permission from Elsevier, copyright 2016.

derived from three process parameters. A schematic of the ANFIS structure with 5 layers is shown in Fig. 8(a), where the number of nodes in the input layer is determined by the number of inputs and membership functions, while hidden layers are given by the number of fuzzy rules.[218] The prediction based on the ANFIS model developed on three input variables (V, F_z, and EFI) compared to experimental UTS is plotted in Fig. 8(b). In addition, the surface plot for predicted UTS values from the ANFIS model with two input variables V and EFI is presented in Fig. 8(c). In general, their study highlighted that ANFIS models performed better than ANN due to their lower prediction errors. Their analysis indicated a strong relationship between EFI and UTS, as well as a non-linear correlation of EFI with the other three inputs N, V, and F_z. Their ANFIS model is proficient to estimate appropriate weld process parameters to achieve desired joint strength.[220]

3.6 Decision trees (DT)

DT is a supervised learning algorithm used for classification or regression, based on the simple decision control rules (decision nodes) and predicted actions (branches).[221] In addition to the simplicity in understanding and interpretability, DTs require minimal preprocessing irrespective of hard or soft data. Bucholz *et al.* have illustrated the use of DTs in designing ceramic pairings by using data from dry sliding POD experiments.[170] A total of 24 ceramic samples spanning through 15 variables were generated using POD tribometer experiments. However, a multivariate problem necessitates a dimensionality reduction step, which would result in efficient recursive partitioning through DT. Initial exploration through PCA suggested that the first two principal components (PCs) captured ~65.8% variation, which could be sufficient for higher information gain. Fig. 9(a) shows an evident grouping among oxides, chalcogenides, halides, and pnictides, and Fig. 9(b) illustrates the corresponding property relation. PCA suggested that the key material properties such as cation electronegativity, melting temperature, and Madelung constant were critical in determining the data-driven friction model. A regressive DT was developed with these attributes as well as R_{ij} distance, cation radius, and charge, as the decision nodes as

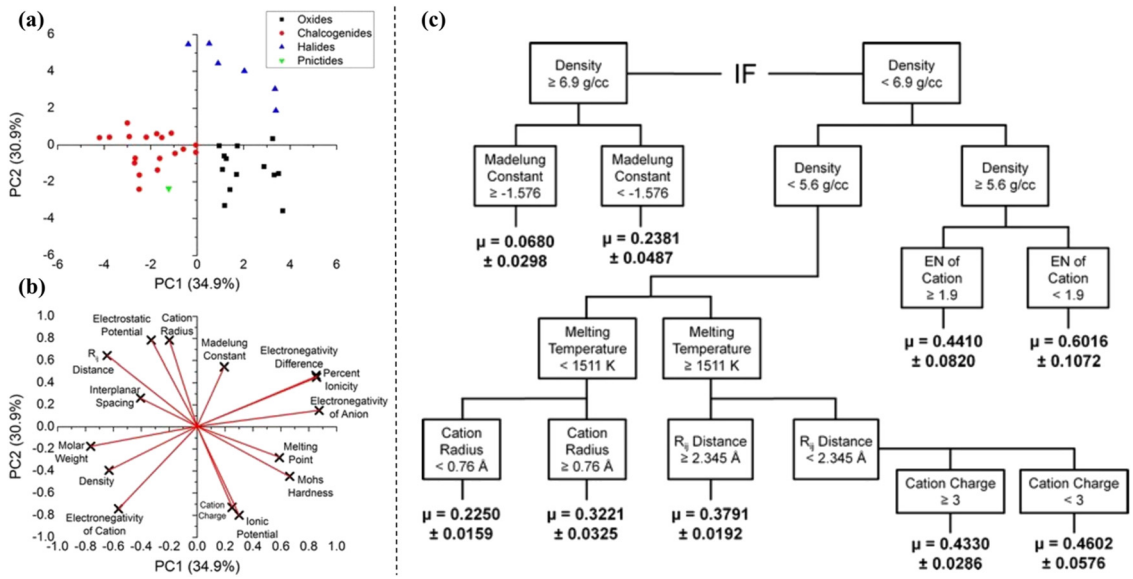

Fig. 9 (a and b) Representation of PCA analysis for grouping oxides, chalcogenides, halides, and pnictides and their respective property relationships. (c) The schematic representation of the DT constructed on the basis of PCA results. Reproduced from ref. 170 with permission from Springer Nature, copyright 2012.

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shown in Fig. 9(c). The trained DT model with R^2 accuracy of $\sim$0.89 in the prediction of CoF, was in excellent agreement with the experimental validation.[170]

3.7 Random forests (RF)

A RF is an ensemble learned technique constructed from many independent DT.[221] Specifically, the RF model is trained *via* bagging and bootstrap aggregating techniques to overcome DT's missing data and overfitting problems. Prost *et al.* utilized the RF classifier to predict the states of operation for tribological sliding experiments in oscillating and translatory motion.[53] The tedious and time-consuming task of labeling states of operating conditions was overcome by a semi-automated process based on dimensionality reduction, PCA, and clustering algorithms, *k*-means. This study emphasized on the flexibility of the labeling approach since it is a critical step and may require the expert knowledge of tribologists. Particularly, with four operating states (steady-1, steady-2, precritical, and critical), their RF model with a training accuracy of $\sim$0.94 on the high-resolution force signals, was validated against the labeled dataset of another experiment.[53]

3.8 Support vector machines (SVM)

Support vector machines are based on statistical learning.[222] One of the most robust prediction methods, SVM is efficient for non-linear classification specifically for high-dimensional feature space. Yin *et al.* investigated the acoustic emissions (AE) from the experiments conducted under varying operating conditions of the gas face seal test rig.[223] SVM regression model was trained and validated through leave-one-out (LOO) cross-validation on the data obtained from experiments to predict the eccentric load on the stator of the seal. This study primarily highlights the use of vectorization and SVR to estimate the load in gas face seal test rig experiments.[223]

The work conducted by Das *et al.* sheds light on the internal defect identification in the FSW process using real-time torque signals.[224] Discrete wavelet transforms and statistical features including dispersion, asymmetry, and excess were computed to analyze these experimentally obtained signals. Moreover, general regression models, ANN, and support vector regression (SVR) models were trained on these signals to predict the UTS. Particularly, the SVR model's prediction performance with the error of 0.5% was better than even ANN with 3-5-1 architecture with the error of 3.1% and regression models with 13.6%.[224]

3.9 Multiple ML models

Despite the extensive efforts, the relevance of different ML for appropriate applications has not been fully explored. In some cases, black-box ML algorithms have proven useful in identifying correlations in data and developing characterization models with a minimal cost and effort. In such manner, Perĉic *et al.* employed various ML and AI techniques to model and predict the dependencies of synthesizing process parameters on nanoscale friction of Al_2O_3, TiO_2, molybdenum disulphide (MoS_2), and aluminum (Al) thin films.[225] The lateral force microscopy (LFM) within a centroidal Voronoi tessellation (CVT) process included normal forces, sliding velocities, and temperature as input parameters. This study employed ML algorithms like MLP ANN, random DT and RF, SVR, age-layered population structure, grammatical evolution, and symbolic regression multi-gene programming (SRMG). The numerical evaluation of prediction performances of these models through RMSE, MAE, and R^2-value suggested that SRGM model exhibited highest accuracy (R^2-value: 0.72–0.91). By using this approach, simple functional descriptions influencing nanoscale friction for variable parameters in study were derived.[225]

Moreover, tribological operators like a brake or clutch which are an essential safety component of any automobile regardless of the conditions, modeling the wear phenomena and CoF remains a time-consuming and challenging task. Data driven approaches to model brake linens can be exercised through a number of ML approaches. To that extent, Timur and Aydin evaluated the CoF of brakes through the application of 7 different ML regression models.[226] This includes linear, SVM, Gaussian process, pace, simple linear, least median square, and isotonic on 1050 experimental data points, with a 10-fold-cross validation. The models were trained on data that was generated by varying the speed, pressure, and heat, which had a significant impact on the CoF. Out of 7 different models, isotonic regression showed lowest RMSE of 0.0014 and highest correlation coefficient (0.99). An isotonic regression model, which is suitable in multidimensional scaling problems, can be described as a flexible linear model that can be fitted in order to predict data in series, which resulted in the best performance by this model. Moreover, in general, the models showed the RMSE values <0.01 and correlation coefficient with test experiments of >0.99.[226]

A recent study by Hasan *et al.* successfully incorporated and compared different ML algorithms in the tribological behavior of aluminum-based alloys and aluminum–graphite MMCs, including ANN, RF, SVM, *k*-nearest neighbors (KNN), and gradient boosting machines (GBM).[227,228] The experimental data obtained from the literature, including seven material variables (hardness, T_s, yield strength, ductility, heat treatment, processing procedure, and SiC content) and three tribological test variables (sliding distance, sliding velocity, and applied load from POD experiments) was used to train these supervised ML models to predict the CoF and SWR. They found that the RF model performed better compared to other models in predicting wear behavior, which can be traced to its bagging mechanism. The RF algorithm can handle high levels of variability and fluctuations in the dataset. GBM and KNN, however, showed excellent prediction performance for aluminum base alloys and Al/Gr MMCs, respectively.[227,228]

In their critical review, Marian *et al.* highlighted that numerical design and optimization of surface micro-texturing in EHL lubricated contacts to control friction and wear.[229] In their subsequent study, Marian *et al.* investigated EHL contacts' fluid film parameters by employing ML and AI approaches, specifically, SVM, GPR, and ANN. Their work demonstrated better flexibility and higher accuracy in the predicting film's thickness compared to analytical counterparts of EHL simulations.

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The data available from finite-element method (FEM) simulations and Latin hypercube sampling, comprising 12 input parameters including sliding surfaces mechanical and elastic properties, applied load, sliding velocities, and lubricant properties, with minimum and central lubricant gap as output were used to train the ML model. An ANN architecture of 12-12-12-2 was implemented to achieve an accuracy of 1.0. In addition, the study of effect of variation of number of neurons, hidden layers, different activation functions, and varying number of input data was also conducted. Similar to ANN, SVM (R^2 = 0.997) and GPR (R^2 = 1.0) showed excellent prediction accuracy. Moreover, the comparison of computational time for ANN prediction was ~26 times faster than FEM-based simulation.[230]

4. Molecular simulations in tribology

To complement the aforementioned experimental methods that provide macroscopic information, molecular simulations providing insights on tribological processes at the nanoscale, have emerged as a powerful tool. This study of tribological systems, termed as nanotribology, is associated with the study of micro- to nano-scale friction and wear phenomena such as adhesion, scratch, friction, and wear rate properties at the atomic level, as well as the interfacial properties between two surfaces.[23,231,232] While the experimental exploration of nanotribology necessitates the use of costly specialized equipment and is subject to high probabilities of error, computer simulations like MD simulations not only lower the expense of experimentation but also allow for more experiments with little risk to the environment.[233,234] Additionally, MD simulations provide insight into molecular-level interactions and the interfacial structural characteristics that are challenging to examine through experiments.[235,236] Besides, MD simulations also aid in the determination of a material's chemical, mechanical, and structural properties, as well as the validation of experimental data at the molecular-level.[233] Because quantum mechanical *ab initio* calculations are confined to systems of hundreds of atoms, atomistic tribology MD simulations have historically been approached using empirical classical models of atomic interactions. These models are, however, developed to fit both experimental data and *ab initio* calculation results.[237] Below we have highlighted a number of studies that have used different types of MD simulations to gain fundamental insights on different tribological systems.

4.1 Molecular dynamics (MD)

MD simulations have been applied to tribological studies involving crystal growth, drying, and wetting at solid–liquid interfaces,[238,239] structural-property examinations to understand the layering of molecules,[240,241] nanotribological properties of hard materials due to sliding, rolling, vibrations, *etc.*[13,242] Researchers have also utilized MD approaches to visualize the material removal rate during rolling machining and the influence of the indenter on the workpiece in the previous decade.[243] Besides studying the surface of materials, MD simulations have also been utilized to study friction between two sliding surfaces and the structure of these interfaces at the atomic-level. The introduction of nanoparticles for improving tribological characteristics has sparked interest in interfacial layer studies.[244–246] The fluid molecule layer on the solid–liquid contact is known as the interfacial layer. When compared to a bulk fluid, it has a thickness of 1–3 nm and a more organized molecular structure.[246]

Researchers are increasingly interested in exploring the interfacial layer of nanoparticles in various tribological systems using computational approaches. The interaction between water and the talc mineral surface, as well as the adsorption of the cationic surfactant DTAB (dodecyl trimethyl ammonium bromide) was studied using an MD simulation approach by Du and Miller.[247] Talc, a significant magnesium silicate mineral, is made up of three layers held together only by van der Waals forces, which can slide over one another – making it an interesting lubricant.[248] The goal of the research was to look at the interfacial structure of water as well as the configuration of adsorbed molecules at the talc basal plane and edge surfaces. The study revealed that the distribution of water normal to certain surfaces was significantly influenced by the substrate's crystal structure. The lack of hydrogen binding sites at the surface resulted in weak binding between water and the talc surface leading to the formation of voids around the substrate as shown in Fig. 10(a)(i) and (ii). It was also found that exposed oxygen and silicon groups at the edges helped strengthen the interactions between talc and water. Similarly, stronger interactions were observed between the hydrophobic basal plane of talc and the tails of surfactant DTAB. All these factors can have a significant effect on the performance of talc as a lubricant in different conditions.[247] MD simulations have also been used to identify the lubrication mechanism of carbon nano-onions. This study by Bucholz *et al.* identified and simulated two mechanisms of rolling and sliding responsible for reducing the CoF between two diamond like carbon (DLC) substrates.[249] The ability of the nano-onions to roll between the substrates was found to be inhibited by higher pressures and by the presence of a diamond core within the nano-onion, resulting in interfacial bonds. It was also reported that as the nano-onions transitioned from rolling to sliding, the CoF significantly increased.[249]

Another form of classical MD involves the use of coarser beads to represent groups of atoms in atomistic simulations.[250] Known as coarse-graining, this approach has been instrumental in studying larger systems that require longer time scales and computational efficiency.[251,252] Traditionally, CG MD simulations have been used to study much larger tribological systems like polymer architectures, self-assembled particles, *etc.*[252–254] A study by Albina *et al.* investigated the properties of lubricants enclosed between nanostructured metal (Fe) surfaces by obtaining a relationship between normal stress and the shear stress exerted on the lubricant molecules using CG MD simulations. The slope of shear stress *vs.* normal stress was used to calculate the CoF at different conditions. It was observed that the lubricant molecules preferentially adsorbed

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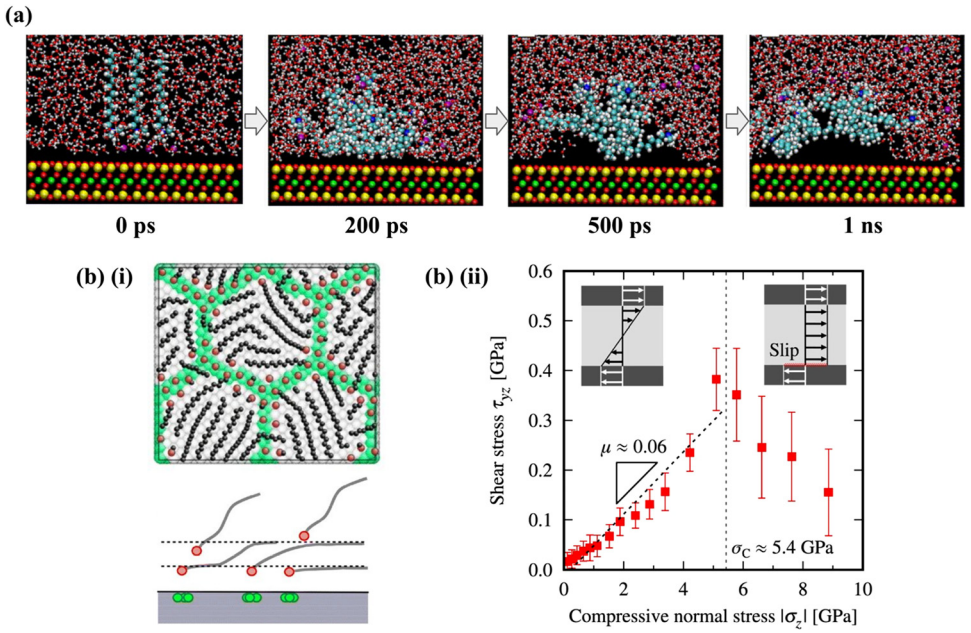

Fig. 10 (a) Snapshots of equilibrated DTAB/water/talc basal plane surface for different simulation times. The color representations are as follows: red-oxygen, white-hydrogen, yellow-silicon, green-magnesium, light blue-carbon, dark blue-nitrogen, and purple-bromide. Reproduced from ref. 247 with permission from Elsevier, copyright 2007. (b) (i) Top view of metal surface (green) with adsorbed lubricant (red COOH group) molecules as well as a schematic illustrating their spatial arrangement, (ii) Shear stress as a function of the compressive normal stress under shear flow for a fixed Fe–COOH interaction strength. The schematics (insets) indicate behaviors of the molecular flow in two characteristic regimes: uniform shear flow (left) and stick–slip motion (right). Reproduced from ref. 255 with permission from Springer Nature, copyright 2020.

to Fe atoms due to strong Fe-COOH interactions as shown in Fig. 10(b)(i). It also was reported that while the strength of the interactions between Fe and the lubricant molecules had little effect on the CoF below the crucial normal stress, as the stress value exceeded, delamination of oil from the metal surfaces occurred resulting in a rapid lateral motion as shown in Fig. 10(b)(ii).[255] Similarly, in a recent study by Kobayashi *et al.*, the authors developed CG bead-spring models for polar PFPE to generate nanometer-thick films sheared between solid surfaces.[256] These systems were simulated to investigate the lubricant dynamic behavior when two types of substrate surface roughnesses were used. More information pertaining to the use of classical MD in tribological systems can be found in a recent review by Srivastava *et al.*[233] as well as several other review articles.[232,257,258]

4.2 Reactive molecular dynamics (RMD)

Following the classical MD simulations, reactive molecular dynamics (RMD) simulations have also been utilized to study tribological applications as they can capture the 'making' and 'breaking' of chemical bonds in order to mimic tribochemical reactions.[259–261] Specifically, their ability to model chemical bonding/debonding has enabled their widespread use in studies aimed at understanding the relevant tribochemical processes that determine friction and wear in sliding contacts. Surface characterization and observation, an essential tool for understanding tribochemical processes and correlating tribofilm composition with friction and wear behavior, still remains a major experimental problem. Experimental research has thus been supplemented with RMD that helps us "see" into a tribological interface, somewhat tackling this difficulty.[26] The accuracy of these RMD simulations is a direct result of their underlying force fields. These force fields are based on Abell's notion of bond order, in which the strength of a bond is determined by the nearby chemical environment.[262] Abell, Tersoff, and Brenner's bond order concept began as an estimated chemical pseudopotential theory, in which the intricate core electron movements are smoothed using an effective potential.[262–264] Bond angles and a symmetry notion account for radical production and investigating the relationship between contacts and local atomic coordination numbers. This resulted in the first- and second-generation reactive empirical bond order (REBO) potentials, which were optimized for carbon-based materials, as well as the adaptive intermolecular REBO (AIREBO) potential, which more realistically treats graphite interlayer repulsion by introducing non-bonded interactions and torsional parameters.[265,266] This family of potentials has been found to be extremely successful in describing carbon-based compounds essential to tribology such as hydrocarbons, diamond, and GR.[267–269] To circumvent the restrictions of fixed-charge bond order formalisms, recent reactive potentials adopt a variable charge method. The charge-optimized many-body (COMB) potential and reactive force field (ReaxFF) are two of the most well-known instances of this in tribochemistry.[270–272]

RMD simulations have been employed for studying chemical reactions that take place between solid substances and their interfaces, within the lubricating substances, or

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between the lubricant and solid surfaces. The REBO potential was used by Harrison and Brenner and was utilized to investigate the tribochemistry and wear between diamond surfaces ending with hydrogen and ethyl groups.[273] Hydrogen atoms sheared off ethyl groups were found to either recombine with radical sites or abstract another H to form H_2 molecules at the interface. The formation and breaking of bonds between radical sites on opposing surfaces was discovered as the process of molecular wear debris formation.[273] A further study by Harrison and co-workers focused on tribochemical explanations for the friction performance of H-terminated diamond and H-free amorphous carbon tribopairs using REBO potential.[274] Due to increased adhesion *via* tribochemical processes, films with a larger fraction of surface sp^2-hybridized carbon were found to display higher levels of friction (relative to sp^3).[275] In another path-breaking study by Berman *et al.*, using AIREBO potentials, assisted in discovering the mechanism of macroscale superlubricity that was achieved using GR in combination with crystalline diamond nanoparticles and amorphous DLC. Simulations, alongside experimental observations, revealed that sliding GR patches over nanodiamond particles resulted in nanoscrolls with a smaller contact area that slid smoothly against the amorphous diamond-like carbon surface.[13] Studies on hydrogenated DLC coatings using a screening potential based on REBO showed that the passivation caused by the migration of methylene groups from one surface to another led to a reduction in friction.[276–278] These studies have also revealed the formation of an amorphous adsorbed layer due to the mechanical dissociation of bonds when polished diamond experiences an sp^3 to sp^2 order–disorder transition, the catastrophic interface failure between self-mated diamond and the amorphous C surfaces due to the formation of hybridized carbon chains, the formation of soft sp^2 + sp amorphous C with interspersed nanodiamond grits upon repeated collisions between diamond asphericities, *etc.*[279]

RMD simulations have also been used for studying the dry friction between tungsten and silica-based surfaces.[278,280] Studying the sliding behavior of rough tungsten upon tungsten carbide, grain refinement was observed at the surface of the tungsten substrate using a modified Tersoff potential.[281] However, the carbide surface displayed a mixed amorphous layer owing to discrete atomic events at the tungsten-carbide sliding surface. When the carbide counter-body was replaced with DLC, hydrogen diffusion into the tungsten surface was observed into the distorted tungsten surface. Similarly, tungsten transfer was also observed in case of non-hydrogenated DLC counter bodies. However, significantly lower transfer was observed when the system was lubricated as shown in Fig. 11(a).[278,280] Similar studies on silica-based surfaces, employing the Tersoff potential, showed that shear created denser amorphous surfaces in diamond-cubic silicon and silicon.[282] Studies have also explored the shear-driven chemical reactions between lubricants and solids such as water and silica.[283] Yue *et al.* showed that submonolayer water aided wear in silicon oxide by supplying oxygen for the formation of Si–O–Si bonds across the sliding contact, thus increasing the interfacial mixing rates. However, when the amount

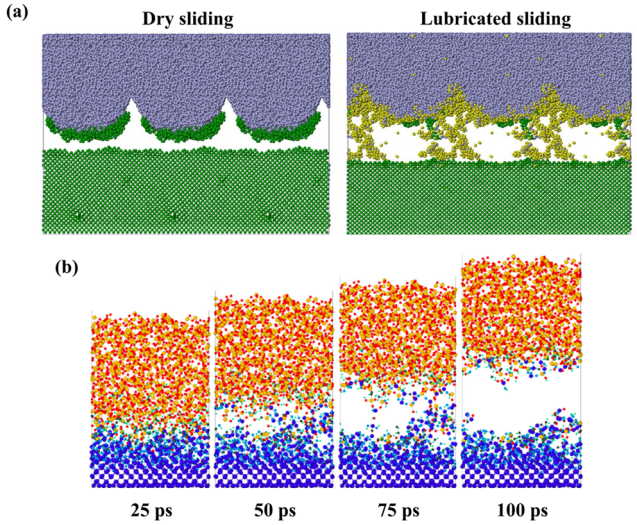

Fig. 11 (a) Atomistic state of ta-C/W sliding couples at 300 K for both dry and lubricated conditions after the two bodies have been pulled apart. The color representations are as follows: green-tungsten, purple-DLC, yellow-hexadecane lubricant. For the dry sliding conditions, significant transfer from the tungsten surface onto the DLC is observed, while in the lubricated case almost no transfer occurs. Reproduced from ref. 278 with permission from Elsevier, copyright 2014. (b) Snapshot views of the vertical separation at a 20 m s^{-1} speed for 100 ps after sliding two amorphous SiO_2 slabs for 1 ns in the presence of 100 water molecules at 500 K. The separation time is shown in each frame. Water molecules are enough to create a full monolayer and thus prevent wear in the sliding surfaces. The color representations are as follows: green-hydrogen, purple-Si of lower slab, yellow-Si of upper slab, blue-O of lower slab, red-O of upper slab, gray-O of water. Reproduced from ref. 284 with permission from American Chemical Society, copyright 2016.

of water was sufficient to form a full monolayer, the degree of atom transfer, and thus wear, reduced dramatically since the silicon atoms could no longer make Si–O–Si bonds as shown in Fig. 11(b).[284] Similarly, another study by Wen *et al.* showed that aqueous H_2O_2 oxidized the Si substrate faster than H_2O, resulting in faster Si atom loss.[284–286] A few studies have investigated solid–liquid reactions between hexadecane with sliding surfaces of W, WC, or DLC with a screened REBO potential.[287] Similarly, a considerable amount of work has been carried out by Martini and collaborators using reactive FFs to study interactions between solid and liquid lubricants, nanoscale contact and sliding, *etc.*[288–291] Comprehensive details regarding the use of RMD simulations in tribological applications can also be further accessed in a detailed review article by Martini *et al.*[26]

4.3 Non-equilibrium molecular dynamics (NEMD)

Non-equilibrium molecular dynamics (NEMD) simulations are used to model the flow of atoms or a group of atoms. The perturbation of equilibrium may be necessitated by external environmental factors like force, temperature or pressure gradient, *etc.*[292] In the context of tribology, NEMD simulations, which involve applying a shear force to the simulated system, have also led to a better understanding of both dry friction, where the sliding surfaces are in close contact, and wet friction,

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where the surfaces are separated by a liquid lubricant.[293–295] A number of factors must be considered in order to perform NEMD simulations, including the inherent limitations of the time and length scales that can be modeled, as well as the accuracy of the representation of intramolecular and intermolecular interactions, similar to classical MD. The fundamental consequence of the short accessible timescales in NEMD simulations is that relatively high shear rates are required to ensure that the parameters of interest (most typically the viscosity) achieve a stable state.[296] Simulating lower shear rates has long been a goal of NEMD simulations in order to permit direct overlap with experiments and real-world components. With this goal, over the last three decades, numerous improvements to the original NEMD techniques have been suggested to increase their signal-to-noise ratio, simplify their implementation, and extend them to different experimental circumstances.[25,297,298]

NEMD simulations have been carried out to study free and confined liquid lubricants. For several linear (C16, C22, and C28) and branched (5,12-dipropyl hexadecane) alkanes, Khare *et al.* were able to replicate lower shear rates and thereby reproduce the Newtonian plateau.[299] The NEMD simulations of n-Newtonian decane's viscosity were in good accord with experiments. Using a united atom (UA) force field which included repulsive and attractive interactions through a Lennard Jones (LJ) potential, they were able to predict the viscosity and thus, the rheological behavior of these lubricant-sized alkanes.[299] The shear-thinning behavior of lubricant-sized molecules has also been studied using NEMD simulations. From 1996 to 2022, several studies have investigated the different shear-thinning behaviors of a number of small molecules using the ever-evolving techniques of NEMD simulations.[293,300–305] Dini and collaborators have used NEMD simulations to study nanotribology,[306–312] including, to investigate the mechanochemistry of phosphate esters confined within sliding iron surfaces,[313] and to derive the transient-time correlation function (TTCF) expression for the computation of shear stress and slip velocity.[314] More details regarding the use of NEMD simulations in tribological applications can be found in several articles available in the literature.[25,310]

5. Applications of ML integrated with computational modeling techniques

The theoretical modeling techniques have demonstrated the ability to simulate the experiments at nano- and macro scale. However, despite the fact that computational researchers have provided many remarkable insights through MD, CG MD, NEMD, RMD, and so on, the immense data generated through MD approach from every time step still remains underexplored. To that extent only few studies have shown the potential to explore this data wisely and efficiently in the field of tribology.[315–318] Table S8 (ESI†) tabulates these four articles describing their tribological investigations on different materials using ML algorithms in MD and DFT.

Quach *et al.*[315] applied a Python-based Molecular Simulation and Design Framework (MOSDeF)[319] with a signac data and workflow management framework[320,321] to perform high-throughput screening of CoF and adhesion force for about 10 000 monolayer films.[321] These two properties are then used as the expected labels for the ML model using the RF algorithm. The 32–42 input physical and chemical features were taken from the RDKit cheminformatics library.[321] The high-throughput screening NEMD simulation results first suggested 22 monolayer designs with target tribological properties which are low CoF and low adhesion force. According to the MD results, the shape and size of the terminal groups play a significant role in determining the CoF of the monolayer. The charge distribution polarity and hydrogen bonding had a strong effect on increasing the adhesion force. The RF models' performance indicates a positive correlation with the size of the datasets, and a training dataset of 1000 points is sufficient. Besides, the RF models trained on a limited dataset could still give meaningful predictions for monolayer designs outside the training set, which suggested a good transferability.[315]

Kadupitiya *et al.* conducted NEMD simulations and applied PCA on the data obtained from these simulations.[316] Specifically, a study was conducted to investigate the rheological properties of squalane under elastohydrodynamic lubrication (EHL) conditions, the lubricant under large pressure of more than 500 MPa and strain rate greater than 10^5 s^{-1}, which is difficult to achieve in an experiment at the same time.[316] Orientation tensors for all-atom pairs were collected from the NEMD simulation trajectories to examine the relationship between rheological properties and the molecular order change of squalane, which in total resulted in 6×435 dimensions data. Then, PCA was applied to reduce the 6 dimensions to 2 for visualization and analysis. It has been demonstrated that the dimension reduction methods successfully group the atom pairs for small rates and pressures systems which show a significant change in the flow behavior. Besides, it also indicated the ability to describe the shear flow of small-molecular liquids.

The statistical model of Bayesian analysis estimates the uncertainty of an event using the probabilistic interpretation. Using the Bayes theorem, probabilities are calculated and updated based on the prior data.[322,323] A posterior distribution is determined by combining knowledge from existing data in terms of prior distributions and the observations in the form of likelihood function.[324] A complex data sets can be modeled with extreme flexibility and certainty through monte carlo sampling techniques.[325,326] Baboukani *et al.* exercised the Bayesian learning approach and transfer learning technique integrated with DFT and MD simulations approach.[317] Particularly, the data generated from DFT and MD simulations included descriptors like structural, electronic, thermal, electron–phonon coupling, mechanical and chemical results, which were used as input for ML models. Using the ML model and the above inputs, a potential energy surface of maximum energy barrier (MEB) was estimated. In their study, they explored various 2D materials including GR and transition metal dichalcogenides (TMDCs) families as lubrication additives,

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as they are known to reduce the friction and wear. Based on the fact that Bayesian models are excellent models in the case of missing data, sparse data or noisy data, the prediction of potential energy surface (PES) through ML models was simplified. The most accurate model for a single-layer 2D material against a similar layer in an inert environment, with the MSE < 0.25 was developed and validated against MD simulations in this study. This combinatorial approach of statistical learning and molecular simulations aided in developing, predicting, and validating the robustness of the MEB–PES successfully.[317]

The Bayesian approach can be also extended through integration with the NN algorithm. Zaidan *et al.* applied a Bayesian neural network (BNN) to model the fluid-friction relation of lubricant.[318] To solve the difficulty of statistical imbalance of data for lubrication performance, the Gaussian mixture model was introduced, and the data was grouped into four clusters for analysis. The data for frictional behavior was obtained from MD simulations using a toy model. The inputs for the BNN was a 25-dimensional array describing the structure information for a system, which is sufficient to capture the fluid characteristics in MD, the output is the shear response. The BNN model was good to deal with uncertainty and prevent overfitting; it could successfully predict the shear with the error around its mean prediction, which can clearly figure out the poorly sampled regions in the dataset.

5.1 ML in MD: our perspective

It should be noted that although the use of ML has been extensively examined in experimental tribological studies, only four papers,[315–318] to the best of our knowledge, have implemented ML in computational modeling studies. The combinatorial approach of ML with MD simulations demonstrated the efficient exploration of MD-obtained data. Through data-driven approaches in MD, it is possible to develop models around the simulation trajectories including positions, velocities, forces as well as the energetics of the system. In addition, the human brain may not be able to extract definitive conclusions from various descriptive modeling analyses. Therefore, to identify the structure–property relationships in complex multi-dimensional problems, ML can be effective in extracting and analyzing hidden features. A ML algorithm learned from these input-output relationships can serve as a surrogate model for the tribological simulations or experiments. This surrogate model as an objective function in the optimization techniques like PSO, GA, *etc.* remain a much efficient approach to design novel materials.

A deep-learning approach called convolutional neural networks (CNN) has proven highly effective in image classification, segmentation and object detection, due to its ability to extract high-level features.[327–329] Few studies have reviewed the advancements of CNN and summarized their exemplary applications through various architectures.[330] Moreover, classical CNN models like LeNet, GoogleNet, RestNet, U-Net, and so on, eliminate the need to tune hyperparameters. A recent study in our group demonstrated a proof-of-concept study of CNN to map 3-dimensional structure of bottlebrush polymers and analyze shapes of complex structures.[331] CNNs, either in 1D, 2D, or 3D, which have shown significant potential to extract structural/imaging features to build their relationship with output in various research fields may prove valuable to assist these MD applications in tribology.[332–336]

Researchers may find it challenging to train ML models at present since they may be unable to identify a combination of features that are appropriate for their learning objectives. Therefore, other deep learning (DL) methods like restricted self-organizing maps (SOMs), restricted Boltzmann machine (RBM), and autoencoders (both stacked and denoising) may assist researchers for feature map generation. In addition, the lack of data in experiments may also contribute to the challenges encountered when using ML. Consequently, deep generative models such as generative adversarial networks (GAN), variational autoencoders (VAE), and deep belief networks (DBN) have been useful in developing models in the absence of large quantities of data.[337–340] A VAE that encodes or decodes sequences of inputs to and from a continuous latent space, with a much lower computational budget, is called syntax-directed VAE (SDVAE) was integrated with Gaussian process regression (GPR) to design novel polymer with high glass transition temperature (T_g) and bandgap by Batra *et al.*[62] The approach can be applied to the development of new polymer lubricants as a classification model could be trained using the data with the known polymers and their tribological properties such as CoF, wear resistance *etc.* Although a couple of studies have shown applications of deep learning models like RNN and radial basis function neural networks (RBFNN), the promising prospects of these algorithms are still underexplored. Specifically, these models may allow one to identify new lubricants with enhanced performances (*i.e.*, reducing CoF and improving wear resistances). Therefore, in general, through the use of these deep learning methods, traditional challenges associated with handling big data, lack of flexibility and multi-task learning in simpler machine learning methods, as well as high computational costs can be overcome. Moreover, surrogate ML or DL models for experiments and simulations both offer an efficient and accelerated method to explore a large design space in material discovery.

6. Emerging materials

Even though our review focuses on the application of different ML algorithms in tribology, the materials used in this study remain largely unrecognized. Only a handful of materials including soft polymers, oils, alloys, *etc.* have been explored. Here, we shed light on other unexplored or less explored classes of materials such as glycomaterials and MXenes.[341–345] Following sections discuss recent advances of these materials in tribological investigations. Although ML has shown the ability to explore composites and lubricants, we believe these new classes of materials are capable of advancing tribological performances through integration with ML.

6.1 Glyco-materials

Matrix composites cater to the needs of automobiles and several other types of industries including mining, construction

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and manufacturing. Despite these diverse applications, their heavy usage can lead to damage of the environment as they are extracted from conventional sources of energy and are toxic in nature.[346] These composites, unfortunately, are not environment friendly and researchers have been venturing to identify greener alternatives to petroleum-based lubricants.[347] In light of this issue, bio-lubricants are viewed as a potential replacement for petroleum-based and matrix composite lubricants.[76,346,348–350] Bio-lubricants, are generally extracted from renewable sources of energy and their greatest advantage is that they are environmentally friendly.[349,350] Bio-lubricants possess desirable characteristics including high lubricity, good temperature-viscosity relationship, biodegradability and low volatility and lower costs.[346,348] However, bio-lubricants suffer from a drawback, which is low oxidation stability.[351] This drawback can be circumvented by several chemical processes including esterification,[352] acetylation[353] and epoxidation.[354,355] Thermal stability and antioxidant properties of castor oil, which is a bio-lubricant were found to be enhanced by the addition of lignin-based compounds.[356] Bio-lubricants derived by epoxidation of waste cooking oil similarly showed improved low temperature performance and oxidation stability compared to waste cooking oil.[357] The enhancement of thermal and oxidation stability of vegetable oils was made possible by genetically modifying the organisms from which they are extracted.[346,358,359] Most commonly used genetically modified oils are sunflower, canola and soybean oils. Gene modification of the organisms is done by DNA transcription in a way that increases the oleic acid content and decreases the linoleic acid content of the vegetable oils.[360] The pour point of vegetable oils can also be improved by increasing the unsaturated long chain or saturated short chain fatty acid content of the oil.[360] Non-conventional hydrocarbons derived by electrochemical decarboxylation, hydro-deoxygenation and ketonic decarboxylation of fatty acids are also available as bio-lubricants.[361] These hydrocarbon-based bio-lubricants can potentially be the replacement for synthetic lubricants. Glycomaterials, are carbohydrate based materials that comprise of complex chains of sugars, called glycans. They have the potential to be developed as a new generation biocompatible lubricants as they are available from renewable energy resources, in addition to being environmentally friendly. For instance, starch when suspended in water has the capability to act as a lubricant.[362] However, the dissolution of starch in water is challenging because of the formation of intermolecular hydrogen bonds between the hydroxyl groups of starch. Solubility of starch in water can be improved by reacting starch with a cyclic dicarboxylic acid anhydrate or by heating it at high temperature and pressure.[362–364] This reaction leads to breakage of strong hydrogen bonded intermolecular structure which reduces the crystalline nature of starch and thereby enhances its solubility in water. Loss of crystalline structure of starch leads to the formation of free hydroxyl groups of glucose which interact with ester groups of triglycerides present in fatty acids forming starch-oil composites which are used as lubricants.[362,365] Starch-oil lubricants are completely derived from renewable sources of energy and are also environmentally friendly. Chemically modified starch contains free hydroxyl groups which increases the polarity of the surface and thereby its CoF.[366] Addition of canola oil to chemically modified starch interacts with the free hydroxyl groups of starch and thereby decreases the CoF.[366,367] Overall applications of glycomaterials are yet to be fully explored and glycomaterials, in general, show a lot of promise of becoming the lubricants of the next generation due to their abundant availability and bio-degradability. Thus, it is necessary to focus in this direction as heavy use of environmentally hazardous materials is a threat to nature.

6.2 MXenes

MXenes are emerging two dimensional (2D) materials, which are synthesized by chemical delamination of ternary or quaternary layered carbides or nitrides of metals.[343,368,369] These materials have wide range of applications including electrochemical storage, lubrication, light emitting diodes (LED), thermal heaters, sensors and optoelectronics.[368,369] Ti_3C_2 coated on copper disk was able to reduce the CoF and wear rate by 4 times and 10 times, respectively, as compared to uncoated copper disks.[370] Enhanced lubricative properties of Ti_3C_2 arise from the creation of a carbon-rich lubricating transferred film by the friction induced graphitization.[370] TiO_2/$Ti_3C_2T_x$ nanocomposites when mixed with base oil lubricant were able to reduce the CoF between the steel surfaces by 2.5 times.[371] This reduction in the CoF value was due to the formation of uniform tribofilm on the steel surface which thereby reduces the scratching of the steel surface.[371] The tribological performance of PAO8 base oil was enhanced by the addition of $Ti_3C_2T_x$ nanosheets.[372] The maximum decrease in the CoF and wear volume were observed when the $Ti_3C_2T_x$ concentration was 0.8 wt% and this improved tribological performance is attributed to the adherence of $Ti_3C_2T_x$ nanosheets to the surfaces and thereby preventing the direct contact between them.[372] Addition of Mo_2CT_x to lithium hexafluorophosphate-based ionic liquid leads to reduction in the value of CoF between Si_3N_4–sapphire interfaces at pressures (1.42 GPa) exceeding the superlubricity regime.[373] Enhanced lubricity and anti-wear performance of the IL was improved due to the tribochemical reaction between the IL and Mo_2CT_x.[373] $Ti_3C_2T_x$-nanoparticles when used as a solid lubricant were able to reduce the CoF by 300% as compared to the value of CoF between bare steel surfaces.[374] A theoretical DFT study on MXenes has provided a detailed perspective on the effect of surface terminations on tribological properties of MXenes. –F and –O terminated MXenes exhibit low adhesion which leads to enhancement in their tribological performance as compared to –OH terminated MXenes. The presence of higher amounts of –F and –O groups on MXenes demonstrates weaker adhesion to ferrous substrates which helps in lubricant deportation under sliding conditions.[375]

7. Overall challenges and conclusion

Overall, researchers have magnificently exemplified the powerful approach of ML and AI, primarily using experimental data.

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Specifically, numerous studies have incorporated the use of ANN in studying non-linear relationships between input variables (operating conditions and material composition) and output (wear and friction). However, only few studies have demonstrated the applicability of other ML models, which may be attributed primarily to their inability of mapping existing non-linear data. Moreover, the proficiency exhibited by ANN on a smaller data set is unparalleled compared to other ML models. Unfortunately, the lack of data, guidance regarding how to use data, and uncertainty regarding learning objectives have resulted in a limited number of publications pertaining to the use of machine learning across a wide range of fields. This task has been assisted in part by deep learning models such as CNN, SOMs, RBM, and autoencoders as they can construct a feature map. It is possible to use these models as surrogates where the user lacks knowledge about the use of input features. Moreover, these models can be implemented for classification as well as regression analysis. Beginners in the field should consider the classic inbuilt models (such as LeNet, GoogleNet, U-Net, *etc.*) as a resource.

The interpretability of big data through ANN, given they are often encountered, remains challenging. For example, in the development of BPNN, the challenges include a large number of samples, slow simulation speed, choice of appropriate hyperparameters like number of hidden layers and neurons comprising it, a choice of training functions and transfer functions and so on. According to the available data, a choice of a desired number of neurons and number of hidden layers can be estimated. Moreover, statistical analysis like ANOVA has proven helpful in interpreting data and associated important input parameters. In order to develop ML models efficiently, it is necessary not only to select the most appropriate algorithms for the desired applications, but also to possess a thorough understanding of their workings. Moreover, ML combined with optimization algorithms like Monte Carlo methods, and improved bat algorithms have indicated that hyperparameter tuning can be performed with a high degree of efficiency. Another aspect of using ML as an objective function by evolutionary-based optimization algorithms has also been discussed.

It has been demonstrated that computational modeling techniques are capable of simulating tribological experiments at microscopic level. To that intent, remarkable insights through MD (including MD, RMD, and NEMD), exemplary properties using DFT are exhibited. These computational approaches generate enormous amounts of data at every time step, however, only a few researchers have exploited molecular simulations data with ML methods. This can be attributed to the lack of tools to processing tools as well as clear paths to integrate this data with ML models. We believe that in the coming years, with more widespread applicability of ML methods and innovations, they will be integrated more frequently with molecular simulations to perform analysis on simulations trajectories. This, in turn, will enable us to discover hidden patterns, structures, and mechanisms at the nanoscale that may not be captured with traditional analysis methods, thus assisting the discovery of new lubricants for various tribological applications.

We also review current trends of ML in tribological applications and encourage the exploration of other classes of materials like glycomaterials and MXenes. Overall, with these emerging materials efforts to develop and implement ML models that can potentially assist experiments and simulations are needed.

Abbreviation list

AE	Acoustic emissions
AIREBO	Adaptive intermolecular reactive empirical bond order
GDX	Adaptive learning rate
ANFIS	Adaptive neuro-fuzzy inference system
ART-2	Adaptive resonance theory
Adj SS	Adjusted sum of squares
ASTM	American society for testing and materials
ANOVA	Analysis of variance
ANN	Artificial neural network
BPNN	Back propagation neural network
BA	Bat algorithm
BNN	Bayesian neural network
BFS	Blast furnace slag
BFGS	Broyden–Fletcher–Goldfarb–Shanno
CF	Carbon fiber
CNT	Carbon nanotube
CNSL	Cashew nut shell liquid
CBPD	Cement by-pass dust
CVT	Centroidal Voronoi tessellation
CMC	Ceramic matrix composite
CG MD	Coarse grained molecular dynamics
CoF	Coefficient of friction
CMO	Commercial mineral oil
CNN	Convolutional neural network
CC	Correlation coefficient
CFPC	Cotton fiber polyester composite
DT	Decision trees
DFT	Density functional theory
DBSCAN	Density-based spatial clustering of applications with noise
DOE	Design of experiments
DLC	Diamondlike carbon
DTAB	Dodecyl trimethyl ammonium bromide
EHL	Elastohydrodynamic lubrication
EFI	Empirical force index
EBP	Error back propagation
ELM	Extreme learning machine
FEM	Finite element method
FF	Force field
FM	Friction modifier
FSW	Friction stir welding
FGM	Functionally graded materials
GA	Genetic algorithm
T_g	Glass transition temperature
GBM	Gradient boosting machine
GR	Graphene

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GO	Graphene oxide
GRA	Gray relational analysis
HA	Hydroxyapatite
IBA	Improved bat algorithm
KNN	*K* nearest neighnours
LFM	Lateral force microscopy
LOO	Leave one out
LJ	Lennard Jones
LM	Levenberg–Marquardt
LED	Light emitting diodes
ML	Machine Learning
MDp	Marble dust particles
MEB	Maximum energy barrier
MAE	Mean absolute error
MRE	Mean relative error
MSE	Mean squared error
MF	Membership function
MMC	Metal matrix composite
MNN	Modular neural network
MD	Molecular dynamics
MOSDeF	Molecular simulation and design framework
MC	Monte carlo
MWCNT	Multi walled carbon nanotube
MoGA	Multi-objectives genetic algorithm
MRA	Multiple regression analyses
NCO	Neutralized castor oil
NFSS	Nickel-free stainless steel composites
NN	Neural network
NEMD	Non-equilibrium molecular dynamics
NSGA	Non-sorting genetic algorithm
PAES	Pareto-archived evolution strategy
PFPE	Perfluoropolyether
POD	Pin-on-disk
PWD	Pine wood dust
PEEK	Poly ether ether ketone
PA	Polyamide
PEK	Polyetherketone
PE	Polyethylene
PMC	Polymer matrix composite
PPS	Polyphenylene sulfide
PTFE	Polytetrafluoroethylene
EP-PUR	Polyurethane
PTW	Potassium titanate whisker
PES	Potential energy surface
CGB	Powell–Beale conjugate gradient algorithm
PC	Principal component
PCA	Principal component analysis
QSTR	Quantitative structure tribo-ability relationship
RBFNN	Radial basis function neural network
RF	Random forests
REBO	Reactive empirical bond order
ReaxFF	Reactive force field
RMD	Reactive molecular dynamics
RNN	Recurrent neural networks
r-GO	Reduced graphene oxide
RSM	Response surface methodology
RH	Rice husk
RHA	Rice husk ash
RMSE	Root mean squared error
RPM	Rotations per minute
SCG	Scaled conjugate gradient
SCF	Short carbon fiber
SGF	Short glass fiber
SWR	Specific wear rate
SPEA	Strength pareto evolutionary algorithm
SVM	Support vector machine
SVR	Support vector regression
SRGM	Symbolic regression multi-gene programming
T_s	Tensile strength
TTCF	Transient-time correlation function
TMDC	Transition metal dichalcogenide
T-BFRP	Treated betelnut fiber polyster
UTS	Ultimate tensile strength
UHMWPE	Ultra high molecular weight polyethylene
UA	United atom
WMD	Waste marble dust
WSD	Wear scar diameter
Y	Young's modulus

Conflicts of interest

There are no conflicts to declare.

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