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Master equation modelling of non-equilibrium chemistry in stellar outflows†‡

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Received 31st January 2022, Accepted 16th February 2022

DOI: 10.1039/d2fd00025c

A current challenge in astrochemistry is to explain the formation of Fe–Mg silicate dust around evolved stars. The dust is observed to form within 2 to 3 stellar radii of oxygen-rich AGB stars, where the typical conditions are kinetic (translational) temperatures between 1200 and 1600 K, and total gas densities below 10^{11} cm^{-3} . At these high temperatures, molecules with bond energies $< 400 \text{ kJ mol}^{-1}$ should be short-lived, and this results in kinetic bottlenecks in postulated mechanisms for converting the observed Fe, Mg, SiO and H_2O into silicate. Here we show that, in the very low pressure regime of a stellar outflow, molecules can exhibit significant vibrational disequilibrium because optical transitions – both spontaneous and stimulated by the stellar radiation field – occur on a much faster timescale than collisions. As a result, relatively less stable molecules can form and survive long enough to provide building blocks to silicate formation. Here we use the molecule OSi(OH)_2 , formed by the recombination of SiO_2 and H_2O , as an example. When vibrational disequilibrium is accounted for in a master equation treatment which includes optical transitions, the quantity of metal silicates produced in a low mass loss rate evolved star (R Dor) is increased by 6 orders of magnitude.

Introduction

The chemical evolution of galaxies depends on mass loss from stars during the late stage of their evolution: asymptotic giant branch (AGB) stars lose a significant fraction of their mass in a short period, during which they tend to be surrounded by an optically thick shell of dust.¹ The absorption and emission of radiation by this circumstellar dust creates a radiation pressure which induces a substantial acceleration in the outflow velocity of the dust (and gas), allowing escape from the star's gravitational field. The dust is also a significant source of interstellar dust

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† Electronic supplementary information (ESI) available. See DOI: 10.1039/d2fd00025c

‡ Potential energy surface for $\text{SiO}_2 + \text{H}_2\text{O}$, molecular parameters used in the master equation and rate coefficients in the stellar outflow model are provided in DOI: 10.5281/zenodo.5925205

In oxygen-rich outflows the dust is observed (by emission spectroscopy in the IR and far-IR) to be mostly composed of the Mg-Fe-silicates olivine and pyroxene ($\text{Fe}_{2-2x}\text{Mg}_{2x}\text{SiO}_4$ and $\text{Fe}_x\text{Mg}_{1-x}\text{SiO}_3$, respectively, where $0 \leq x \leq 1$).^{2,3} However, a continuing challenge in astrochemistry is to explain how these metal silicates form from the components – chemically inert Fe, Mg, SiO – that are observed in the inner wind region close to the star. Although the overall formation of metal silicates from these components is thermodynamically favourable,⁴ identifying a convincing chemical network (*i.e.* a set of elementary reactions) which have favourable kinetics has proved to be elusive.⁵⁻⁹ Fig. 1(a) illustrates the typical kinetic (*i.e.* translational) temperature and total gas density (mostly H_2) modelled as a function of distance r (in units of stellar radius, R^*) for the semi-regular

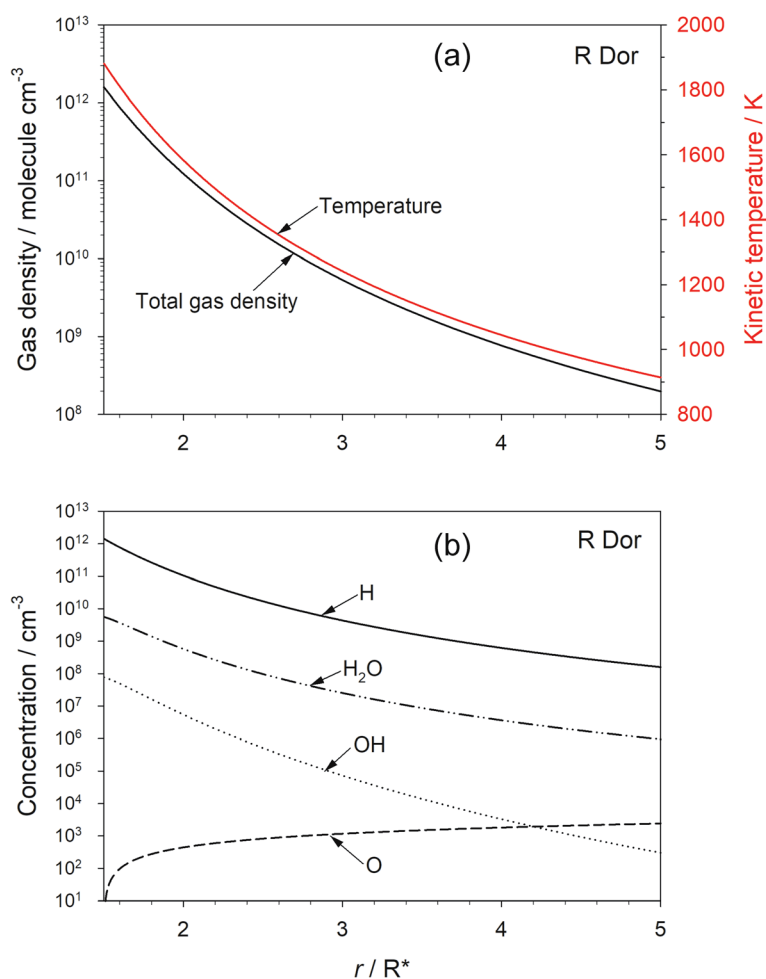
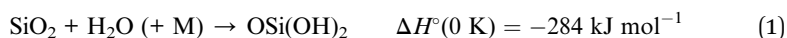


Fig. 1 (a) Predicted total gas density and kinetic temperature as a function of radial position (r , in units of stellar radius R^*) for the β -velocity trajectory model of the SRV star R Dor. (b) Predicted concentration profiles of H, H₂O, OH and O.

It has therefore been concluded that metal silicates are unlikely to form directly in an outflow at temperatures above 1000 K,⁷⁻⁹ so that attention has focused on more refractory alternatives in an O-rich stellar outflow, such as corundum (Al_2O_3),¹¹ titania (TiO_2),¹⁴ and perovskite (CaTiO_3).⁶ If small “seed” particles of these substances were able to form in the inner wind at relatively high temperatures, then they might act as condensation nuclei for metal silicates in the cooler outer wind. However, this would still require metal silicate molecules to form at some point in the outflow.

In this discussion paper we explore the role of vibrational disequilibrium, which we define here as the internal vibrational temperature of a molecule being significantly different from its kinetic temperature. Vibrational disequilibrium can arise when the gas density is low enough so that optical transitions occur at a faster rate than collisional energy transfer. Nuth and co-workers pointed out in the 1980s that the assumption of local thermodynamic equilibrium (LTE) in some astrophysical regions may not be valid.^{15,16} This idea does not appear to have been pursued further, probably because the assumption of LTE greatly simplifies astrochemical modelling. However, observations in this century are clearly showing that molecules in the inner winds of AGB stars are far from LTE. For example, a very recent paper from Fonfría *et al.*¹⁷ shows that at $2R^*$ around the AGB star Y CVn the vibrational temperature of HCN is only 590 K, compared with a kinetic temperature of 1800 K (see Fig. 9 of that paper); similarly low vibrational temperatures have been observed for C_2H_2 and C_2H_4 .^{18,19}

Here we consider the effect of vibrational disequilibrium on the formation and dissociation of the dehydrated form of silicic acid, $\text{OSi}(\text{OH})_2$. This molecule is postulated to form in an outflow from the recombination reaction⁶

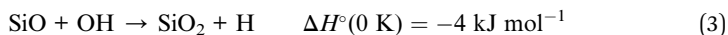


where the reaction enthalpy change is calculated at the CBS-QB3 level of theory.^{20,21} Metal atoms, such as Ca, Fe and Mg, can then react with $\text{OSi}(\text{OH})_2$ to form pyroxene-like molecules, *e.g.*

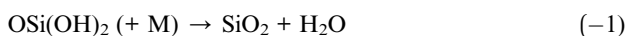




Two problems have been identified with this (otherwise) straightforward route to forming silicates.⁶ First, the only apparent route to forming SiO_2 is oxidation of SiO by OH :



This reaction has been studied at room temperature and is reasonably fast.²² However, because the reaction is only slightly exothermic, the very large concentration of atomic H in an outflow (e.g. Fig. 1(b)) rapidly destroys SiO_2 through the reverse reaction. The second problem is that reaction (1) is only exothermic by around 280 kJ mol^{-1} .⁶ Thus, *assuming* it is in LTE, $\text{OSi}(\text{OH})_2$ should have a relatively short lifetime against thermal dissociation at the high temperatures in the inner wind:



In this study we first determine the Einstein coefficients for spontaneous emission (A) and stimulated emission/optical absorption (B) for the vibrational infra-red active transitions of $\text{OSi}(\text{OH})_2$. These are then incorporated into a master equation treatment to estimate the non-LTE rates for reactions (1) and (-1) , as a function of radial distance r from the star. The resulting rates are then used in a simple stellar outflow model to show that the non-LTE treatment produces a substantial increase in the formation of metal silicates in the outflow.

It is interesting to note that in the *Faraday Discussions* meeting of 1922 there was a vigorous debate about whether dissociation reactions were caused by collisions, the side championed by F. A. Lindemann, or by infra-red photon absorption (from the sun, or reactor walls) – the “radiation theory of chemical action” championed by the French physical chemist J. Perrin.²³ The story of the relatively short-lived radiation hypothesis is well described by King and Laidler.²⁴ Our aim is not to resurrect it here as originally proposed, but rather to show that in the very unusual environment of a stellar outflow optical transitions can have an important influence on the kinetics of recombination and dissociation.

Methods

Photochemistry of $\text{OSi}(\text{OH})_2$

The harmonic vibrational frequencies and infra-red intensities of $\text{OSi}(\text{OH})_2$ were calculated at the B3LYP/6-311+g(2d,p) level of theory, using the Gaussian suite of programs.²⁰ The absorption cross section spectrum is illustrated in Fig. 2, and the vibrational frequencies are listed in Table 1 (note that the 4th mode is infra-red inactive).

The integrated cross section σ_{int} (in units of $\text{cm}^2 \text{ Hz}$) for each vibrational mode was used to calculate the Einstein coefficients for spontaneous and stimulated emission (A_{ij} and B_{ij} , respectively) from the relations:²⁵

$$A_{ij} = \frac{8\pi\nu^2}{c^2} \sigma_{\text{int}} \quad (\text{E1})$$



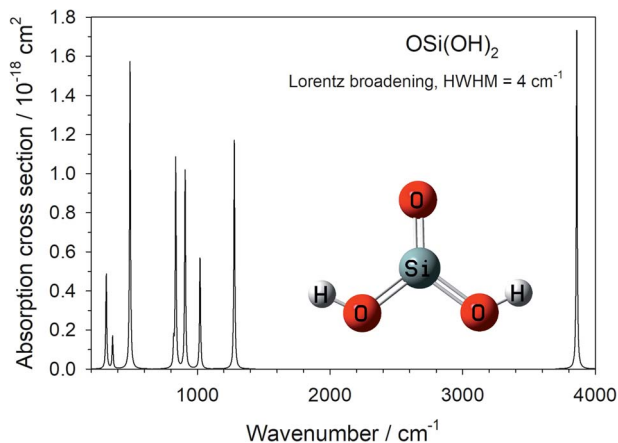


Fig. 2 Absorption cross section of OSi(OH)_2 , calculated at the B3LYP/6-311+g(2d,p) level of theory.

Table 1 Vibrational frequencies, Einstein coefficients and optical absorption/stimulated emission rates for OSi(OH)_2

Mode number	Frequency/ cm^{-1}	A_{ij}/s^{-1}	$B_{ij}/\text{m}^2 \text{J}^{-1} \text{s}^{-1}$	$B_{ij}I^b/\text{s}^{-1}$
1	313.19	0.468	3.04×10^9	0.48
2	321.27	0.038	2.28×10^8	0.037
3	361.07	0.21	8.92×10^8	0.183
4 ^a	423.91	—	—	—
5	492.2	3.57	6.00×10^9	2.2
6	820.78	3.5	1.27×10^9	1.28
7	836.79	7.24	2.48×10^9	2.51
8	907.47	8.13	2.19×10^9	2.3
9	1019.81	5.75	1.09×10^9	1.59
10	1278.14	18.8	1.81×10^9	3.57
11	3859.43	243	8.51×10^8	4.43
12	3861.1	1.91	6.67×10^6	0.032

^a Not infra-red active. ^b Optical absorption/stimulated emission rate at $1R^*$ for the AGB star R Dor.

$$B_{ij} = \frac{c^2}{8\pi h \nu^3} A_{ij} = B_{ji} \quad (\text{E2})$$

where ν is the band frequency (Hz), c is the speed of light, and h is Planck's constant. The rates of absorption and stimulated emission were estimated by multiplying the B_{ij} coefficients by a stellar irradiance flux from the MARCS database²⁶ for an evolved star with $T^* = 2500$ K, which is close to the surface temperature of R Dor.²⁷ The irradiance range was extended to 80 000 nm by fitting a Planck distribution curve at 20 000 nm, the upper wavelength limit of the MARCS model. The values of A_{ij} , B_{ij} (in units of $\text{m}^2 \text{J}^{-1} \text{s}^{-1}$) and the product of B_{ij} with the irradiance I (in units of $\text{J m}^{-2} \text{s}^{-1} \text{Hz}^{-1} \equiv \text{J m}^{-2}$) at $1R^*$ are listed in Table 1 for each vibrational mode. Note that close to the stellar surface the rates of



spontaneous and stimulated emission are fairly similar, apart from the highest frequency modes 11 and 12 where spontaneous emission is much faster.

Optical transitions in the master equation

The Einstein coefficients in Table 1 are for excitation from the ground state to the first vibrational level of each mode. Here we assume that these coefficients remain constant for transitions between higher vibrational levels in each manifold. We also do not include overtone transitions (which would be formally correct for the harmonic oscillator approximation). The justification for these assumptions is that there is some evidence that the Einstein coefficients actually increase somewhat going up a vibrational manifold (which would enhance the role of optical transitions even more), and overtone transitions are much less probable.²⁸

Formation or dissociation of $\text{OSi}(\text{OH})_2$ is assumed to proceed *via* an excited adduct, which can either dissociate to $\text{SiO}_2 + \text{H}_2\text{O}$ or be stabilized by collision with the H_2 third body and spontaneous/stimulated emission, depending on the third body pressure and stellar radiation field *i.e.*, the reaction occurs in a single well. In practice, the potential energy surface connecting SiO_2 and H_2O with $\text{OSi}(\text{OH})_2$ is somewhat more complicated: an initial $\text{SiO}_2\text{--H}_2\text{O}$ complex rearranges over a barrier to produce an asymmetric form of $\text{OSi}(\text{OH})_2$, which then undergoes an internal torsional rotation to produce the most stable symmetric form. The complete surface is shown in the ESI† along with all the relevant molecular parameters for carrying out a full multi-well master equation analysis. In fact, the $\text{SiO}_2\text{--H}_2\text{O}$ complex and subsequent barrier are 89 and 59 kJ mol^{-1} below the entrance channel, respectively; we used the Master Equation Solver for Multi-well Energy Reactions program (MESMER)²⁹ to show that these features are sufficiently submerged to have a very small effect (<1%) on the overall kinetics under the conditions of interest in this study. Hence, reaction (1) is treated here as a simple recombination involving a single well containing the more stable $\text{OSi}(\text{OH})_2$ isomer.

The internal energy of the $\text{OSi}(\text{OH})_2$ adduct was divided into a contiguous set of grains (width = 40 cm^{-1}) containing a bundle of rovibrational states. Each grain was then assigned a set of microcanonical rate coefficients for dissociation, which were determined using inverse Laplace transformation to link them directly to $k_{\text{rec},\infty}$, the high-pressure limiting recombination coefficient. This was estimated using long-range transition state theory³⁰ to be $k_{\text{rec},\infty} = 8.7 \times 10^{-10} (T/1200 \text{ K})^{1/6} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$. The density of states of each adduct was calculated with the vibrational frequencies in Table 1, without making a correction for anharmonicity, and a classical densities of states treatment for the rotational modes (see the ESI† for all rotational constants and vibrational frequencies used, including those of SiO_2 and H_2O). The probability of collisional transfer between grains was estimated using the exponential down model, where the average energy for downward transitions, $\langle \Delta E_{\text{down}} \rangle$, was assigned a value of 200 cm^{-1} for H_2 at 300 K and a small temperature dependence of the form $T^{0.25}$.³¹ The probabilities for upward transitions were determined by detailed balance.^{31,32} The collision rate of H_2 with the adduct as a function of temperature was calculated using Lennard-Jones parameters to characterise the intermolecular potential, giving $Z(T) = 8.4 \times 10^{-10} (T/1200 \text{ K})^{1/2} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}$.

The master equation, which describes the evolution with time of the adduct grain populations, is given by:



$$\begin{aligned} \frac{d\rho_i(t)}{dt} = & \omega \sum_j \text{Pr}_{ij} \rho_j(t) - \omega \rho_i(t) - k_i \rho_i(t) \\ & + \sum_{s=1}^{11} (A_{i,i+\delta\varepsilon^s} \rho_{i+\delta\varepsilon^s}(t) - A_{i-\delta\varepsilon^s,i} \rho_i(t) + I^s (B_{i,i+\delta\varepsilon^s} \rho_{i+\delta\varepsilon^s}(t) - (B_{i-\delta\varepsilon^s,i} + B_{i+\delta\varepsilon^s,i}) \rho_i(t) \\ & + B_{i,i-\delta\varepsilon^s} \rho_{i-\delta\varepsilon^s}(t))) + R_i \end{aligned} \quad (\text{E3})$$

where $\rho_i(t)$ is the grain population; ω is the frequency of collisions of $\text{OSi}(\text{OH})_2$ with the bath gas (*i.e.* $Z(T)$ [M], where $M = \text{H}_2$); Pr_{ij} is the probability of transfer from grain j to grain i on collision with M; and k_i is the microcanonical rate coefficient for dissociation of the adduct. s is the vibrational mode number of $\text{OSi}(\text{OH})_2$ (the sum is over 11 because the 4th mode is inactive – Table 1). Optical transitions for each mode can only occur between states that are separated by a fixed energy, $\delta\varepsilon^s$, which depends on the frequency of mode s . So for the spontaneous transitions, state i can receive density *via* an optical transition from a grain that is $i + \delta\varepsilon^s$ higher in energy (Einstein coefficient $A_{i,i+\delta\varepsilon^s}$), and lose density to a grain that is $\delta\varepsilon^s$ lower in energy (Einstein coefficient $A_{i-\delta\varepsilon^s,i}$). The stimulated transitions can go both ways, so grain i can gain population by absorption from grain $i - \delta\varepsilon^s$ (Einstein coefficient $B_{i,i-\delta\varepsilon^s}$) and stimulated emission from grain $i + \delta\varepsilon^s$ (Einstein coefficient $B_{i,i+\delta\varepsilon^s}$), but also lose population *via* absorption from grain i to $i + \delta\varepsilon^s$ or emission from state i to $i - \delta\varepsilon^s$. I^s is the radiance. Lastly, R_i is the rate of population of grain i if recombination is occurring.

The master equation was then expressed in matrix form and solved *via* diagonalization to yield the recombination rate coefficient (k_1) or dissociation rate coefficient (k_{-1}) at a specified pressure and temperature.

Stellar outflow model

The stellar outflow is modelled here using a β -velocity law, which describes the net acceleration of the wind without explicitly considering pulsations:

$$v_\beta(r) = v_0 + (v_\infty - v_0)(1 - R^*/r)^\beta \quad (\text{E4})$$

where v_∞ is the terminal velocity, which is 5.7 km s^{-1} for R Dor,²⁷ $v_0 = v(R^*) = 1.5 \text{ km s}^{-1}$ is the initial velocity at the stellar surface $r = R^*$ ($= 2.5 \times 10^8 \text{ km}$), and the parameter $\beta = 1$. The temperature profile is given as a power-law with an exponent $\alpha = 0.6$ and the density $n(r)$ is expressed using the pressure scale height $H = RTR^{*2}/(\mu M^*G)$ (where R is the gas constant, μ is the molecular mass of H_2 , M^* the mass of the star, and G the gravitational constant), the ideal gas law, and parameter $\gamma (= 0.89)$.⁵

$$T(r) = T^*(r/R^*)^{-\alpha} \quad (\text{E5})$$

and

$$n(r) = n^* \exp\left(\frac{R^*(1-\gamma)^2}{H(1-\alpha)}\right) \left(1 - \left(\frac{r}{R^*}\right)^{\alpha-1}\right) \quad (\text{E6})$$

The surface pressure for R Dor is taken as $n^* = 10^{14} \text{ cm}^{-3}$ and the effective temperature T^* is 2400 K .^{11,27}



The chemistry network in the model is taken from Plane.⁶ Measured rate coefficients are adopted from the NIST kinetics database,³³ and those of other reactions (e.g. reactions (2), (3) and (−3)) were calculated⁶ using electronic structure theory combined with MESMER;²⁹ these are listed in the ESI.† The model predictions of the total gas density, kinetic temperature, and major constituent concentrations are shown in Fig. 1.

Results and discussion

Fig. 3(a) shows how the first-order dissociation rate of $\text{OSi}(\text{OH})_2$ varies as a function of $[\text{M}]$, for the conditions of the star R Dor at $r = 2R^*$, where

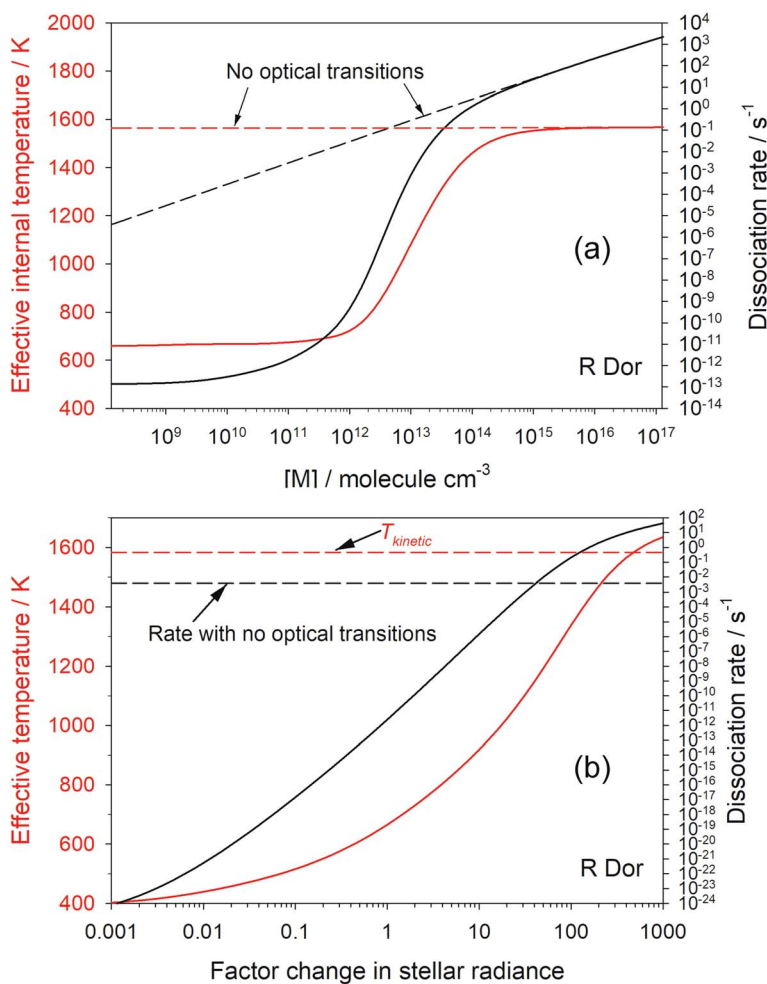


Fig. 3 (a) Variation of the first-order dissociation rate of $\text{OSi}(\text{OH})_2$ as a function of third body (H_2) concentration, with optical transitions (black line) and with them turned off (dashed black line). The effective internal temperature of $\text{OSi}(\text{OH})_2$ is shown by the corresponding red lines. (b) Dependence of the $\text{OSi}(\text{OH})_2$ dissociation rate and internal temperature on the stellar radiance, for a fixed $[\text{M}] = 1.2 \times 10^{11} \text{ cm}^{-3}$. The conditions are for R Dor at $2R^*$.



Fig. 3(b) shows how the internal temperature of $\text{OSi}(\text{OH})_2$ and its first-order dissociation rate vary as a function of stellar intensity ($[\text{M}]$ is fixed at $1.2 \times 10^{11} \text{ cm}^{-3}$). As the star gets brighter, the internal temperature and dissociation rate increase. The dissociation rate exceeds that with optical transitions turned off when the intensity is increased by a factor of 42, and the internal temperature exceeds the translational temperature when the radiance is increased by a factor of 520. In contrast, if the star gets very dim (radiance factor $< 10^{-3}$), the dissociation rate and temperature become constant because spontaneous emission keeps the molecule cool, but collisional excitation is still occurring.

Fig. 4 shows the second-order rate coefficient for the recombination of SiO_2 and H_2O (reaction (1)), as a function of $[\text{M}]$. The dashed line is the case for optical transitions turned off, where the reaction exhibits the expected fall-off behaviour as $[\text{M}]$ increases. However, when optical transitions are included (solid line), the rate coefficient levels off at low $[\text{M}]$ ($< 10^9 \text{ cm}^{-3}$) to a constant value, which is the radiative recombination rate. Once $[\text{M}] > 10^{14}$, the effect of optical transitions is minimal and collisional stabilization dominates. At this point the ratio of the recombination rate to the dissociation rate equals the thermal equilibrium constant of reaction (1), consistent with the internal temperature approaching the kinetic temperature (Fig. 3(a)).

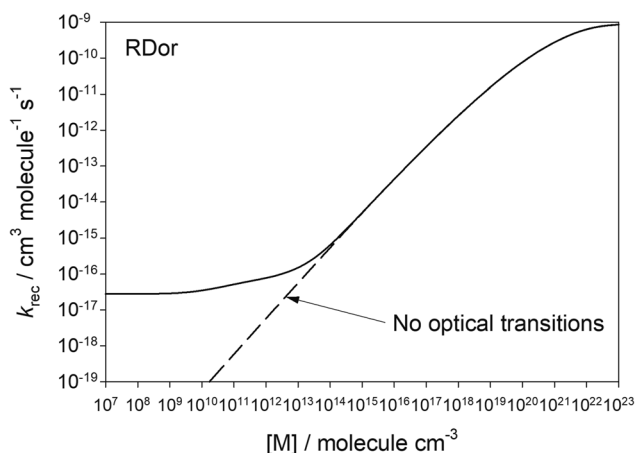


Fig. 4 Second-order recombination rate coefficient for reaction (1) as a function of $[M]$. The stellar radiance is for R Dor at $2R^*$.

Fig. 5(a) shows the predicted variation of the internal temperature and kinetic temperature of $\text{OSi}(\text{OH})_2$ as a function of r for the star R Dor. At $2R^*$, these temperatures are 725 and 1583 K, respectively, illustrating significant

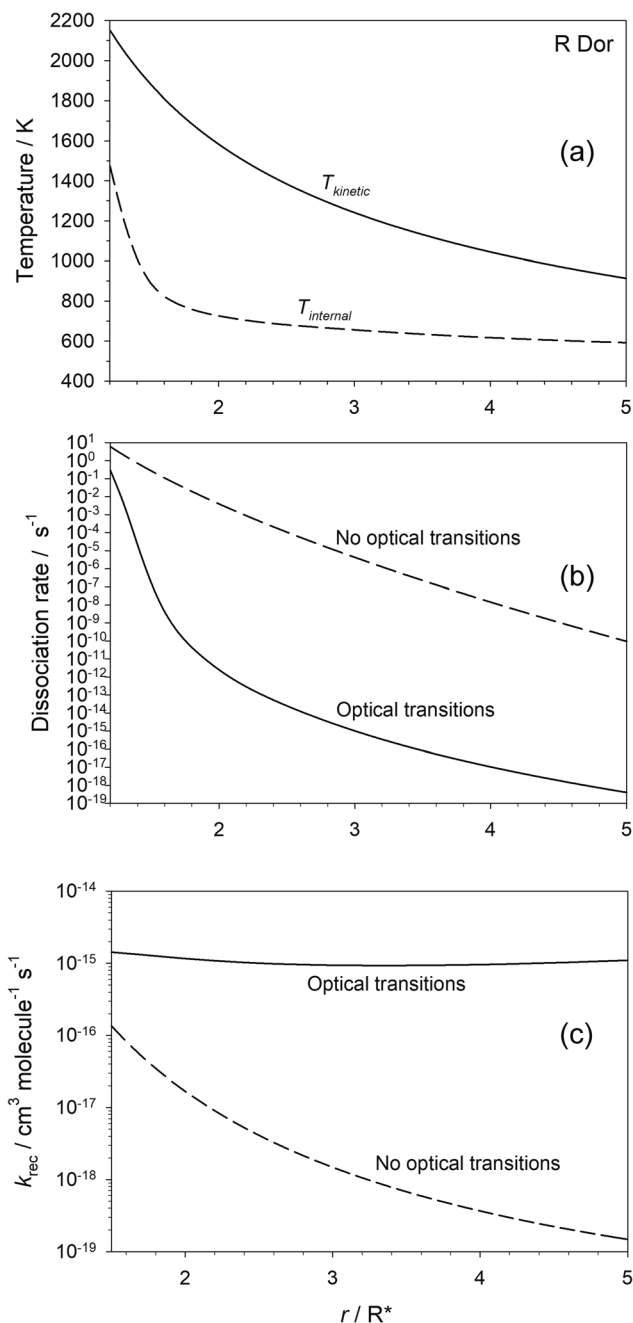


Fig. 5 (a) Kinetic and internal temperature of $\text{OSi}(\text{OH})_2$; (b) first-order dissociation rate coefficient of $\text{OSi}(\text{OH})_2$ and (c) second-order recombination rate coefficient for $\text{SiO}_2 + \text{H}_2\text{O}$, with and without optical transitions, as a function of r for R Dor.

disequilibrium of the molecule that is comparable to that observed recently for HCN,¹⁷ as discussed in the Introduction. Fig. 5(b) shows that when optical transitions are included, the dissociation rate of OSi(OH)₂ becomes orders of magnitude lower because of the much colder internal temperature of the molecule. It is only close to the star that the H₂ density is high enough for collisional energy transfer to warm the molecule to the point where the dissociation rate approaches that when optical transitions are turned off in the model.

The effect on the second-order recombination rate of SiO₂ and H₂O is illustrated in Fig. 5(c). Moving away from the star, the decrease in [H₂] by 4 orders of magnitude between 1.5 and 5R* is only partially offset by the decrease in temperature, so that k_{rec} decreases by ~ 3 orders of magnitude. In contrast, when optical transitions are turned on, there is very little change in the recombination rate with r , because radiative recombination quickly becomes the dominant process, particularly as the stellar radiance is decreasing as r^2 so that spontaneous emission becomes more important than absorption.

The rate coefficients plotted in Fig. 5(b) and (c) were parameterised as a function of r (see Table S2 in the ESI†) and then input into the stellar outflow model (Methods). Fig. 6 illustrates the predicted concentrations of the three metal silicates – CaSiO₃, FeSiO₃ and MgSiO₃ – as well as OSi(OH)₂ as a function of r . The black and red lines show the model run with and without optical transitions, respectively. When optical transitions are included for reactions (1) and (–1), the OSi(OH)₂ concentration is on average 9.0×10^5 times higher between $r = 1.5$ and 5R*. This accounts for the metal silicate concentrations being around 10^6 times larger when the OSi(OH)₂ optical transitions are turned on. Note that CaSiO₃ is predicted to be the dominant silicate that forms in the outflow: on average it is 3×10^4 higher in concentration than FeSiO₃, and 3×10^7 higher than MgSiO₃, in this part of the outflow. The reason is that reaction (2) does not have an energy

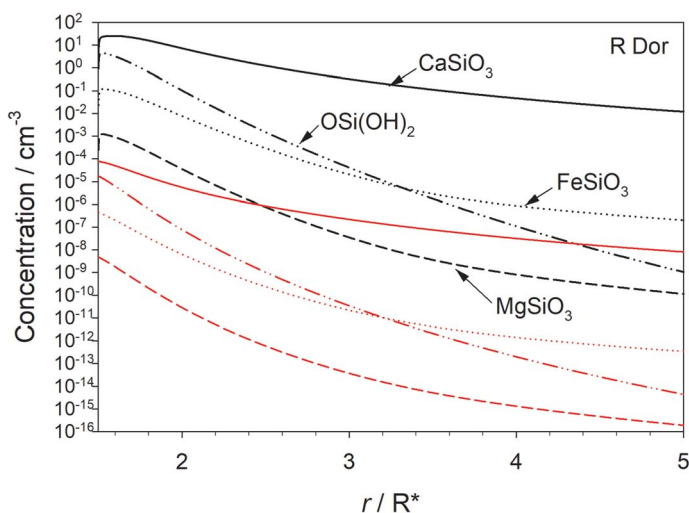


Fig. 6 Concentration profiles of CaSiO₃ (solid lines), MgSiO₃ (dashed lines), FeSiO₃ (dotted lines) and OSi(OH)₂ (dot-dash lines) as a function of r for R Dor, when optical transitions of OSi(OH)₂ are included (black lines) or turned off (red lines).



barrier, whereas the analogous reactions of Fe and Mg with OSi(OH)_2 have barriers of 31 and 51 kJ mol^{-1} , respectively (see the ESI†).⁶ Fe, Mg, SiO and H_2O probably then add to CaSiO_3 , producing mixed metal pyroxenes and olivines. This chemistry will be the subject of future work.

Conclusions

This study is a first step in incorporating optical transitions into a master equation treatment of recombination and dissociation reactions, motivated by the observation of significant molecular vibrational disequilibrium in stellar outflows. For this exploratory work we have made various assumptions and approximations, the most important being that the vibrational modes are treated as harmonic oscillators with Einstein coefficients that remain constant in each of the vibrational manifolds. Nevertheless, this model is able to reproduce the magnitude of vibrational disequilibrium that has been observed in small molecules.^{17,18} If a molecule is vibrationally cool then its dissociation rate will be reduced compared to the dissociation rate if the molecule were vibrationally equilibrated with the high kinetic temperatures in this environment. In addition, radiative recombination becomes more important than collisional energy transfer at these low pressures, so that the recombination rates are greatly enhanced over what would be expected by extrapolating from the higher pressures where these reactions tend to be studied in the laboratory.

An important astronomical result is the substantial increase in the concentration of metal silicates that are predicted to form *via* this mechanism involving OSi(OH)_2 when optical transitions are included. The modelled silicate mixing ratio with respect to H_2 is 6×10^{-11} , which would produce a relatively small amount of dust.⁶ However, R Dor has a relatively low mass loss rate of only $2 \times 10^{-7} M_\odot$ per year (where $M_\odot$ = solar mass), whereas mass loss rates range from 2×10^{-8} to $4 \times 10^{-5} M_\odot$ per year for M-type AGB stars.³⁴ Because the rates of silicate-forming reactions like reaction (2) depend on the square of the concentrations of the relevant species (metals and SiO) in the outflow,⁶ for a high mass loss rate star of $1 \times 10^{-5} M_\odot$ per year the predicted silicate mixing ratio would be ~ 2500 times larger.

Author contributions

JMCP: conceptualisation, funding acquisition, formal analysis, software, writing.
SHR: formal analysis, software, writing.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

This work was supported by the UK Science Technology and Facilities Council (grant ST/T000287/1).



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