



Cite this: DOI: 10.1039/d1re00098e

An automated computational approach to kinetic model discrimination and parameter estimation†

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We herein report experimental applications of a novel, automated computational approach to chemical reaction network (CRN) identification. This report shows the first chemical applications of an autonomous tool to identify the kinetic model and parameters of a process, when considering both catalytic species and various integer and non-integer orders in the model's rate laws. This kinetic analysis methodology requires only the input of the species within the chemical system (starting materials, intermediates, products, etc.) and corresponding time-series concentration data to determine the kinetic information of the chemistry of interest. This is performed with minimal human interaction and several case studies were performed to show the wide scope and applicability of this process development tool. The approach described herein can be employed using experimental data from any source and the code for this methodology is also provided open-source.

Received 8th March 2021,
Accepted 7th May 2021

DOI: 10.1039/d1re00098e

rsc.li/reaction-engineering

Introduction

Rapid process development can be critical for the commercial success of new chemical products. For example, within the pharmaceutical industry time-to-market from initial discovery is one of the most important factors for companies to maximise commercial viability.¹ As the cost of this product development can be up to 35% of the total cost of bringing a new drug to market,² there is an emphasis on fast and efficient process optimisation and scale-up of active pharmaceutical ingredients (APIs).^{3–5} Ideally to achieve this a detailed understanding of all elements of the process in question is required, including fundamental synthetic chemistry considerations such as the reaction mechanism and kinetics, and the effects of chemical engineering aspects such as transport phenomena (transfer of heat, mass *etc.*). Statistical techniques are commonly used to map the design space during process development in modern industrial labs typically through a design of experiments (DoE) approach,^{6–8}

with closed loop algorithm methods also becoming more popular.^{9–11} However, a more robust description of the process can be determined by developing an accurate mechanistic rate model of the chemical reaction steps.^{12,13}

Such kinetic models can be complex and occur over many reaction steps, involving many measurable and immeasurable intermediates. This allows quantitative chemical synthesis information to be obtained, allowing classical reaction engineering principles to be applied to shorten process development times and lower costs.¹⁴ In these instances, obtaining stoichiometric and kinetic descriptions of the individual transformations is often more important than detailed mechanistic insights and rationales.¹⁵ For a system involving multiple reactions, each featuring multiple species with differing stoichiometric coefficients and respective kinetic parameters, this is referred to as a chemical reaction network (CRN). Upon determination of a CRN, mathematical relationships are thereby established between participating species, allowing simulations and process engineering to drive reaction understanding and ultimately optimise chemical systems through a reduction in laboratory experiments.^{16–18} However, in this report we will be explicitly focussing on the identification of the process CRN from apparent kinetics; for further discussions on the scale-up of chemical processes, refer to work by Levin¹⁹ and Khang and Levenspiel.²⁰

There are many reports in the literature involving the use of computation to evaluate aspects of a CRN,^{21–27} many of which are based on work reported by Aris and Mah,²⁸ then

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† Electronic supplementary information (ESI) available. See DOI: 10.1039/d1re00098e



later Bonvin and Rippin.²⁹ However, there are no CRN identification tools to date that identify catalytic reaction pathways or non-integer species orders, which greatly limits the applicability of these techniques for many chemical systems. Other techniques have also emerged, such as the use of model-based design of experiments (MBDoE) for various applications.^{30–35} Whilst there is an increased scope for this methodology, assigning a model may be difficult for noisy systems due to standalone measurements in otherwise empty chemical space.³⁶ Furthermore, expert chemical intuition is necessary in compiling initial model candidate sets for evaluation and many models may be excluded based on their presumed inability to occur.

We recently illustrated the first experimental application of a comprehensive CRN determination methodology,³⁷ initially reported by Tsu *et al.*¹⁴ This machine-learning-based tool identifies and evaluates all possible kinetic models, then uses statistical analysis to establish which model is most likely to be correct. The user simply inputs the mass of each participating species and experimental data, then the approach autonomously identifies the most likely CRN. This paper reports significant improvements to this technique, including how the scope of application has been expanded to zero- and non-integer-order reactions and catalytic processes. This work represents the first CRN determination tool in the literature with these capabilities. Two new experimental case studies are herein reported and one further case study was revisited due to the applicability of this tool to its unusual and complex kinetic model. The methodology can be used with data from any source and any analytical technique, although this work features exclusively reactions in batch using both NMR sampling and HPLC analysis. This upgraded open-source tool serves as a comprehensive, automated resource for the process development of almost any chemistry, where scalable process understanding can be achieved with minimal need for high-level chemical intuition.³⁸

The approach

It is firstly important to note that following from the initial inputs of the measurable species of interest and the experimental time-series data, the approach behaves as a black box to identify the most likely reaction model and corresponding kinetic parameters. Initially, every possible chemical transformation is identified based on mass balance alone using an integer linear programming (ILP) optimiser. All feasible rate laws for these reactions are then constructed – this relates to different allowed species orders: 0, 0.5 and 1. These species orders are considered as they are the most likely to be encountered, whereas further non-integer orders are not considered due to their rarity and significantly increased computational burden their inclusion would cause. If a catalytic species is also present, this is incorporated into the respective rate laws at this point. Each of these reactions can then be treated as building blocks for potential CRNs. Every combination of these reactions (and therefore every

possible CRN) is then built and saved to a CRN library, therefore describing the chemistry in every feasible way – this stage of the approach is referred to as the model generation stage. The total number of possible models, η , is equal to the sum of the binomial coefficients for every number of individual reaction rate laws in the model, up to the total number of possible reactions, δ , as shown in eqn (1):

$$\eta = \sum_{i=1}^{\delta} \binom{\delta}{i} \quad (1)$$

The second stage of the approach relates to the suitability of each individual CRN, or model, to the supplied experimental data, referred to as the kinetic fitting stage. A cycle is conducted as a CRN is loaded, then a gradient-based local minimisation algorithm is used to optimise kinetic parameters and fit simulated kinetic curves to the data points using the CRN's respective rate laws, thereby measuring the convergence of the CRN to the chemical data. These simulated kinetic curves are referred to as ordinary differential equations (ODEs), as they are a result of solving a linked set of differential equations. The sum of squared error (SSE) measurement between the measured (experimental) and estimated (simulated) concentrations is the objective function that is minimised to ensure maximum convergence of the model to the data. This SSE value is calculated using eqn (2), where N_{Data} is the number of data points sampled, E_j is the j th experimental point and S_j is the j th simulated point:

$$\text{SSE} = \sum_{i=1}^{\delta} \sum_{j=1}^{N_{\text{Data}}} (E_j - S_j)^2 \quad (2)$$

This sequence is repeated until all CRNs have been assessed. The determination of the most likely CRN from the library is finally conducted by evaluating the corrected Akaike's information criterion (AIC_C), which is used as a statistical measure to identify the simplest models that show the highest convergence to experimental data.³⁹ This is calculated using eqn (3):

$$\text{AIC}_C = N_{\text{Data}} \cdot \ln \left(\frac{\text{SSE}}{N_{\text{Data}}} \right) + 2\delta + \frac{2\delta(\delta + 1)}{N_{\text{Data}} - \delta - 2} + N_{\text{Data}} \cdot \ln(2\pi) + N_{\text{Data}} \quad (3)$$

An overview of the approach is shown in Fig. 1. Although herein used as a black box, the approach is open-source³⁸ and a further publication will detail all working components and the considerations made in building the methodology.

This approach serves as an automated tool that removes high-level chemical expertise from both model and kinetic parameter determination during process development. Conducting this model discrimination, without chemical intuition, creates a system whereby a model is identified based purely on the most statistically accurate and quantitative physical-organic description of the chemistry. This allows experts to spend their human resource on more challenging aspects of process development that cannot be otherwise automated, including critically appraising the



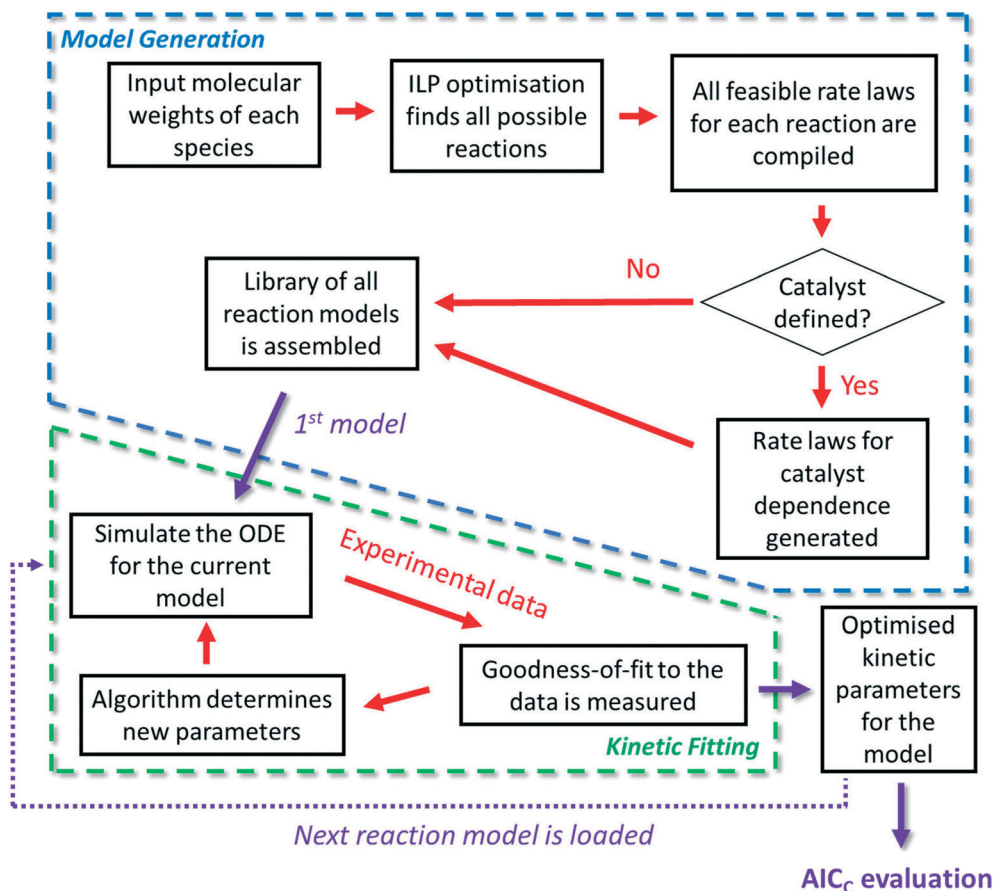
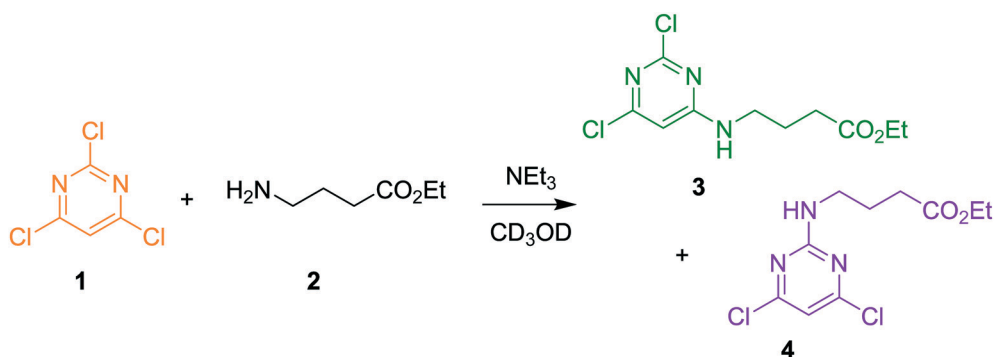


Fig. 1 An overview of the approach, consisting of two main stages: model generation and kinetic fitting. Every feasible reaction model based on mass balance is assembled and subsequently evaluated, optimising the kinetic parameters to maximise convergence to the experimental data. Each model is also assigned an AIC_c evaluation, from which the most likely CRN is obtained.

resultant list of model candidates. For example, after this initial model discrimination experts can alter the identified CRN based on perceptions of chemistries that are unlikely to be true, as model terms may be included due to anomalies in the experimental data provided. More advanced engineering principles may also be applied or further experiments may be prescribed by experts to discriminate between the list of ranked CRNs generated.

Results and discussion

The approach can receive inputs from many different analytical sources and the implementation, scope and accuracy of this methodology was demonstrated *via* several pharmaceutically relevant case studies. The first case study of interest is the S_NAr reaction of 2,4,6-trichloropyrimidine, **1**, with ethyl 4-aminobutanoate, **2**, to form the major 4-substituted product,



Scheme 1 The presupposed reaction model of the S_NAr case study.



3, and the minor 2-substituted product, 4, and forming HCl, 5, after each step - this is shown in the presupposed model in Scheme 1. As the desired major product from this reaction can be further functionalised to synthesise bioactive derivatives of pharmaceuticals,^{40,41} this initial transformation is of interest in the transfer of these molecules to scale up, meaning that kinetic information would be very useful for process development.

Experiments were undertaken at various temperatures between $-25\text{ }^{\circ}\text{C}$ and $50\text{ }^{\circ}\text{C}$ using an NMR tube within a 500 MHz NMR machine with a constant acquisition rate, thereby obtaining complete reaction profiles. This experimental data could then be inputted into the computational approach, as well as the species involved (1–5) to identify all possible elementary reactions. Every combination of these reactions (in every form of their corresponding rate laws) were then constructed and comprehensively assessed, resulting in 3320 unique model evaluations. It was found *via* AIC_C analysis that the most likely model is the reaction model shown in Scheme 1 with a first-order dependence of both 1 and 2 in forming the major and minor products. The approach also determined the kinetic parameters of the transformation to the major product: $k_{25^{\circ}\text{C}} = 0.499 \pm 0.006\text{ M}^{-1}\text{ min}^{-1}$, $E_a = 44.19 \pm 0.57\text{ kJ mol}^{-1}$ and to the minor product: $k_{25^{\circ}\text{C}} = 0.384 \pm 0.009\text{ M}^{-1}\text{ min}^{-1}$, $E_a = 36.57 \pm 0.88\text{ kJ mol}^{-1}$. In this example the user has only inputted the experimental data, the molecular weights of each of the species and indicated that the reaction is not catalytic. All kinetic analysis was then performed autonomously, producing the list of ranked CRNs to be evaluated by a trained chemist shown in Table 1. After appraisal, this newly obtained information can subsequently be used to significantly shorten the overall process development time during pharmaceutical manufacture. The top-ranked model and the corresponding kinetic parameters allowed a fit to the experimental data with an average residual of less than 0.3% and is shown in Fig. 2. Full experimental details and raw data can be found in the ESI† (Section 3).

It is clear from the kinetic plots that the fit of the ODEs to the experimental data do not result in normally-distributed residuals. This could be for one of many reasons but is most likely due to either NMR integrations errors, evaporation of solvent (CD_3OD) into the headspace at higher temperatures or changes in solvent viscosity at these differing temperatures. It is also possible that liberation of HCl as the reaction progresses

forms rapid equilibria with the base, NEt_3 , and partial protonation of the nucleophile leading to reduced reactivity. Although this approach can automatically determine the most likely reaction model and kinetic parameters from experimental data, all of these factors must still be considered by a trained chemist upon completion of the computation to confirm the methodology output. In this case, however, the residuals are only a small consideration and it can be observed that the model still provides a good fit to the data. This kinetic information can then be used to optimise this process for the highest yields of the 4-substituted product, 3, when scaling up production of the material.

The next case study conducted was a chemical system featuring the protection of an amino acid for further functionalisation, where alanine methyl ester (Al-Me), 6, reacts with 9-bromo-9-phenylfluorene (PbBr), 7, to form the protected amino acid (Pf-Al-Me), 8, and hydrobromic acid, 9, as shown in Scheme 2 as a presupposed model. PbBr is the reagent used to introduce the 9-phenylfluorene (Pf) protecting group in synthesis. Pf is a pharmaceutically relevant and bulky protecting group, that can be introduced as a more acid stable alternative to the more commonly used trityl group.^{42,43} This case study is the protection step involved in the total synthesis of (*S*)-elegantine from *L*-alanine. Therefore, understanding this transformation by performing kinetic analysis would lower costs and accelerate process development in the overall bioactive alkaloid manufacture,⁴⁴ following promising reports of potent analgesic properties.⁴⁵

Three experiments were run between $30\text{ }^{\circ}\text{C}$ and $40\text{ }^{\circ}\text{C}$ in a batch vessel, then the four identified species (6–9) and all experimental data were inputted into the computational approach. In this system a heterogeneous base, K_3PO_4 , was added to remove the HBr as it formed. Two feasible mass-balance-allowed reactions were calculated, then each combination of these reactions (in every variant of their rate laws) were assessed by the approach automatically, resulting in 30 unique model evaluations. The most likely representation of the model was identified by the approach as the presupposed forward reaction shown in Scheme 2, with a first-order dependence on PbBr (7) and a zero-order dependence on Al-Me (6). This has not been reported elsewhere in the literature, but this discovery makes chemical sense as the bulky aromatic rings would stabilise the cation formed, should the reaction proceed *via* a traditional $\text{S}_{\text{N}}1$ mechanism; this means that the rate-determining step is likely to be the loss of the bromide ion, followed by a fast nucleophilic addition by the alanine methyl ester. The approach also determined the kinetic parameters of this transformation to be $k_{35^{\circ}\text{C}} = 1.06 \times 10^{-2} \pm 0.01 \times 10^{-2}\text{ min}^{-1}$, $E_a = 62.91 \pm 0.23\text{ kJ mol}^{-1}$. This example further proves how using this automated methodology in conjunction with chemical study helps to both elucidate reaction mechanisms and gain process understanding for real-life applications. The top-ranked model and corresponding parameters allowed a fit to the experimental data with an average residual of less than 0.4% and is shown in Fig. 3. Full

Table 1 A ranked list of reaction models generated from the computational approach, showing also the kinetic parameters for each model, the fit to the experimental data using the sum of squared error (SSE) of fitted residuals and model scoring using AIC_C. α is a variable for each model depending on the overall model order

Rank	Reaction model	Kinetic parameters		SSE/ 10^3 M	AIC _C
		$k_{25^{\circ}\text{C}}/\text{M}^{\alpha}\text{ min}^{-1}$	$E_a/\text{kJ mol}^{-1}$		
1	1 + 2 → 3 + 5	0.499	44.19	1.614	−51.91
	1 + 2 → 4 + 5	0.384	36.57		
2	1 + 2 → 3 + 5	0.407	40.61	3.723	−48.57
	1 + 2 ^{0.5} → 4 + 5	0.073	31.01		
3	1 + 2 → 3 + 5	0.466	42.25	3.777	−48.51
	1 ⁰ + 2 → 4 + 5	0.017	27.56		



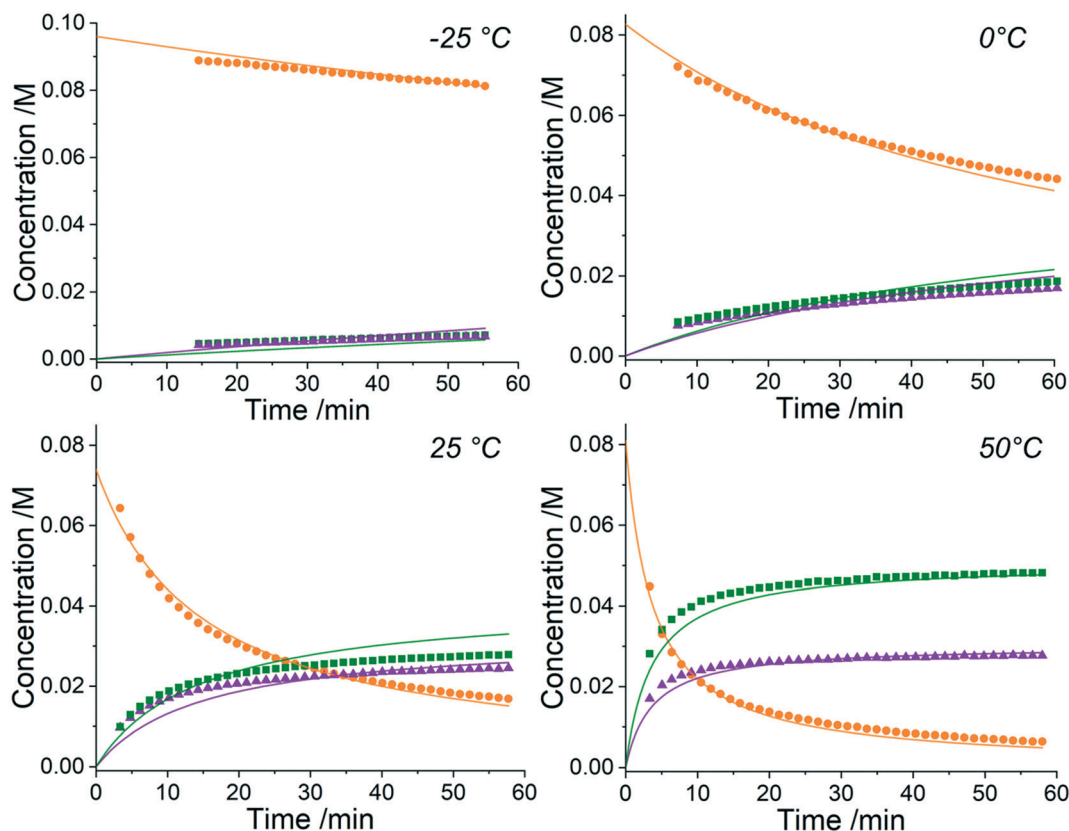
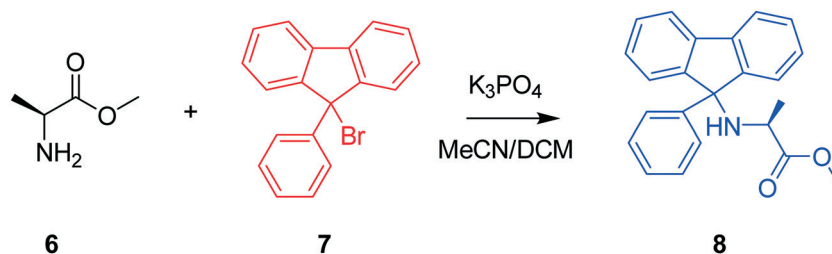


Fig. 2 Results from the four kinetic experiments (at $-25\text{ }^{\circ}\text{C}$, $0\text{ }^{\circ}\text{C}$, $25\text{ }^{\circ}\text{C}$ and $50\text{ }^{\circ}\text{C}$) in the $\text{S}_{\text{N}}\text{Ar}$ case study in CD_3OD , where: $\bullet$ = 2,4,6-trichloropyrimidine, $\blacksquare$ = major product, $\blacktriangle$ = minor product, — = 2,4,6-trichloropyrimidine (ODE), — = major product (ODE), — = minor product (ODE).



Scheme 2 The presupposed reaction model of the PfBr protection case study.

experimental details, raw data and model rankings can be found in the ESI† (Section 4).

The final case study explored was the chemical system involving maleic acid, **10**, reacting with methanol, **11**, to form the monomethylated maleic acid ester (mono-product), **12**, and the dimethylated maleic acid ester (di-product), **13**, each liberating a molecule of water, **14**, as shown in the presupposed model in Scheme 3. Our collaborators at AstraZeneca were interested in this reaction following the contamination of a batch of an API maleate salt with the corresponding monomethyl maleate salt, as this contamination could be mitigated if the impurity formation was well understood.

Kinetic experiments were run using this system and the findings were published, as it was found that the reaction forming the mono-product was self-catalytic.⁴⁶ In this case, the reaction was found to be catalytic with an order of 0.5,

meaning that the overall order with respect to the maleic acid was 1.5 in forming the mono-product. The consecutive reaction forming the di-product is also catalytic with respect to the maleic acid with a 0.5 order dependence. As methanol is the solvent in this reaction with an effective concentration of $\sim 24\text{ M}$, pseudo-order conditions are assumed and rate laws with non-zero-order dependence on methanol were removed from consideration for simplicity. Although the kinetics of this process are now known and reported, it took several months for physical-organic chemists to decipher this model as the reactivity is not immediately intuitive. Therefore, this case study was run to validate the approach in elucidating non-intuitive reaction models, and how this methodology can serve as a viable, automated substitute for many hours spent on a project by experts that could be working on other aspects of process development.



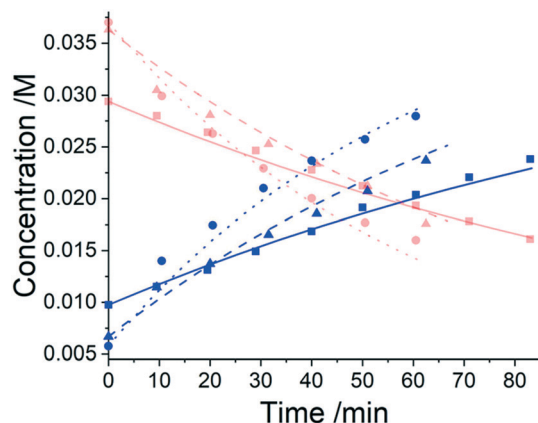
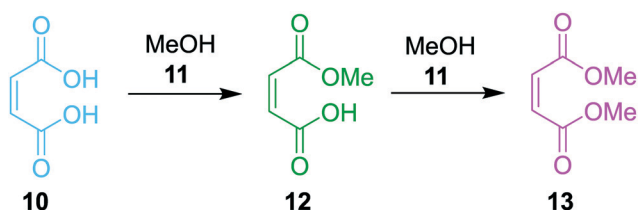


Fig. 3 Results from the kinetic experiments in the PfBr protection case study in 50:50 acetonitrile/dichloromethane, where red plots indicate PfBr concentrations and blue plots indicate Pf-Al-Me concentrations. At 30 °C: ■ = experimental data, — = ODE. At 35 °C: ▲ = experimental data, — = ODE. At 40 °C: ● = experimental data, = ODE.



Scheme 3 The presupposed reaction model of the maleic acid case study.

Five experiments were conducted in batch at differing starting concentrations and temperatures in the range of 40 °C to 60 °C and analysed using ^1H NMR sampling. This experimental data and the five species (10–14) were inputted into the approach, resulting in six mass-balance-allowed transformations identified. The catalyst was defined, then every combination of these catalytic reactions (and corresponding rate law variants) were compiled into different reaction models, resulting in 5086 automatic unique model evaluations. Each of these models were then ranked based on their AIC_C and it was found that the most likely representation of the system is the reaction model shown in Scheme 3, but each step is catalysed by maleic acid with an apparent species order dependence of 0.5. These are the same findings that our collaborators made during their kinetic analysis, as they also employed a pragmatic approximation of a 0.5 catalytic order in maleic acid due to the observation of specific acid catalysis. The approach also determined the kinetic parameters of this transformation to be: $k_{\text{mono } 50^\circ\text{C}} = 3.85 \times 10^{-3} \pm 0.01 \times 10^{-3} \text{ M}^{-0.5} \text{ min}^{-1}$, $E_a = 72.61 \pm 0.12 \text{ kJ mol}^{-1}$ and $k_{\text{di } 50^\circ\text{C}} = 4.66 \times 10^{-4} \pm 0.01 \times 10^{-4} \text{ M}^{-0.5} \text{ min}^{-1}$, $E_a = 69.74 \pm 0.10 \text{ kJ mol}^{-1}$. These parameters are in agreement with those obtained by our collaborators. This model and the corresponding kinetic parameters allowed a fit to the experimental data with an average residual of less

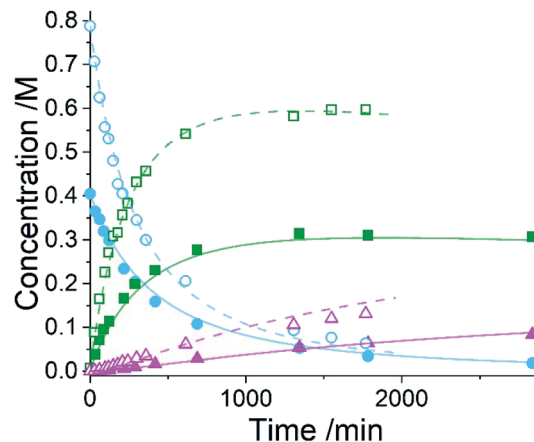


Fig. 4 Kinetic profiles for two kinetic experiments at 50 °C in methanol, with the initial concentration of maleic acid at 0.4 M and 0.8 M. At 0.4 M: ● = maleic acid, — = maleic acid (ODE), ■ = mono-product, — = mono-product (ODE), ▲ = di-product, — = di-product (ODE). At 0.8 M: ○ = maleic acid, — = maleic acid (ODE), □ = mono-product, — = mono-product (ODE), △ = di-product, — = di-product (ODE).

than 0.2% and two experimental fittings at 50 °C are shown in Fig. 4. Full experimental details, raw data and model rankings can be found in the ESI† (Section 5).

As the model was already identified by our collaborators, this methodology has corroborated their findings and shown that process understanding can be accelerated using this approach. This approach automatically identified the correct reaction model in ~17 hours of computational time, whereas the more traditional science-led approach took appreciably longer with significant human resource required. Clearly the use of this comprehensive model-based approach would be an asset to kinetic specialists during similar case studies when there is significant time pressure to find robust solutions to manufacturing problems identified.

Conclusion

It has been shown from these case studies that in using this computational methodology as a black box approach, scalable process understanding can be automatically achieved without the need for high-level chemical intuition in the model determination and parameter estimation steps. The widened scope of this new approach has been proven to be effective in three experimental case studies, each with differing rate laws and kinetic structural motifs. The efficiency and accuracy of the approach remain robust in all cases, when observing 'typical' kinetic models where each species has a first-order dependence, for zero-order and non-integer rate laws and for catalytic species of variable integer- and non-integer-orders.

It has also been shown from these case studies that using this methodology can greatly accelerate process development and reduce the workload of kinetic analysis for physical-organic chemists. After experimentation, all kinetic analysis



can be implemented autonomously whilst experts focus on other aspects of process development. After the computational evaluations have finished running, these experts can then work in conjunction with the approach to identify which models are the most likely to be statistically and scientifically correct as well as determine if further studies are necessary. The increased breadth of scope of this reported approach serves as an open-source enabling tool in discriminating kinetic models, thereby greatly reducing the time and cost barriers to complete process understanding.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

CJT, TWC and RAB thank the School of Chemical and Process Engineering and the School of Chemistry at the University of Leeds for their support, and EPSRC (EP/R032807/1) and AstraZeneca (EP/N509681/1) for their funding and support. The authors thank Ian W. Ashworth for his contributions and help in the preparation of the manuscript. HS and FMD thank Duncan J. Howe and Andrew Mason for analytical support, Trinity College Cambridge, and AstraZeneca and BBSRC, respectively, for studentship support. RAB was supported by the Royal Academy of Engineering under the Research Chairs and Senior Research Fellowships scheme (RCSRF1920\9\38).

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