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Highly sensitive and room temperature detection of ultra-low concentrations of O₃ using self-powered sensing elements of Cu₂O nanocubes

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The fundamental development of the design of novel self-powered ozone sensing elements, operating at room temperature, based on p-type metal oxides paves the way to a new class of low cost, highly promising gas sensing devices. In this work, p-type Cu₂O nanocubes were synthesized by a simple solution-based method and tested as a self-powered ozone sensing element, at room temperature (25 °C) for the first time. Highly crystalline Cu₂O nanocubes with 30 nm size were characterized by X-ray Diffraction (XRD), Scanning Electron Microscopy (SEM) and Transmission Electron Microscopy (TEM). Self-powered sensing elements of Cu₂O nanocubes have been successfully fabricated by deposition of Cu₂O nanocubes on interdigitated electrodes (IDEs) consisting of two connection tracks with 500 digits and a gap of 5 μm in order to investigate their response to ozone at room temperature. The experimental results showed that the use of nanocubes as sensing elements was suitable for detecting ultra-low concentrations of O₃ down to 10 ppb at room temperature with very high sensitivity (28%) and a very low response/recovery time. The reversible sensing process of the relatively weak binding of O₃ species by trapping sites on Cu₂O facets with increased oxygen content was studied by using density functional theory (DFT) calculations.

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Introduction

Some of the most common pollutant gases in air are NO₂, O₃, CO, SO₂ and NO. Among them, ozone (O₃) is closely related to human life since it is widely used in a numerous applications such as in food storage and in the pharmaceutical, textile and chemical industries. Moreover, it works as a protective layer in the Earth's stratosphere for human health, absorbing the harmful ultraviolet (UV) radiation. On the other hand, according to the World Health Organization (WHO), excess exposure to ozone concentrations of more than 1 parts per million (ppm) can cause breathing problems, trigger asthma, reduce lung function and induce lung diseases and induce the burning eyes symptom. Thus, it is apparent that detection of ozone at ultra-low concentrations (*i.e.* low ppb levels) is of great importance.¹

The use of metal oxide semiconductors as sensing elements for monitoring air quality has emerged as a low cost alternative

due to fast response/recovery rates and low detection limits.^{2–4} In particular, cuprous oxide (Cu₂O) as a p-type semiconductor, with a narrow direct energy band gap of $E_g = 2.17$ eV, has been tested as gas sensor material in recent years and highlighted due to its good stability and high conductivity. In addition, Cu₂O is non-toxic and copper is earth abundant and hence inexpensive. To date, numerous micro- and nano-structures of octahedral^{4,5} and polyhedral⁶ Cu₂O have been reported, with a variety of morphologies, such as nanocubes,^{7,8} spheres,⁹ nanowires,¹⁰ and quasi-spherical shapes,¹¹ using solution-based synthetic methods. Cu₂O films have been also been produced *via* a variety of methods including thermal oxidation, magnetron sputtering, spray pyrolysis, *etc.*^{12–15} In the field of gas-sensing, Cu₂O has great potential in detecting various pollutants in their gaseous form, due to its significant surface reactivity with both reducing (ethanol, gasoline, CO, and H₂S)^{3,5,7,8,16} and oxidizing gases (NO₂, CO₂, CH₄, and O₃).^{4,6,7,9,10,17,18} However, the working temperature of the sensors fabricated using Cu₂O is significantly higher than room temperature (25 °C).^{4,6,9–13}

Considering the detection of O₃, the majority of studies are related to composites with other metals such as CuAlO₂ and CuCrO₂ tested against a variety of gas concentrations and at different working temperatures. To the best of our knowledge, Ouali *et al.* were the only report on the use of Cu₂O for 10 to 1000 ppb level sensing of O₃ at an operating temperature of 175 °C.¹⁷ Moreover, Zhou *et al.* synthesized both nanocrystals

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(10–80 nm) and thin films of CuCrO_2 for the detection of 50–200 ppm O_3 at room temperature (25 °C), with the maximum response (6%) measured at 200 ppm.¹⁸ Deng *et al.* prepared CuCrO_2 thin films for the detection of 100 ppb O_3 at room temperature, using air for the recovery of the system.¹⁹ Zheng *et al.* prepared transparent CuAlO_2 thin films for the detection of 0.1% O_3 (99.9% O_2) at room temperature,²⁰ while Thirumalairajan *et al.* synthesized CuAlO_2 nanostructures of two different sizes (40 and 80 nm) with flower-like and hexagonal morphologies, for the sensing of 200, 600, and 1150 ppb O_3 at 250 °C, with the best response and recovery time of 25 and 39 s for 200 ppb.²¹ Finally, Baratto *et al.* used CuAlO_2 thin films for the detection of a wide range of O_3 concentrations (70–350 ppb) at an operating temperature between 300 °C and 500 °C in a humid air background²² and Thirumalairajan *et al.* synthesized CuAlO_2 microspheres to detect 200, 600, and 1150 ppb O_3 at 200 °C, with the response and recovery times being equal to 29 s and 45 s (for 200 ppb at 200 °C), respectively, and the highest response reaching the value of 2.8 at 1150 ppb.²³

In this work, we describe a one pot, controllable synthesis of p-type Cu_2O nanocubes with approximately 30 nm size, through an additive-free aqueous solution route, at room temperature. The method is facile, fast, eco-friendly and inexpensive. Highly crystalline Cu_2O nanocubes were deposited on interdigitated electrodes for gas sensing measurements. Two-terminal direct current–voltage measurements showed that the use of the nanocubes as the sensing element was suitable for detecting ultra-low concentrations of O_3 down to 10 ppb at room temperature (25 °C) with high sensitivity (28%) and low response/recovery times. The reversible sensing process of the relatively weak binding of O_3 species by trapping sites on Cu_2O facets with increased oxygen content was calculated by employing density functional theory (DFT). This is the first report on the use of Cu_2O nanocubes for the detection of ultra-low O_3 concentrations, at room temperature, highlighting the tremendous potential of this rather simple technology.

Experimental section

Copper(II) acetate hydrate ($\text{Cu}(\text{CH}_3\text{CO}_2)_2 \cdot x\text{H}_2\text{O}$, 98%), sodium hydroxide (NaOH, 98–100.5%) and L-ascorbic acid ($\text{C}_6\text{H}_8\text{O}_6$, 99%) used in this work were obtained from Sigma-Aldrich. All the reagents were used as received without any further purification.

Synthetic procedure of Cu_2O nanocubes

In a typical synthesis, a mixture of 40.0 mL of 0.009 M L-ascorbic acid solution and 64.0 mL of 0.1 M NaOH solution was added to 64.0 mL of previously prepared 0.005 M copper(II) acetate ($\text{Cu}(\text{Ac})_2$) solution under stirring. The mixed solution was then stirred vigorously for 15 min, during which the solution became yellow and turbid, indicating the formation of Cu_2O . Finally, the precipitates were collected through centrifugation and washed with distilled water and absolute ethanol several times. All the experiments were carried out at room temperature.

Materials characterization

The crystallographic structure of Cu_2O was demonstrated by X-ray diffraction (XRD) measurements using a Rigaku RINT-2000 system with $\text{Cu K}\alpha$ ($\lambda = 1.5418 \text{ \AA}$) X-rays produced at 40 kV and 82 mA. The 2θ collection range was 10–80° with a scan rate of $0.05^\circ \text{ s}^{-1}$. The average crystal size (D in nm) of nanoparticles was calculated from the line broadening of the X-ray diffraction peak according to the following Scherrer's formula:

$$D = k\lambda/\beta \cos \theta, \quad (1)$$

where k is the Scherrer constant (~ 0.9), λ is the wavelength of the X-ray radiation ($1.54 \text{ \AA}$ for $\text{CuK}\alpha$), β is the full width at half maximum (FWHM) of the diffraction peak measured at 2θ , and θ is the Bragg angle. The surface morphology and microstructure analysis was performed by both Field Emission Scanning Electron Microscopy (JEOL 7000) at an acceleration voltage of 15 kV and Transmission Electron Microscopy (TEM) using a JEM-2100 instrument equipped with LaB6 filament, operating at 200 kV.

Gas sensor fabrication and measurements of ozone sensing properties

A paste of Cu_2O nanoparticles was prepared by dispersing 4.0 mg of Cu_2O nanocubes in 1 mL of methanol. Subsequently, the paste was drop-cast onto pre-patterned interdigitated (IDT) Pt electrodes on a glass substrate and left to dry at room temperature, resulting to the formation of a thin layer. The interdigitated electrodes were composed of two connection (all made of platinum on a glass substrate) tracks with 500 digits and a gap of $5 \mu\text{m}$ to ensure a good coverage of the Cu_2O nanocubes. Moreover, they are compatible with CMOS technology and able to operate at room temperature allowing low power consumption. The as-prepared devices were used for the ozone sensing measurements, inside a purpose-built gas test chamber (Fig. 1). The ozone was obtained using a calibrated ozone generator equipped with an internal analyzer (Thermo Electron Corporation, model 49i) at different concentrations in the range 10 to 820 ppb, while for the recovery of the sensor the chamber was backfilled with ambient air. Electrical characterization of the devices as a function of ozone concentration was performed by monitoring the electrical current level at a constant bias voltage of 10 V, using a Keithley 6517A electrometer. All the sensing measurements were carried out at room temperature. The sensitivity of the sensor is defined as

$$S (\%) = [(I_{\text{gas}} - I_{\text{air}})/I_{\text{air}}] \times 100\%, \quad (2)$$

where I_{air} denotes the current value before gas injection, while I_{gas} denotes the maximum current value in the presence of ozone. The response time of the sensor is defined as the time required for a change in the current to reach 90% of the initial value when exposed to a set ozone gas concentration. Similarly, the time required for the current of the sensor to reach 90% of the initial value after the ozone gas has been turned off is defined as the recovery time.



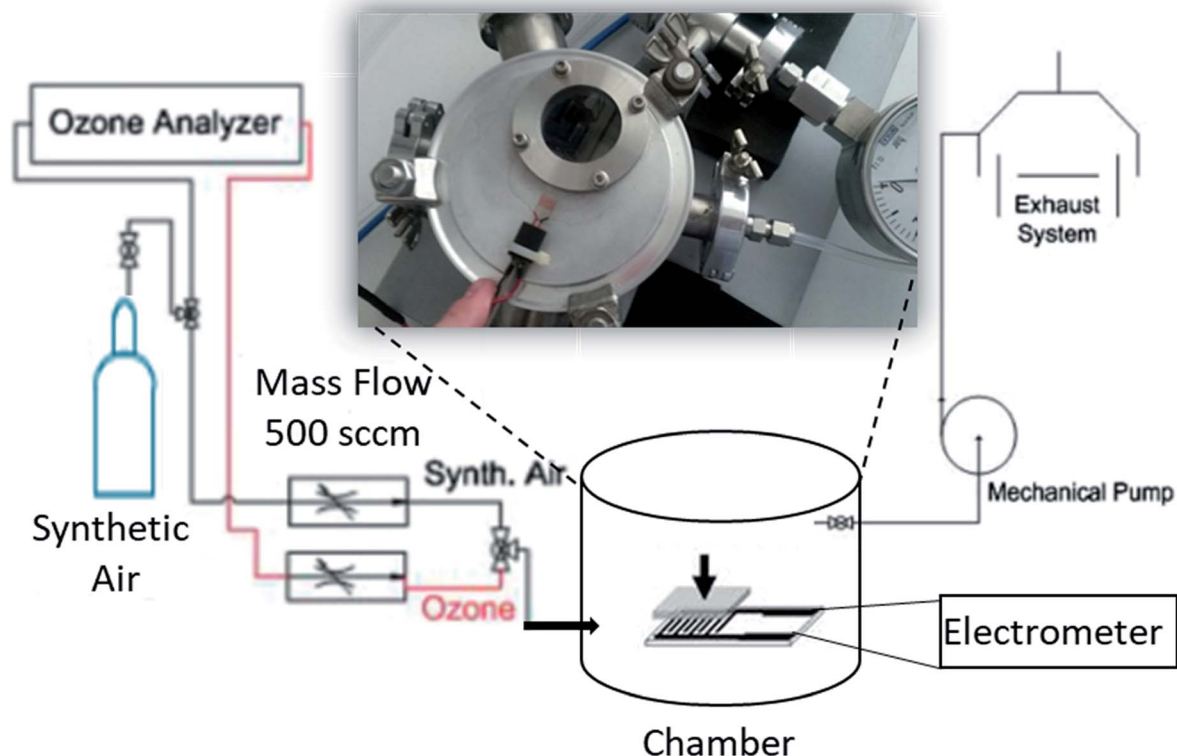


Fig. 1 Conductivity-based system with a gas test chamber.

Density functional theory (DFT) calculations

First-principles spin-polarized calculations were performed with the Density Functional Theory (DFT) code Quantum Espresso,²⁴ projector-augmented waves²⁵ to model the interactions between valence electrons and ionic cores, the PW91 exchange–correlation (xc) functional²⁶ and the DFT-D2 method²⁷ to take into account van der Waals interactions. The energy cutoff of the plane wave basis was set at 75 Rydberg (Ry) and integrations in reciprocal space used $2 \times 2 \times 1$ or $4 \times 4 \times 1$ Monkhorst–Pack k -point grids²⁸ or tetrahedron sampling,²⁹ respectively, for the determination of total energies or electronic densities of states. The (001) surfaces of Cu_2O were modeled as slabs with 7 layers and 2×2 supercells in the lateral directions (with at least 86 atoms). The relaxation of structures was terminated when the energy converged within 10–6 Ry. We also obtained the energies for the highest occupied (HOMO) and lowest unoccupied (LUMO) molecular orbitals of an O_3 molecule with the hybrid B3LYP xc-functional³² and the 6-311+G* Gaussian basis set (as implemented³⁰ in the NWChem code).

Results and discussion

Cu_2O nanocubes were characterized using a powder X-ray diffractometer (XRD). Fig. 2a shows the XRD pattern of Cu_2O nanocubes and the standard Cu_2O card. All the diffraction peaks are consistent with the standard card (JCPDS card no. 05-0667) of cubic phase Cu_2O attributed to the (110), (111), (200), (220), (311) and (222) crystal planes. Specifically, the strong and

sharp peaks indicate that the obtained Cu_2O nanocubes are highly crystalline with an average crystal size of 19.7 nm, as calculated using Scherrer's formula. After the controllable synthesis of Cu_2O nanocubes, the representative morphology and size were determined by field emission scanning electron microscopy (FESEM) and high resolution transition electron microscopy (TEM) as shown in Fig. 2b and c. From this, it can be seen that Cu_2O material is mainly composed of uniform cubes that are 30 to 35 nm in size. Highly crystalline Cu_2O nanocubes with 30 nm size were deposited on interdigitated electrodes with a good coverage as shown in Fig. 3a and b.

The two-terminal interdigitated sensor devices were tested at room temperature whilst been exposed to different concentrations of ozone in the range 10–820 ppb. The repeatability of the sensing response was also examined by repeating the measurement several times using different Cu_2O nanocube-based devices. Fig. 4 shows the evolution of the current (measured at a constant bias of 10 volts) as a function of time and exposure to different ozone concentrations. In particular, the measurement included two steps: (i) the sensor was exposed to an atmosphere containing O_3 with a predetermined concentration for approximately 2 min while the current was monitored in real time; (ii) the ozone flow was turned-off and the device was exposed to ambient air (relative humidity $\approx$ 55%) for approximately 1 min. The same measuring cycle was repeated for O_3 concentrations of 170, 490 and 820 ppb (Fig. 4). It is clearly evident that the current across the Cu_2O nanocube channel increases in the presence of ozone, an observation



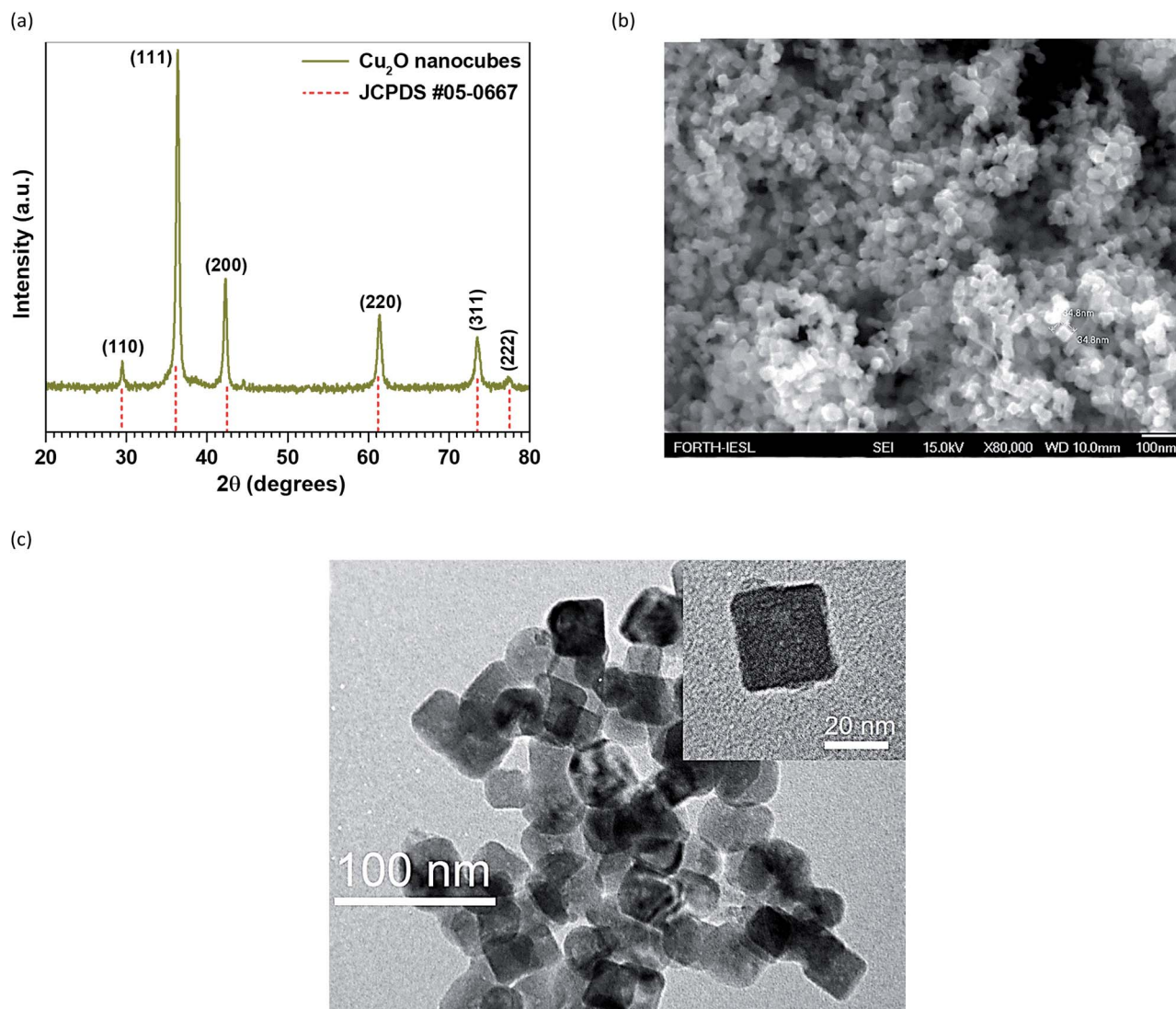


Fig. 2 (a) X-ray diffraction (XRD) pattern of Cu₂O nanocubes and standard Cu₂O card. (b and c) FESEM images and TEM images of Cu₂O nanocubes.

consistent with the p-type conductivity in Cu₂O nanocubes since an oxidizing gas such as ozone was expected to remove electrons from the top of the valence band of the semiconductor leading to an increased concentration of holes²¹ – a process that is discussed in details below. Once the ozone flow is turned off and ambient air is re-injected into the test chamber, the current of the Cu₂O nanocube channel reduces to almost its original value of $\approx 0.525 \mu\text{A}$ (see the current level following exposure to 10 ppb ozone). Although, exposure of the sensor to higher ozone concentrations lead to significantly higher current, the latter does not appear to return to its original value following exposure to ambient air for approximately 1 min. This can be attributed to a residual oxidation caused by the amount of ozone.

It is clear from the data shown in Fig. 5a that as the O₃ concentration increases from 10 to 490 ppb both response (30 s) and recovery times (18 s) of the sensor remain stable, with the only exception being the O₃ concentration of 820 ppb where the

response time decreased to 24 s and the recovery time increased to 24 s. The gas sensitivity of the sensor as a function of ozone concentration at room temperature is shown in Fig. 5b, from which it can be seen that it is decreased by increasing O₃ analytic concentration. The reason for this might be the low working temperature (*i.e.* 25 °C), compared with previous studies in which a T_{work} of 175 °C was employed.¹⁷ More specifically, this is the first report on the use of Cu₂O nanocubes as a self-powered sensing element for the detection of ultra-low O₃ concentrations down to 10 ppb with the highest response value of 28% and a response/recovery time of 30/18 s, respectively, at room temperature.

The experimental data presented so far suggest that O₃ species interact with the Cu₂O nanocrystals, while this interaction allows the whole process to follow in time the periodic supply of ozone molecules to the sample. In order to elucidate possible atomic-scale mechanisms that underlie the key experimental findings, we performed extensive DFT calculations on



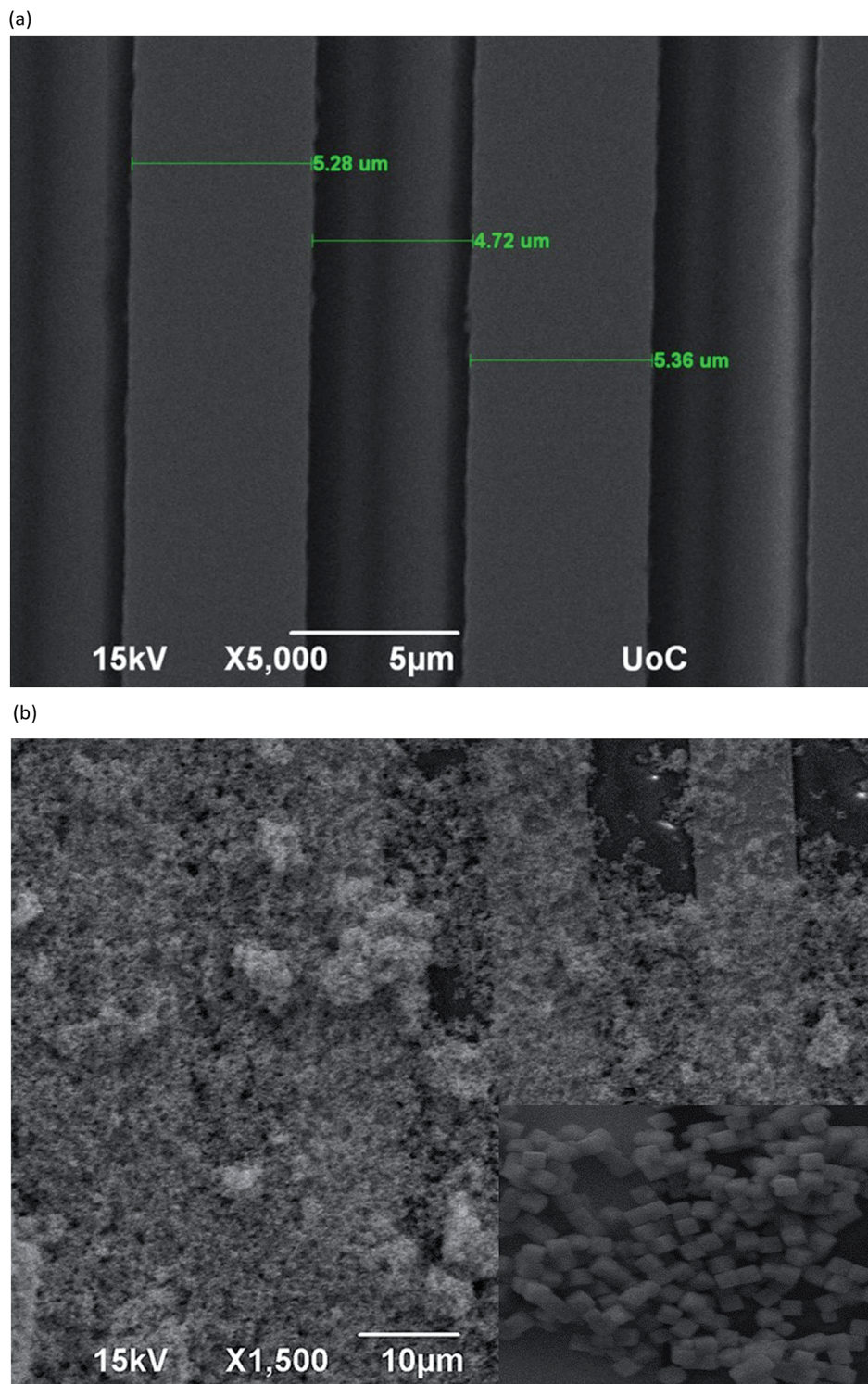


Fig. 3 (a) SEM images of the IDEs with a gap of 5 μm . (b) SEM of coated IDEs and zoomed view of the coated IDEs with nanocubes in the inset.

the adsorption of O_2 and O_3 molecules on (001) surfaces, given that (001) facets dominate Cu_2O nanocubes,⁸ while (110) and (111) terminations appear, respectively, only as truncated edges and corners.³³

First, we should note that the calculated LUMO value (-5.65 eV) is lower than the measured³¹ valence band maximum (-5.3

eV) of Cu_2O . Hence, any physisorbed O_3 species should act as electron acceptors for Cu_2O . By the same token, ozone molecules can interact directly with the Cu_2O facets. We found that when these facets have low oxygen content (close to the value associated with the stoichiometry of Cu_2O), O_2 and O_3 molecules chemisorb to configurations with large binding energies





The main picture that emerges from these calculations is the following. If Cu₂O nanocrystals are not O-rich in the beginning, then the deposition of electronegative oxygen atoms (through, *e.g.*, the dissociation of O₃ molecules) contributes to the p-doping of the material. Taking into account also the experimental findings on enhanced hole conductivity, the main reactions during this first stage can be described schematically as:

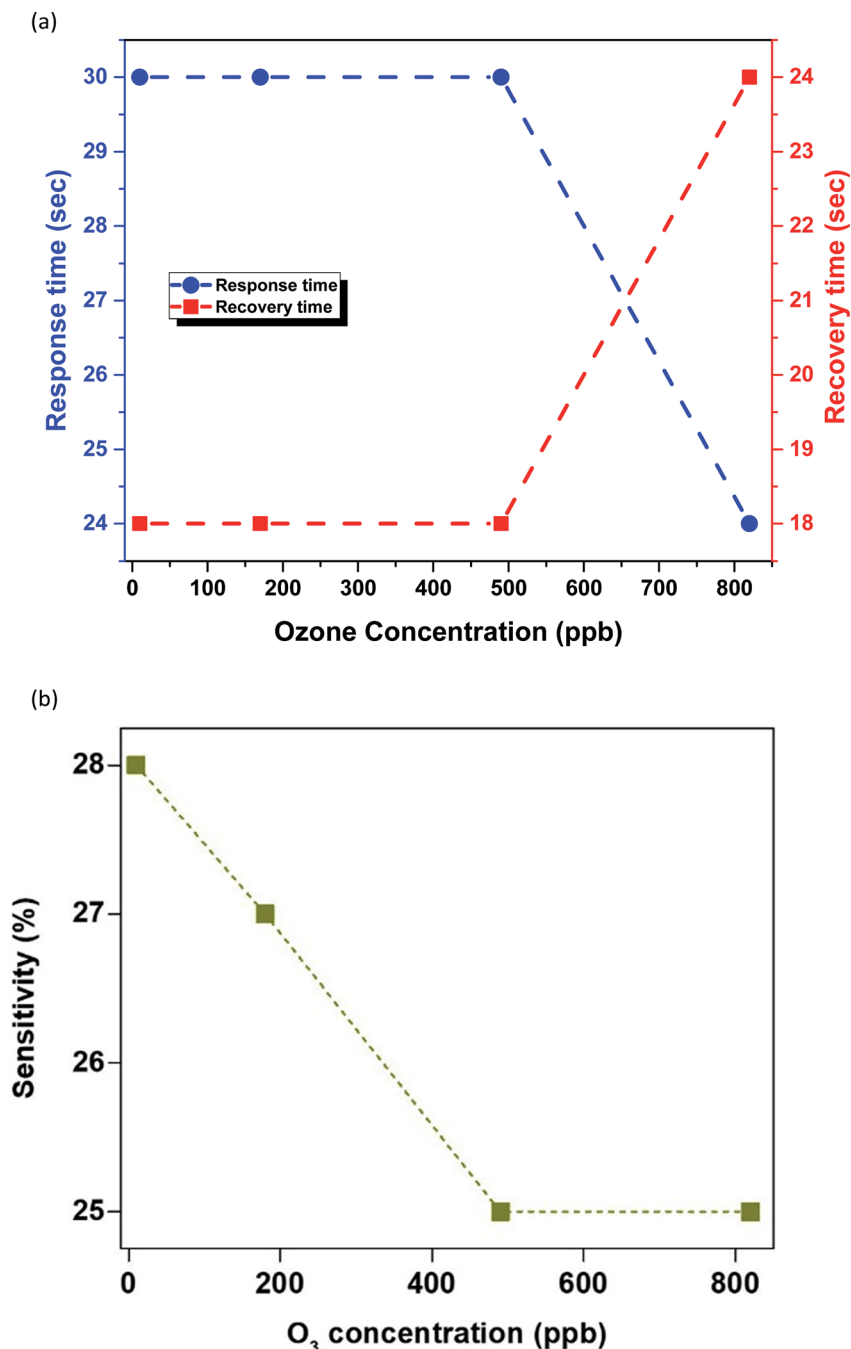
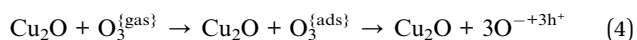
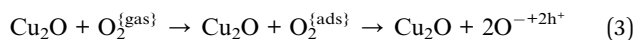
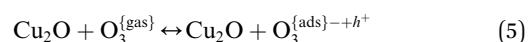


Fig. 5 (a) Response and recovery time (s) of the sensor at different ozone concentrations. (b) Sensing sensitivity as a function of ozone concentration.



When the nanocrystal facets are sufficiently oxidized (a condition which is plausible, but which also depends on the details of growth and operation), then they can selectively trap O₃ molecules with binding energies that are neither very large (so that the process may still be reversible) nor very small (so that it can lead to sensing of even small amounts of ozone). This second stage can be described as:



This atomic-scale picture is consistent with the broad features observed in the experiments. Nevertheless, we should stress that the high reactivity of the material (which also results in large local distortions upon oxygen uptake) leaves open the possibility that other adsorption mechanisms may also be important here. Future studies will explore, for example, the role of humidity or of surface reconstructions.

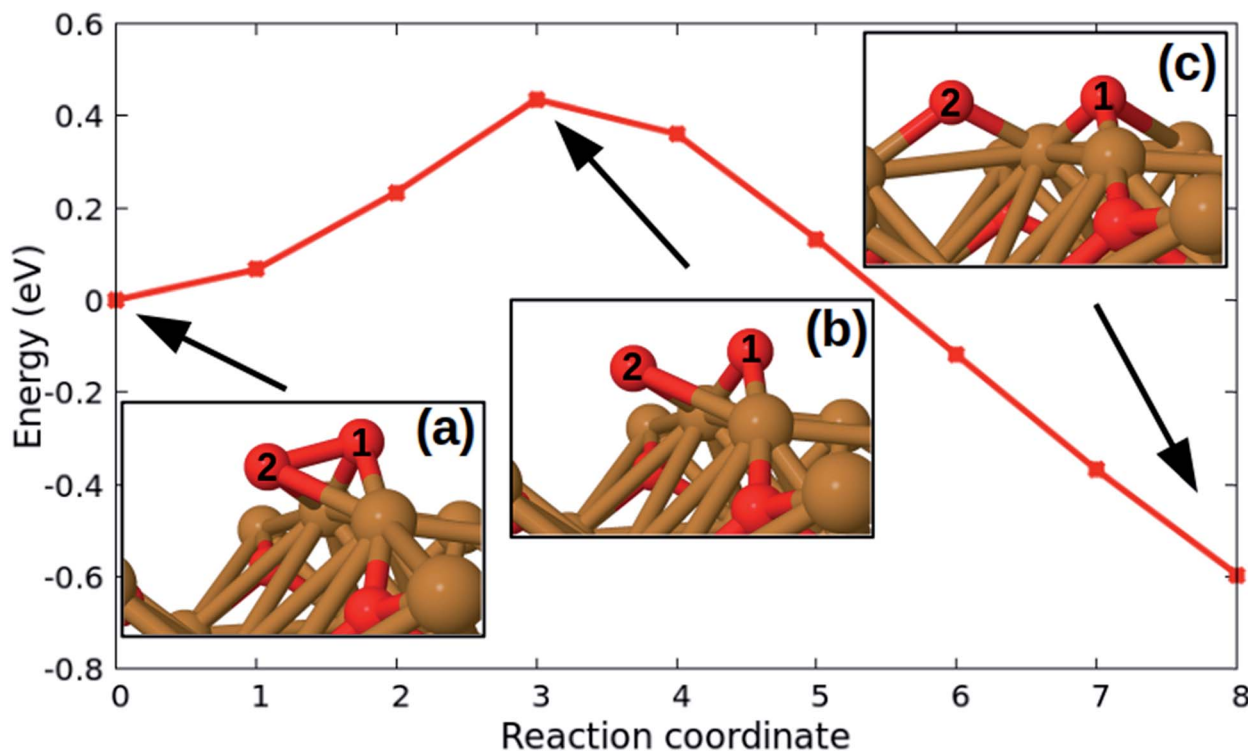


Fig. 6 Energy variation during a typical oxidation reaction on a (001) Cu_2O surface. An O_2 molecule (its atoms are numbered 1 and 2) chemisorbs with a zero barrier to configuration (a), followed by its breakup to atomic O adatoms and structures (b) and (c). The transition state of the reaction is (b) and the barrier is low and equal to 0.43 eV.

On the basis of the results and analysis presented so far one can argue that there are a few plausible reasons responsible for the fact that the current does not fully recover upon re-exposure of the sensor to ambient air (Fig. 4). The first reason is that the amount of air inserted into chamber for the given recovery (reset) period (~ 1 min) is not enough to completely decrease the number of holes that are being created by the adsorption of O_3 on Cu_2O during the

exposure time. Increasing the recovery period would therefore help to reduce the current closer to its original value. Another reason for the incomplete current recovery is dissociation kinetics associated with O_3 desorption from the surface of Cu_2O at room temperature. This issue could potentially be addressed by operating the sensor at elevated temperature and/or through photo-assisted dissociation albeit at the cost of operational simplicity.

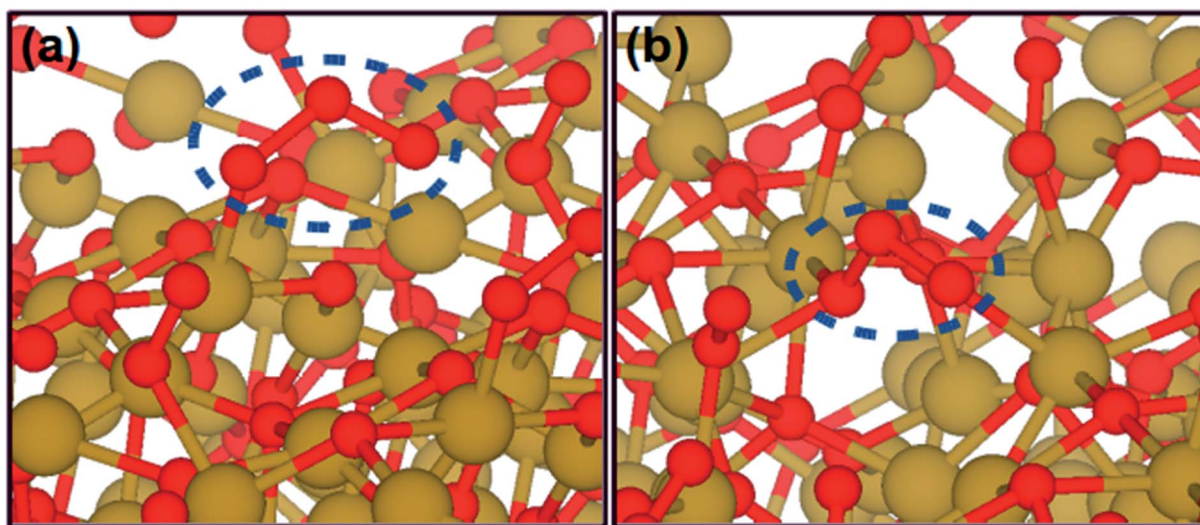


Fig. 7 Top views of O_3 species over a (001) Cu_2O surface: (a) a chemisorbed O_3 protrusion (dashed line) with one Cu–O bond. (b) An O_3 -related bridge (dashed line) between surface Cu atoms. The O_3 moiety forms three O–Cu bonds. (Cu: brown, O: red spheres).



Conclusions

In summary, cuprous oxide nanocubes were successfully synthesized by a solution-based method at room temperature. When the Cu₂O nanocubes were incorporated as the sensing element on IDEs, the resulting sensing element showed excellent sensitivity to O₃ in the range of 10 to 820 ppb, with fast response and recovery times. Importantly, the self-powered sensing elements of Cu₂O nanocubes exhibited a high response (28%) at relatively low ozone concentration (10 ppb) with response and recovery times of 30 and 18 s, respectively. Finally, the p-type nature of the Cu₂O nanocubes was confirmed, as the device current was found to increase in the presence of a strongly oxidizing gas, such as ozone.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

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