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Bose–Einstein oscillators and the excitation mechanism of free excitons in 2D layered organic–inorganic perovskites

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Following intense research on two-dimensional (2D) materials, there has been a resurgence of interest in 2D layered hybrid organic–inorganic perovskites. These 2D perovskites have direct band gaps regardless of their thickness. Excitons are confined to monolayers because of the materials' self-organized quantum-well electronic structure. Gaining insight into the exciton dynamics is central to understanding the light–matter interactions in 2D organic–inorganic perovskites. Herein, we investigate the free-exciton dynamics in 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite, demonstrating an anomalous temperature variation of the photoluminescence (PL) energy, which deviates from the conventional Varshni formula and is consistent with the behaviour of Bose–Einstein oscillators. The acoustic phonons induced by the coherent lattice motion of the atoms result in a positive temperature variation. Two-pulse emission modulation measurements reveal the excitation mechanism of the strong two-photon PL in $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite, in which two photons are simultaneously absorbed through a virtual state.

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Introduction

Hybrid organic–inorganic $\text{CH}_3\text{NH}_3\text{PbX}_3$ ($\text{X} = \text{I}, \text{Br}, \text{Cl}$) perovskites exhibit strong solar absorption, long electron–hole diffusion lengths and low trap densities.¹ Thus, they show fascinating prospects for use in high-efficiency, low-cost solar cells.^{2–10} The efficiencies of such solar cells exceed 20%.^{11–13} All-inorganic halide perovskites (CsPbX_3) synthesized in the form of colloidal quantum dots have also attracted intense interest because of their high quantum yields of up to 90%.^{14–17} To investigate the occurrence of two-dimensionally confined properties, ultra-thin $\text{CH}_3\text{NH}_3\text{PbX}_3$ perovskite single-crystal flakes have been prepared through mechanical exfoliation,¹⁸ chemical vapour deposition (CVD)^{19,20} and solution self-assembly.²¹ The high crystal quality and symmetrical geometries of $\text{CH}_3\text{NH}_3\text{PbX}_3$ perovskites result in high quality factors (Q), which can result in random lasing in whispering gallery mode. However, the crystal structure of a $\text{CH}_3\text{NH}_3\text{PbX}_3$ perovskite is three-dimensional (3D) rather than layered (2D), and consequently, it is difficult to obtain $\text{CH}_3\text{NH}_3\text{PbX}_3$ monolayers.

Nonetheless, ultra-thin single-crystal $\text{CH}_3\text{NH}_3\text{PbI}_4$ with a single unit cell of ~ 1.3 nm in thickness has recently been synthesized,²² and its photoluminescence (PL) peaks were found to exhibit a surprising dependence on the flake thickness.

The crystal geometries of organic–inorganic hybrid $\text{R}(\text{CH}_2)_n\text{NH}_3\text{MX}_m$ perovskites depend on the tolerance factor t , defined as $t = \sqrt{2}(R_M + R_X)/(R_{\text{R}(\text{CH}_2)_n\text{NH}_3} + R_X)$, where $R_{\text{R}(\text{CH}_2)_n\text{NH}_3}$, R_M and R_X are the ionic radii of the corresponding substances. In the case that the radii of the organic chain are larger than that of propylamine, an organic–inorganic hybrid $\text{R}(\text{CH}_2)_n\text{NH}_3\text{MX}_4$ perovskite will adopt a 2D layered structure.²³ Hence, there are on-going efforts to develop 2D layered perovskites in the form of $\text{R}(\text{CH}_2)_n\text{NH}_3\text{MX}_4$ monolayers. Such 2D layered organic–inorganic halide $\text{R}(\text{CH}_2)_n\text{NH}_3\text{PbX}_4$ perovskite materials exhibit a self-organized quantum-well electronic structure (Fig. 1a), consisting of alternating ~ 0.6 nm inorganic layers and ~ 1 nm organic layers.^{24–26} They exhibit strong solar absorption, large exciton binding energies and small Bohr radii, which endow these $\text{R}(\text{CH}_2)_n\text{NH}_3\text{PbX}_4$ materials with excellent optical properties, such as sharp resonant emission with a narrow full width at half maximum (FWHM) and a high quantum yield.²⁷ Previous reports have demonstrated that the PL peaks of $\text{R}(\text{CH}_2)_n\text{NH}_3\text{MX}_4$ perovskites can be tuned within the visible-infrared range by adjusting the organic component, R; the metal cation, M ($\text{M} = \text{Pb}, \text{Sn}, \text{Ge}$); and the halide, X ($\text{X} = \text{I}, \text{Br}, \text{Cl}$).^{28–30} Recently, single- and few-layer $(\text{C}_4\text{H}_9\text{NH}_3)_2\text{PbBr}_4$ single-crystalline perovskite squares have been successfully prepared *via* a solution-

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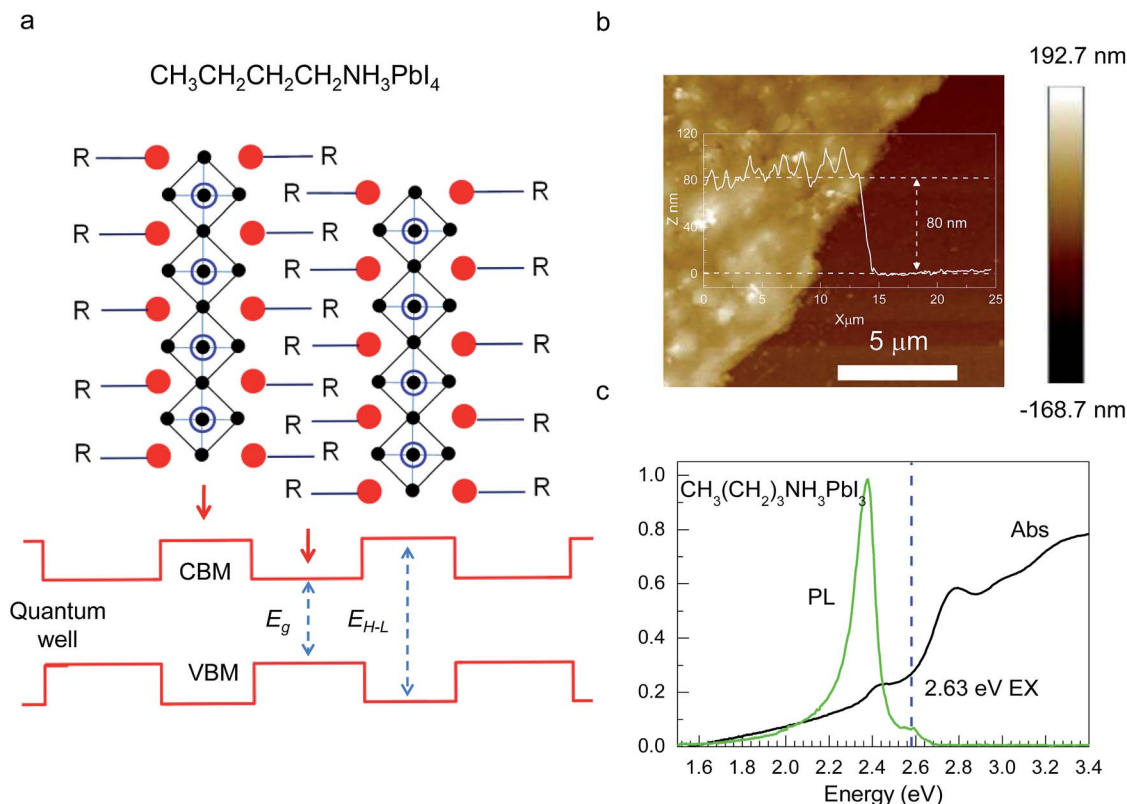


Fig. 1 (a) Schematic illustration of 2D layered $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{NH}_3\text{PbI}_4$ perovskite and its quantum-well electronic structures. (b) AFM image of a $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{NH}_3\text{PbI}_4$ perovskite film spin coated on quartz. (c) Absorption and photoluminescence spectra of the 2D perovskite at room temperature.

phase growth method. The optical band gap of the 2D square sheets was found to be slightly blue-shifted by 40 meV compared with that of the bulk crystal, but it was otherwise nearly indistinguishable for configurations ranging from 1 to 22 layers.²³ In addition, mechanical exfoliation has been applied to produce 2D few-layer $(\text{C}_6\text{H}_5\text{C}_2\text{H}_4\text{NH}_3)_2\text{PbI}_4$ perovskites, in which strong anti-Stokes PL results in laser cooling by ~ 58.7 K.³¹ However, the nature of the excitons in 2D layered $\text{R}(\text{CH}_2)_n\text{NH}_3\text{MX}_4$ perovskites is still not well understood.

Herein, we investigate the exciton dynamics in 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite in the range of 10–300 K by means of PL spectroscopy and two-pulse emission modulation (TPEM) spectroscopy. Interestingly, we find that the variation of the PL peak energy as a function of temperature deviates from Varshni's empirical expression; the phase transition occurs in the range of 200–250 K. Below 200 K, the band gap energy first increases to a maximum of ~ 2.374 eV at 150 K but then monotonically drops to ~ 2.364 eV at 13 K as the temperature decreases. We demonstrate that Bose–Einstein oscillation contributes to the positive temperature variation of the PL peak energy as a result of free excitons. We also investigate the excitation mechanism of two-photon photoluminescence (TPPL), in which two photons are simultaneously absorbed through a virtual state to excite a single electronic transition. Our work reveals the mechanisms underlying exciton dynamics and excitation in 2D perovskites.

Experiment

$\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{I}$ synthesis and film preparation

$\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{I}$ was synthesized using the reported method.³² Briefly, 1.5 mL of $\text{CH}_3(\text{CH}_2)_3\text{NH}_2$ was added to 50 mL of ethanol under Ar gas and stirred for 30 min at 0 °C. Subsequently, 1 mL of hydroiodic acid (55 wt% in water, Sigma-Aldrich) was added. The mixed solution was stirred for a further 2 h. The white raw product $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{I}$ was obtained through rotary evaporation at 50 °C, washed three times with diethyl ether, and then finally recrystallized from a mixed solvent of diethyl ether and ethanol. The white solid was dried in vacuum for 24 h and stored in a glovebox. Then, 138 mg of PbI_2 and 105 mg of $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{I}$ were dissolved in 2.31 mL of DMF. A volume of 20 μL of the mixed solution was spin coated onto quartz with dimensions of $1 \times 1 \text{ cm}^2$ at 2000 rpm for 2 min, and the samples were then placed in vacuum for 24 h for the removal of residual DMF solvent.

TPPL measurements

The TPPL spectra were measured using a home-built two-photon optical microscope. A mode-locked Ti:sapphire oscillator (TiF-100M, Avesta) was used as the excitation source, generating 80 fs pulses with a central wavelength of 785 nm and repetition rate of 84.5 MHz. The laser beam was passed through a 785/10 nm band-pass filter (LD01-785/10-25, Semrock), 5×





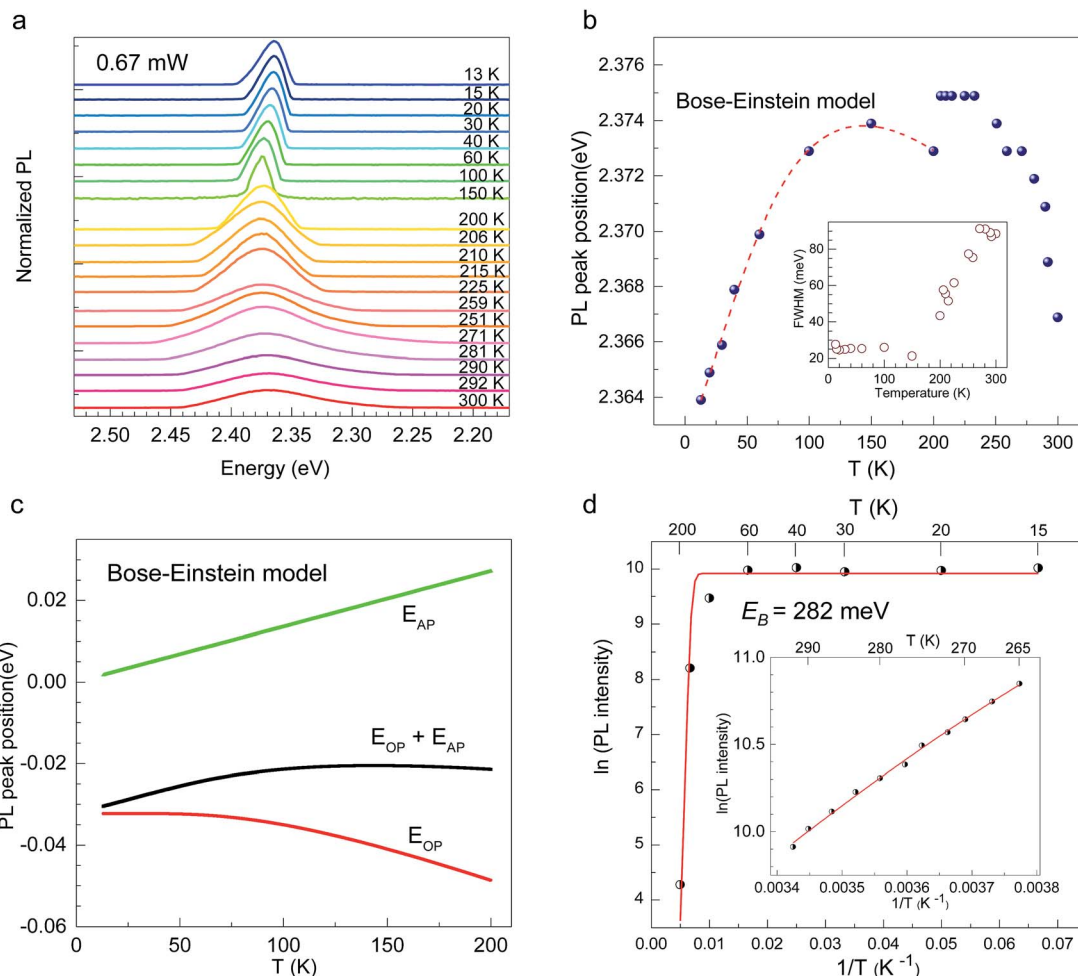


Fig. 2 (a) PL spectra of 2D layered $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{NH}_3\text{PbI}_4$ perovskite for temperatures from 13 to 300 K. (b) PL peak energy vs. temperature, fitted using the Bose–Einstein oscillator model (dashed red curve). The inset shows the FWHM as a function of temperature. (c) The optical and acoustic phonon energies as functions of temperature in the Bose–Einstein oscillator model. (d) PL intensity as a function of temperature. The exciton binding energy is ~ 282 meV.

role in determining the electronic structure.^{41,47} The optical transitions in 2D perovskites thus stem from the 6s to 6p transition in Pb^{2+} , which is similar to that in PbI_2 . Because $\text{Pb}(207)$ has a larger atomic mass than $\text{I}(126)$, the Pb atoms undergo Bose–Einstein oscillation at a low frequency that induces acoustic phonons, whereas the I atoms predominantly exhibit high-frequency Bose–Einstein oscillations, resulting in optical phonons. The electron–phonon interactions critically depend on the amplitudes of the phonons and the corresponding coupling constants. Thus, the temperature dependence of the free-exciton emission energy $E_g(T)$ should be related to that of both the optical phonon energy, $E_{\text{OP}}(T)$, and the acoustic phonon energy, $E_{\text{AP}}(T)$:^{39,40}

$$E_{\text{OP}}(T) = A_1 \left[\frac{2}{\exp(E_1/k_B T) - 1} + 1 \right], \quad (3)$$

$$E_{\text{AP}}(T) = A_2 \left[\frac{2}{\exp(E_2/k_B T) - 1} + 1 \right], \quad (4)$$

$$E_g(T) = E_0 + E_{\text{OP}}(T) + E_{\text{AP}}(T), \quad (5)$$

where E_1 and E_2 are the average energies of the Einstein oscillators corresponding to the optical and acoustic phonons, respectively; A_1 and A_2 describe the strength of the electron–phonon interactions, if negative, indicate that the band gap energy decrease with increasing temperature; k_B and T are the Boltzmann constant and temperature, respectively. Fig. 2b shows the fit of the experimental PL peak energy data to a model based on two types of Bose–Einstein oscillators (red dashed curve). The E_0 value obtained by fitting the data is ~ 2.39 eV. The average energies of the optical (E_1) and acoustic (E_2) phonons are 27.5 meV and 0.028 meV, respectively, and A_1 and A_2 are -32.3 meV and 0.022 meV, respectively. Fig. 2c shows the energies of the optical and acoustic phonons as functions of temperature. The acoustic phonon function E_{AP} is positive and monotonically increases with increasing temperature, whereas the optical phonon function E_{OP} shows the opposite trend, monotonically decreasing as the temperature increases.



Moreover, $|E_{OP}| > |E_{AP}|$. Thus, the total phonon function satisfies $(E_{AP} + E_{OP}) < 0$, resulting in an excitonic energy $E_g(T)$ is smaller than E_0 and shows a non-monotonic variation. Thus, the coherent lattice motion of the atoms in 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ films below 150 K induces acoustic phonons, resulting in an increase in the PL peak energy. However, the out-of-phase movements of the atoms in the lattice dominate above 150 K, giving rise to optical phonons and consequently causing the PL peak energy to decrease. Therefore, the temperature-dependent behaviour of the acoustic and optical phonons results in the non-monotonic temperature variation of the PL peak energy. Free excitons are confined in the quantum-well structure of 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite, giving rise to a large exciton binding energy. Further analysis of the temperature dependence data yields insight into the free-exciton binding energy.

Fig. 2d shows the PL intensity as a function of $1/T$ under laser excitation at 4.88 eV; the plot indicates that the PL intensity first gradually increases and then dramatically decreases as the temperature increases. Under steady-state excitation, the

temperature dependence of the PL intensity can be expressed as⁴⁸

$$I(T) = \frac{I_0}{1 + \eta \exp(-E_B/k_B T)}, \quad (6)$$

where $I(T)$ and I_0 are the PL intensities of $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ at T and 0 K, respectively, and E_B is the exciton binding energy. By fitting the experimental data using eqn (6) (Fig. 2d) in the regions of 15–200 and 265–300 K, the exciton binding energy E_B is estimated to be ~ 282 meV. This value is ~ 14.8 times larger than that of 3D $\text{CH}_3\text{NH}_3\text{PbI}_4$ (~ 19 meV),⁴⁹ suggesting that the 2D material can be utilized as active elements for excitonic devices,^{50,51} such as for excitonic energy transfer.^{52–54}

$\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ exhibits excellent non-linear optical properties. A home-built two-photon optical microscope was used to investigate the TPPL of $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite.⁵⁵ Fig. 3 shows the one- and two-photon photoluminescence (OPPL and TPPL) spectra of the 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ films under pulsed laser excitation at 3.1 and 1.55 eV. The PL intensity shows a linear relationship with the excitation power

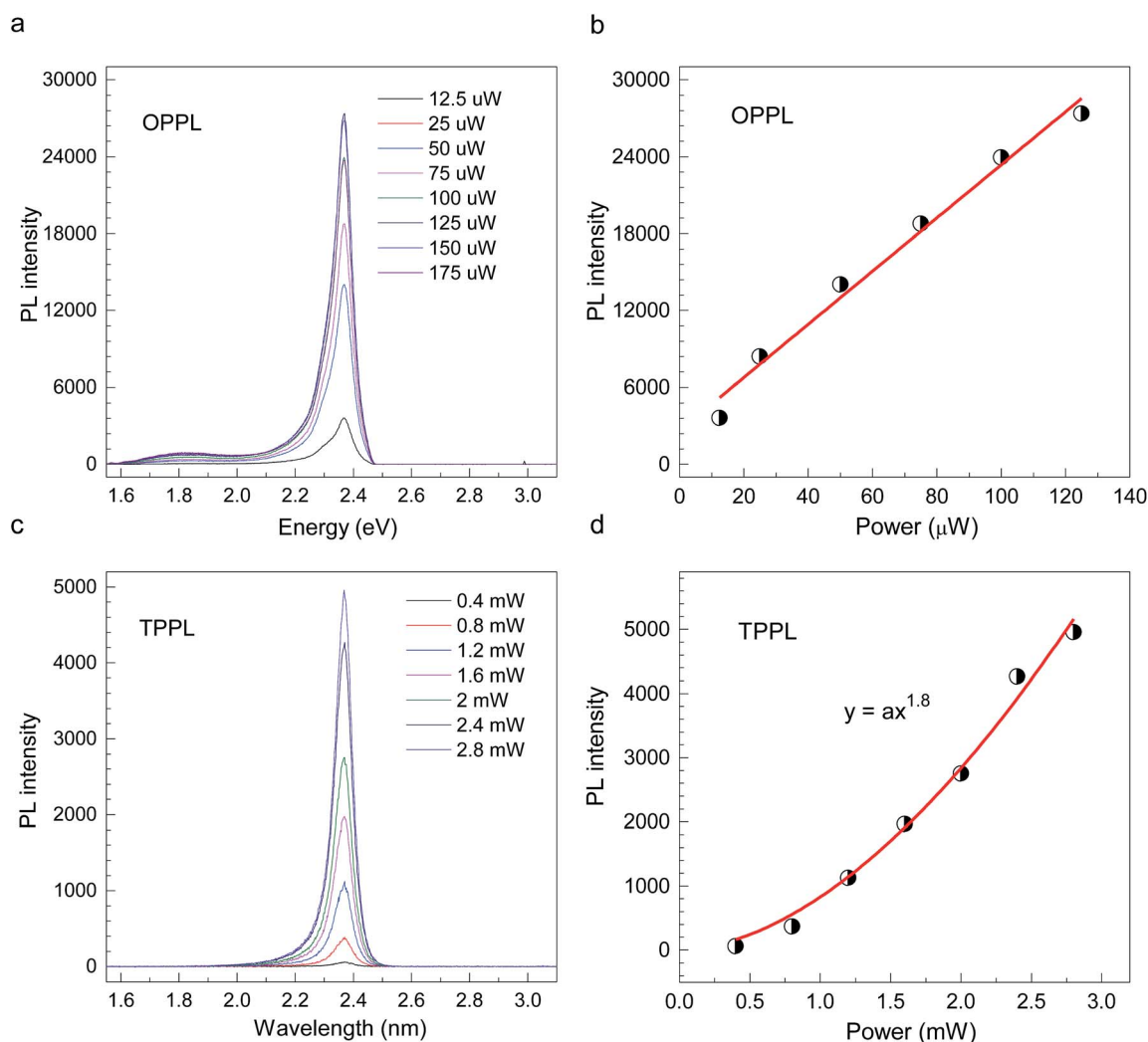


Fig. 3 (a and b) OPPL spectra and (c and d) TPPL spectra of 2D layered $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{NH}_3\text{PbI}_4$ perovskite films at room temperature.



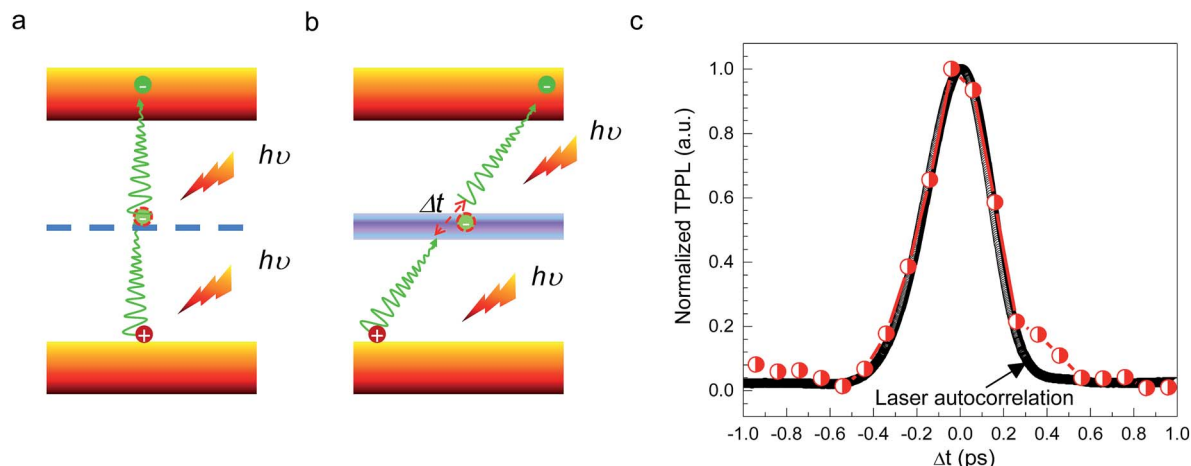


Fig. 4 (a and b) Schematic illustrations of two excitation mechanisms: (a) coherent two-photon absorption through a virtual state and (b) two sequential one-photon absorptions through real intermediate states. (c) TPEM measurement of 2D layered $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{NH}_3\text{PbI}_4$ perovskite (BAP1) at room temperature.

under optical pumping with 3.1 eV (Fig. 3a and b). Under 1.55 eV excitation, an exponential relationship between PL intensity and excitation power is observed, which can be well fitted using the function $y = ax^{1.8}$ (Fig. 3c and d), indicating the occurrence of TPPL. Considering the long tails of the absorption spectrum of the 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ films (Fig. 1c), two possible excitation mechanisms may be responsible for the TPPL, namely, a coherent two-photon absorption process or two sequential one-photon absorption processes. The schematic excitation diagrams of these processes are displayed in Fig. 4, respectively. In the coherent two-photon absorption model, two photons are absorbed simultaneously to drive a single electron from the VB into the CB *via* a virtual intermediate state (Fig. 4a). In the sequential one-photon absorption model, two photons are absorbed sequentially, mediated by a real intermediate state between the VB and CB (Fig. 4b).

To investigate the TPPL excitation mechanism of the 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ films, two-pulse emission modulation (TPEM) measurements were conducted to probe the correlated effects of two pulses on the observed PL emission.⁵⁶ Two 1.55 eV femtosecond laser pulses with similar power were focused onto a 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ film with a good spatial overlap. The TPPL intensity was recorded as a function of the time delay (Δt) between the two laser pulses. In this configuration, the recorded TPPL emission has two possible origins: (1) two photons from the same laser excitation pulse and (2) two photons from different excitation pulses. It is easy to see that the contribution from the former process is independent of the time delay between two laser pulses, as the excitation photons originate from the same pulse. By contrast, the latter represents the cross-contribution of two individual laser pulses to the TPPL; thus, its contribution is maximal when the two pulses temporally overlap and decreases in intensity as they temporally separate. In the case of the coherent two-photon absorption model, the TPEM curve should show the same profile as that of the laser pulses because the emission originates from the simultaneous absorption of two photons

through a virtual state. In the case of sequential one-photon excitations, the two one-photon excitation processes occur at the time scale of the lifetime of the real intermediate state; consequently, the TPEM dynamics should follow the lifetime of the intermediate state, similar to our previous reported TPPL excitation mechanism of gold nanorods.⁵⁶ As shown in Fig. 4c, the measured TPEM curve of $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite exhibits a FWHM of ~ 360 fs, which is consistent with the laser autocorrelation profile. These results suggest that the TPPL in $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite is excited through the coherent two-photon absorption mechanism (Fig. 4a).

Conclusions

In 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite films, we observed a non-monotonic temperature variation of the PL peak energy in which the acoustic phonon energy exhibits a positive temperature variation, which is attributed to Bose–Einstein oscillation, whereas the optical phonon energy displays the opposite behaviour. The dielectric confinement effect due to the quantum-well structure of the material strengthens the Coulomb interaction between an electron and a hole, imparting the $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite with a large exciton binding energy of ~ 282 meV and thus providing an opportunity to study the exciton dynamics. The nonlinear optical properties of TPPL in 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite were also observed, and we confirmed that the excitation is driven by a coherent two-photon absorption mechanism. The strong electron–phonon interactions and large exciton binding energy in 2D layered $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskite suggest its potential for use for high-efficiency excitonic energy transfer in lighting and display applications.

Author contributions

B. P. and K. P. L. conceived and supervised the experiment. B. P. synthesized $\text{CH}_3(\text{CH}_2)_3\text{NH}_3\text{PbI}_4$ perovskites. H. Z. and Q. X.



carried out two photon PL measurements and TPPEM measurement. J. L., Y. L., L. B., H. L., J. X., L. D., L. Z., X. W. carried out the absorption and low temperature PL measurement. All authors discussed the results and wrote the manuscript.

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