


 Cite this: *Soft Matter*, 2025, 21, 3347

## Chain dynamics in polyisoprene stars with arms linked by dynamic covalent bonds to the central core†

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Although the use of dynamic covalent bonding (DCB) is a promising method to obtain easily recyclable polymer networks, there are many aspects of the incorporation of dynamic covalent bonding into polymer systems that remain poorly understood. In order to gain insight into the fundamentals of these materials, well-controlled model systems are required. Here, we present the synthesis of polyisoprene (PI)-based 3-arm stars containing vinylogous urethane DCBs as linkers of the PI arms to the core of the star. The dynamics of these 3-arm stars, with three different arm sizes, is studied by broadband dielectric spectroscopy. A conventional (static) 3-arm PI star of intermediate size has also been synthesized and studied, and all results are directly compared with those of a linear PI chain. A prominent intermediate relaxation between those identified as the slower normal mode and the faster  $\alpha$ -relaxation of PI is found in the stars containing DCBs. This relaxation, which becomes more significant as the molecular mass of the PI arms decreases, seems to originate from the dynamic bond exchange that occurs at the level of the star's core. On the other hand, the arm retraction dynamics responsible for the normal mode relaxation do not show significant differences with respect to that observed in the static star.

 Received 28th January 2025,  
 Accepted 28th March 2025

DOI: 10.1039/d5sm00091b

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## 1 Introduction

Polymers with dynamic covalent bonds (DCBs) have attracted increasing scientific interest due to their reversible bond formation and the broad range of features and functionalities they present, like shape memory, self-healing, responsiveness, improved stretchability, high toughness, malleability, and reprocessability, among others.<sup>1–6</sup> Furthermore, replacing permanent chemical bonds with dynamic bonds transforms regular thermosets into reconfigurable materials known as covalent adaptable networks (CANs).<sup>2,6–17</sup>

In terms of their interaction nature, DCBs are a unique class of bonds that merge the dynamic properties of supramolecular chemistry with the stability of covalent interactions.<sup>18,19</sup> These bonds can reversibly break and reform in response to external stimuli (temperature, light, pH, *etc.*) through associative (new bonds form along with the breaking of old ones) or dissociative (bonds break first, followed by new bond formation) exchange mechanisms.<sup>6,20</sup> In this regard, imine and vinylogous urethane bonds are among the most extensively studied associative DCBs.<sup>18,20,21</sup> They are formed through the condensation reaction between amines and carbonyl or acetoacetate groups, respectively. However, the stability of imine bonds under certain conditions can be a limitation, leading to the development of vinylogous urethanes as an alternative.<sup>22</sup> These bonds exhibit enhanced stability due to their conjugated structure, where the enamine and keto forms are stabilized by intramolecular hydrogen bonding. Unlike conventional urethanes, vinylogous urethanes have increased reactivity, allowing for thermally induced transamination reactions with or without a catalyst *via* Michael addition–elimination or iminium-based pathways.<sup>20,23</sup>

Extensive studies on small model molecules have provided critical insights into the dynamic behavior of CANs and

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† Electronic supplementary information (ESI) available: Details on materials, instrumentation, synthetic methods, and dielectric characterization of linear PI and static PI stars. See DOI: <https://doi.org/10.1039/d5sm00091b>



vinylous urethanes.<sup>22–25</sup> However, model dynamic polymers, well-defined in terms of molecular architecture, composition, and molecular weight with low dispersity, are essential for understanding the structure–property relationships and dynamics within the family of dynamic polymer materials. Anionic polymerization has been one of the most reliable methods for synthesizing model complex macromolecular architectures with static bonds, such as diblocks, stars, grafts, rings, *etc.*, serving as benchmark systems for a detailed quantitative analysis.<sup>26–35</sup> Consequently, anionic polymerization and post-functionalization reactions<sup>36,37</sup> can serve as a synthetic pathway for dynamic model polymers. Despite this progress, a notable gap remains in the synthesis and study of model polymers incorporating DCBs. Polymers with DCBs present relaxation mechanisms with different timescales and length scales, making it possible to tune their viscoelastic properties. A deep understanding at a molecular level of the role played by the DCB in the macroscopic properties is still missing, while there is no clear understanding of the influence of the segmental relaxation in the bond exchange mechanism yet.<sup>14</sup>

In that sense, broadband dielectric spectroscopy (BDS) is a well-suited technique due to its sensitivity to dipole fluctuations, which allows unraveling the dynamics at a molecular level. This is of particular interest for studying the bond exchange process of the DCBs and how that process affects the dynamics of the whole chain.<sup>38</sup> To this end, a thorough investigation can help to understand the role played by the dynamics of the bonds in the structure–property relationship in CANs. For this purpose, the synthesis and characterization of polyisoprene (PI)-based vitrimers (associative CANs) with imine dynamic bonds has been reported, providing new insights into the vitrimer's dynamics, and highlighting the necessity of model polymers.<sup>39</sup> Using PI chains of different lengths and varying the cross-link concentration, model polymers with a constant chain length between dynamic linkages were obtained. In a complete structural study carried out in those vitrimers, a clustering of the cross-linkers was observed by X-ray diffraction.<sup>40</sup> Besides, in a dielectric study, the fluctuation of the dipole moment of the cross-linker was detected. Interestingly, the fluctuation of those dipoles occurs in a concerted way with the PI segments close to the chain ends. Furthermore, type-A polymers<sup>41</sup> like PI present a net dipole moment related to the chain end-to-end vector, allowing the observation of the so-called normal mode (NM) by dielectric spectroscopy, which involves the entire chain motion. In the case of the PI vitrimers with imine dynamic bonds, the full reorientation of the end-to-end vector is hindered, but limited fluctuations of the chain ends presumably occur inside the clusters of cross-linkers.<sup>42</sup>

Macromolecular architectures incorporating DCBs, such as stars, are ideal systems for simplifying the topological complexity introduced by DCBs in CANs. Additionally, recent studies have shown that PI star polymers with static bonds, when used as additives in isofrictional blends with linear PI, effectively reduce the mixture's viscosity through the constraint release mechanism.<sup>43,44</sup> Thus, star polymers through DCBs represent a promising new class of rheological agents, enhanced by the dynamic character of their core.

Considering these factors, we present, for the first time, the synthesis of 3-arm star PI model dynamic polymers *via* anionic polymerization followed by post-functionalization reactions and vinylous urethane chemistry, by varying the arm molecular weight (2, 5, and 11 kg mol<sup>-1</sup>) and we address their dynamics using BDS. Three relaxation processes are detected in the melt state: slow and fast relaxations corresponding to the NM and the  $\alpha$ -relaxation respectively, and an intermediate mode attributed to the dipolar fluctuation of the DCB. Additionally, one model 3-arm star PI through static bonds was synthesized and used as a reference for comparative analysis.

## 2 Materials and methods

### 2.1 Materials

The synthesis and characterization of the 3-arm star PI polymers is extensively described in the Results section. The materials and instrumentation used for the synthesis and characterization of the samples are detailed in ESI.† The synthetic procedure of the final dynamically bonded PI stars is represented in Scheme 1a. The trifunctional cross-linker links the flexible PI chains *via* DCBs. The synthesis route for the 3-arm star PI with static covalent bonds is depicted in Scheme 1b. Additionally, a linear PI was used for reference, synthesized by anionic living polymerization as described in the ESI of ref. 45. All the experiments were performed within a month from the synthesis date. To confirm that the properties of the samples remained unchanged, size exclusion chromatography (SEC) experiments were performed before and after the experiments.

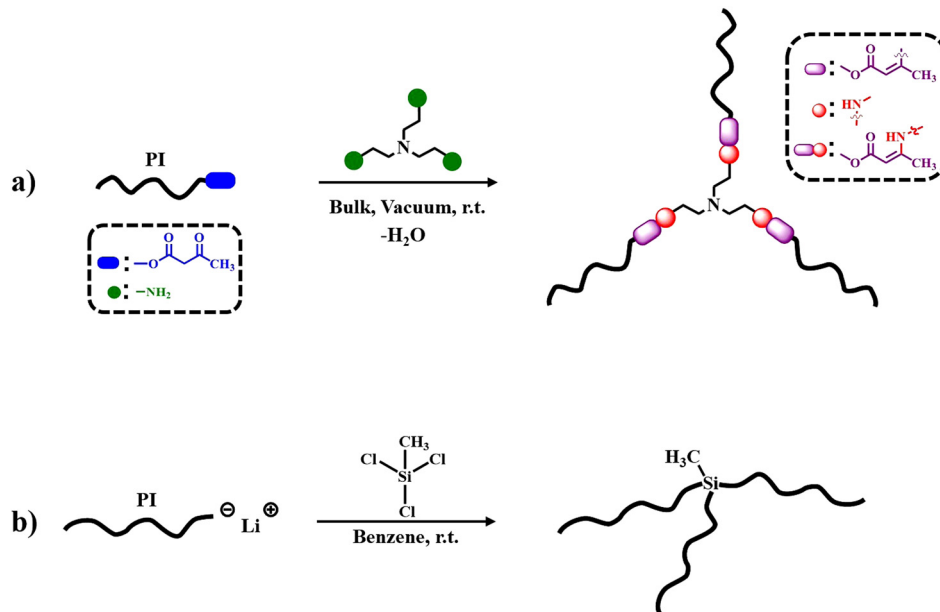
### 2.2 Methods

**2.2.1 Dielectric spectroscopy.** The complex dielectric permittivity was measured in the range 10<sup>-2</sup> to 10<sup>6</sup> Hz, using a Novocontrol Technologies Alpha A impedance analyzer. The sample was sandwiched between two gold-plated brass electrodes (diameter 10 mm) using a 50  $\mu$ m Teflon spacer forming a parallel plate capacitor. The sample was held in a cryostat from Novocontrol, and exposed to a nitrogen gas stream. Both temperature and dielectric measurements were computer-controlled. Measurements were performed at temperatures ranging from 180 to 340 K, on heating and cooling with different temperature steps, being stabilized to 0.5 K.

When conducting dielectric measurements in rubber-like materials, the thickness of the sample capacitor is affected by diverse factors, such as the normal force applied to ensure good electric contact, which changes with temperature due to thermal expansion. To overcome this problem and be able to compare the dielectric permittivity of the DCB stars with those reported for linear PI,<sup>46,47</sup> the values of the complex dielectric permittivity were re-scaled by comparing the residual high-frequency permittivity  $\epsilon_\infty$  at a temperature well below the glass transition temperature (190 K), assuming that at that temperature the physical mechanism contributing to  $\epsilon_\infty$  is mainly the induced polarisation.

**2.2.2 Small-angle X-ray scattering.** Experiments were performed in a Rigaku 3-pinhole PSAXS-L equipment using CuK $\alpha$ ,





**Scheme 1** Schematic representation of the reactions between (a) PI-AcAc and tris(2-aminoethyl)amine (TAEA) forming a dynamic 3-arm star PI, and (b) living PI and methyltrichlorosilane generating a 3-arm star PI with static covalent bonds.

transition photons of wavelength  $\lambda = 1.54 \text{ \AA}$ . The Dectris EIGER2 R 1M is a water-cooled hybrid-photon-counting (HPC) detector offering a micrometric spatial resolution ( $75 \mu\text{m} \times 75 \mu\text{m}$ ) over an active area of  $77.1 \text{ mm} \times 79.65 \text{ mm}$  with 1 M pixels. After azimuthal integration, the scattered intensities were obtained as a function of the modulus of the scattering vector  $Q = 4\pi \sin(\theta/2)/\lambda$ , where  $\theta$  is the scattering angle. Reciprocal space calibration was done using silver behenate as standard. Samples were placed in transmission geometry, with a sample-to-detector distance of 0.5 m, covering a  $Q$ -range between 0.05 and  $0.9 \text{ \AA}^{-1}$  by combining 9 different detector positions with a  $3 \times 3$  detector scan profile. Measurements under vacuum in isothermal conditions were performed employing a Linkam Scientific Instruments THMS600 temperature controller with temperature stability of 0.1 K. Measuring times were of 400 s for each scan.

**2.2.3 Modulated differential scanning calorimetry.** Differential scanning calorimetry (DSC) measurements were carried out on samples of approximately 5 mg encapsulated in aluminum pans using a Q2000 TA instrument with a liquid nitrogen cooling system with  $25 \text{ mL min}^{-1}$  helium flow rate. Indium melting was utilized for temperature and heat flow calibrations. Temperature-modulated experiments (MDSC) were performed using a sinusoidal variation of 0.5 K amplitude and 60 s period. Data were acquired during heating and cooling at  $3 \text{ K min}^{-1}$  over the temperature range 180 to 340 K.

## 3 Results

### 3.1 Synthesis and characterization

For the first time, model dynamic 3 arm-star PI [ $d\text{-}(\text{PI})_3$ ], was synthesized through anionic polymerization<sup>27,28,30</sup> and vinyllogous

urethane chemistry<sup>22,25</sup> as depicted in Scheme 1. Additionally, a 3-arm star PI [ $(\text{PI}_{6k})_3$ ] with static covalent bonds was synthesized according to the literature<sup>29,48</sup> and served as a reference for comparison in the BDS dynamic study. Specifically, three different  $\omega$ -hydroxy functionalized polyisoprenes (PI-OH) were synthesized with molecular weights of 2, 5, and  $11 \text{ kg mol}^{-1}$  (Table S1, ESI<sup>†</sup>). Standard high vacuum techniques and custom-made glass apparatuses were employed to synthesize well-defined PI-OH polymers. *s*-BuLi initiated the isoprene polymerization in a benzene solution at room temperature while ethylene oxide and methanol served as end-capping and terminating agents, as depicted in Scheme S1a (ESI<sup>†</sup>). Subsequently, the reaction of PI-OH with *tert*-butyl acetoacetate produced  $\omega$ -acetoacetate functionalized polyisoprenes (PI-AcAc) (Table S2 and Scheme S2, ESI<sup>†</sup>). Following this, three  $d\text{-}(\text{PI})_3$  with PI arm molecular weights of 2, 5, and  $11 \text{ kg mol}^{-1}$ , were synthesized by the condensation reaction of PI-AcAc with tris(2-aminoethyl)amine (TAEA) in a 3:1.02 molar ratio, in bulk under vacuum at room temperature (Table 1 and Scheme 1a). Additionally, one 3-arm star PI with  $M_n$  (PI-arm)  $\sim 6 \text{ kg mol}^{-1}$ , labeled as  $(\text{PI}_{6k})_3$ , was synthesized *via* static covalent bonds (Table 1, Scheme 1b and Scheme S1b, ESI<sup>†</sup>). Initially, isoprene was anionically polymerized with *s*-BuLi in benzene at room temperature to generate the living  $\text{PI}_{6k}$  arm. A coupling reaction was followed between methyltrichlorosilane and the living PI arm in a 1:0.95 molar ratio of PI arm to  $-\text{Cl}$ , forming the 3-arm star PI. The pure 3-arm star  $\text{PI}_{6k}$ , free from the unreacted PI arm, was isolated using the fractionation technique. Furthermore, the dynamic associative behavior of the PI macromolecular architectures was experimentally investigated and confirmed by reacting  $d\text{-}(\text{PI}_{2k})_3$  with aniline as illustrated in Scheme S3 (ESI<sup>†</sup>).<sup>25</sup> All linear precursors (PI-OH, PI-AcAc, and PI arm) and the corresponding 3-arm star PI were characterized by SEC, <sup>1</sup>H NMR and FT-IR analysis. All the PI-OH exhibited low dispersity



**Table 1** Molecular characteristics and glass transition temperatures ( $T_g$ ) of 3-arm star PI via vinylogous urethane bonds, and 3-arm star PI via static covalent bonds

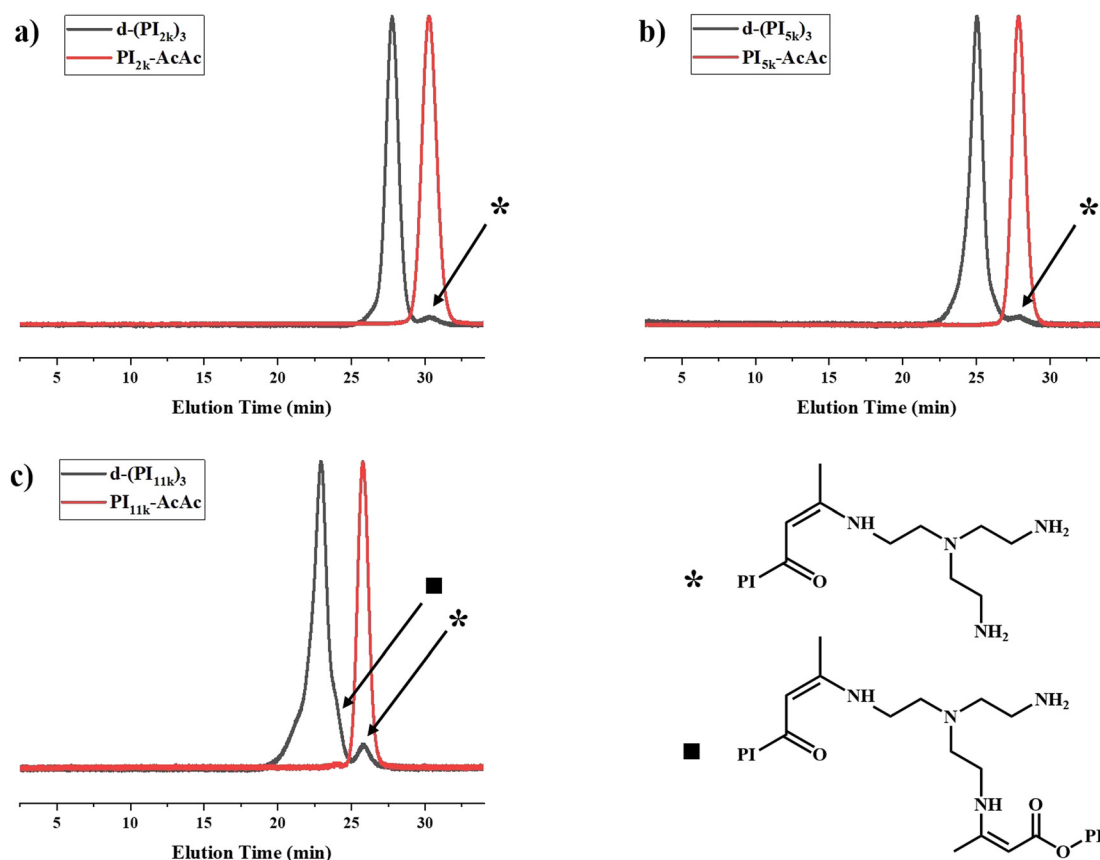
Sample	$M_n^a$ (g mol <sup>-1</sup> )	$D^a$ main peak	1,4 microstructure <sup>b</sup> (mol%)	3,4 microstructure <sup>b</sup> (mol%)	$T_g^c$ (K)
d-(PI <sub>2k</sub> ) <sub>3</sub>	5500	1.04	89.7	10.3	211.3
d-(PI <sub>5k</sub> ) <sub>3</sub>	14 700	1.07	92.2	7.8	212
d-(PI <sub>11k</sub> ) <sub>3</sub>	33 300	1.13	92.4	7.6	212.3
(PI <sub>6k</sub> ) <sub>3</sub>	18 200	1.02	93.0	7.0	210

<sup>a</sup> From SEC (THF, 35 °C, calibrated with PI standards). <sup>b</sup> Determined by <sup>1</sup>H NMR spectroscopy (500 MHz, chloroform-*d*, 25 °C). <sup>c</sup> From the inflection point of reversing heat flow curve obtained from modulated DSC measurements, determined from cooling cycles.

( $D = M_w/M_n \leq 1.06$ ) and Gaussian molecular weight distribution, as shown in Fig. S1a (ESI<sup>†</sup>). The specific conditions and use of Schlenk techniques for the acetoacetylation of PI-OH yielded well-defined PI-AcAc, free from dimer byproducts, as indicated by the SEC traces in Fig. S1b (ESI<sup>†</sup>). The SEC trace corresponding to the PI<sub>6k</sub> arm, of the (PI<sub>6k</sub>)<sub>3</sub>, shows a small side peak to the left of the main peak corresponding to dimers formed during the aliquot termination with methanol under air. The SEC trace of the fractionated (PI<sub>6k</sub>)<sub>3</sub> star reveals a well-defined product free of unreacted PI arm (Fig. S2, ESI<sup>†</sup>).

The formation of well-defined 3-arm star PI *via* vinylogous urethane bonding was challenging due to the system's dynamic chemistry (Scheme 1). To ensure that no unreacted PI-AcAc remained and to promote catalyst-free transamination within the system,<sup>22</sup> a 2% excess of TAEA was used in all cases,

producing a small number of mono and di-arm star PI chains with free -NH<sub>2</sub> functionality, as shown in Scheme S4 (ESI<sup>†</sup>). The formation of d-(PI)<sub>3</sub> was verified by the appearance of the high molecular weight traces in the SEC chromatograph, as depicted in Fig. 1. A minor right-side peak appeared in the chromatogram for all three d-(PI)<sub>3</sub>, which can be attributed to the one-arm structure, as illustrated in Scheme S4 (ESI<sup>†</sup>). Noticeably, in the case of the d-(PI<sub>11k</sub>)<sub>3</sub>, the system appeared to reach equilibrium after about 10 days, with only minor changes thereafter. According to SEC, besides the main peak corresponding to the d-(PI<sub>11k</sub>)<sub>3</sub>, two additional peaks on the right are attributed to the two-arm and one-arm structures. An explanation for that could be that the higher steric hindrance of the PI<sub>11k</sub>-AcAc ( $M_n = 11$  kg mol<sup>-1</sup>) restricts the complete formation of the 3-arm star, compared to the lower molecular weight of d-(PI<sub>2k</sub>)<sub>3</sub>



**Fig. 1** SEC traces of 3-arm star PI [d-(PI)<sub>3</sub>] with molecular weight of PI-AcAc (a) 2 kg mol<sup>-1</sup>, (b) 5 kg mol<sup>-1</sup>, and (c) 11 kg mol<sup>-1</sup> in THF at 35 °C.



and  $d\text{-(PI}_{5k})_3$ . The dynamic behavior of the vinylogous urethane architectures was examined using SEC.  $d\text{-(PI}_{2k})_3$  was mixed with an excess of aniline at room temperature, where no change was detected in the SEC traces after 24 hours due to the slow kinetics of the transamination reaction. However, upon heating to 130 °C, the  $d\text{-(PI}_{2k})_3$  peak almost disappeared, with a small peak appearing corresponding to the 2-arm structure, along with the main peak of  $d\text{-PI}_{2k}\text{-Ph}$  as shown in Fig. S3 and Scheme S3b (ESI<sup>†</sup>).

Subsequently, <sup>1</sup>H NMR analysis was conducted, confirming the success of the synthetic steps in this study. The PI-OH spectrum shows a characteristic peak at 3.60 ppm (designated as **a** in Fig. S5, ESI<sup>†</sup>) for the terminal  $\text{-CH}_2\text{-OH}$  protons (2H). A signal appeared at 5.13 ppm (1H) corresponding to the olefinic protons of the PI backbone (1H), and a multiplet at 4.7–4.68 ppm attributed to the vinyl group protons ( $\text{-C=CH}_2$ ). Additionally, the 1,4 microstructure of PI precursors was estimated to range from 90% to 93%. The successful acetoacetylation of  $\text{PI}_{2k}\text{-OH}$  was confirmed by the disappearance of the  $\text{-CH}_2\text{-OH}$  protons signal at 3.60 ppm (assigned as **a**) and the appearance of three new signals:  $\text{-CH}_2\text{-O-}$  at 4.07 ppm (assigned as **b**, **m**), ( $\text{O=C-CH}_2\text{-C=O}$ ) at 3.43 ppm (assigned as **c**, **s**) and ( $\text{O=C-CH}_3$ ) at 2.27 ppm (assigned as **d**, **s**), as shown in Fig. S6a (ESI<sup>†</sup>). Similar spectra were observed for  $\text{PI}_{5k}\text{-AcAc}$  and  $\text{PI}_{11k}\text{-AcAc}$  as shown in Fig. S7a and S8a (ESI<sup>†</sup>). The condensation reaction of PI-AcAc and TAEA was also analyzed by <sup>1</sup>H NMR, confirming the formation of vinylogous urethane bonds and the successful synthesis of  $d\text{-(PI)}_3$  (Fig. S6b, ESI<sup>†</sup>). In more detail, the  $d\text{-(PI}_{2k})_3$  spectrum shows the disappearance of the characteristic peaks of  $\text{PI}_{2k}\text{-AcAc}$  at 3.43 ppm and 2.27 ppm. Additionally, some new proton signals are observed and assigned as follows: two multiplets appear at 8.69–8.57 ppm, attributed to the nitrogen proton ( $\text{-CH}_2\text{-NH-}$ ) (designated as **h**), two signals appear at 4.53–4.43 ppm corresponding to the ( $\text{O=C-CH=CH-}$ ) proton (designated as **j**), and a multiplet at 3.90 ppm that assigned to ( $\text{H}_2\text{C-CH}_2\text{-O-C=O}$ ) (designated as **k**). Furthermore, a multiplet signal shows at 3.25 ppm, attributed to ( $\text{N-CH}_2\text{-CH}_2\text{-NH}$ ) (designated as **g**), with another multiplet at 2.68 ppm assigned to ( $\text{N-CH}_2\text{-CH}_2\text{-NH}$ ) (designated as **f**).  $d\text{-(PI}_{5k})_3$  and  $d\text{-(PI}_{11k})_3$  show similar <sup>1</sup>H NMR spectra to that of  $d\text{-(PI}_{2k})_3$  (Fig. S7 and S8b, ESI<sup>†</sup>), confirming the successful synthesis across all molecular weights. Fig. S9 (ESI<sup>†</sup>) shows the <sup>1</sup>H NMR spectrum of the 3-arm PI star synthesized through static covalent bonds,  $(\text{PI}_{6k})_3$ , similar to the precursor of  $\text{PI}_{6k}\text{-arm}$ . The peak at 5.13 ppm (designated as **a**) corresponds to the olefinic protons of the PI backbone, while the peaks at 4.7–4.68 ppm (designated as **b**) are assigned to the vinyl group protons ( $\text{-C=CH}_2$ ). A comparison of the integrations of these signals reveals that the microstructure of the star  $(\text{PI}_{6k})_3$  consists of 93% 1,4 units and 7% 1,3 units.

Along with SEC and <sup>1</sup>H-NMR, FT-IR analysis was conducted at all steps of the synthesis. The FT-IR spectrum of  $\text{PI}_{2k}\text{-OH}$  displays a broad signal at 3330  $\text{cm}^{-1}$  corresponding to the O-H stretching band, and two peaks at 1643  $\text{cm}^{-1}$  and 1663  $\text{cm}^{-1}$ , attributed to the  $\text{-C=C-}$  vibrations of the PI backbone<sup>49</sup> as shown in Fig. S10 (ESI<sup>†</sup>). The acetoacetylation of  $\text{PI}_{2k}\text{-OH}$  was also confirmed *via* FT-IR (Fig. S11, ESI<sup>†</sup>). More specifically, the

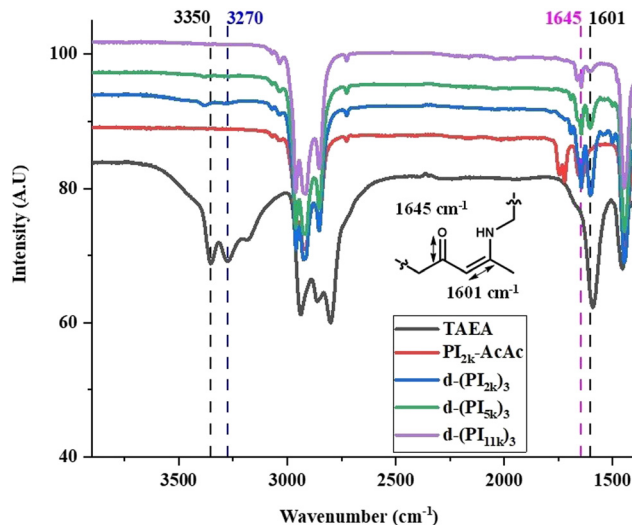


Fig. 2 FT-IR spectra of the linear precursor  $\text{PI}_{2k}\text{-AcAc}$ , TAEA, and the 3-arm PI stars  $[d\text{-(PI)}_3]$  through vinylogous urethane chemistry.

*t*-butyl acetoacetate precursor exhibits two characteristic signals at 1712  $\text{cm}^{-1}$  and 1738  $\text{cm}^{-1}$ , corresponding to the ketone and ester carbonyl groups, respectively.<sup>22</sup> Similar signals (1722  $\text{cm}^{-1}$  and 1738  $\text{cm}^{-1}$ ) appeared in the case of  $\text{PI}_{2k}\text{-AcAc}$  confirming the effective functionalization by *t*-butyl acetoacetate. Furthermore, the formation of  $d\text{-(PI}_{2k})_3$  through vinylogous urethane chemistry is confirmed firstly by the near disappearance of the  $\text{-NH}_2$  bands of TAEA at 3350  $\text{cm}^{-1}$  and 3270  $\text{cm}^{-1}$ , a weak residual signal remains attributed to the 2% excess of TAEA, and second from the disappearance of the acetoacetate vibrational band at 1722  $\text{cm}^{-1}$  and 1738  $\text{cm}^{-1}$ . Additionally, two new bands emerge at 1601  $\text{cm}^{-1}$ , and 1645  $\text{cm}^{-1}$  attributed to the C=C and C=O groups of the vinylogous urethane (Fig. 2). The FT-IR analysis was primarily conducted on the 2 kg  $\text{mol}^{-1}$  samples due to the lower molecular weight for enhanced signal clarity. Similar results were obtained for the 5 and 11 kg  $\text{mol}^{-1}$ , as depicted in Fig. 2. It is worth noting that initial evidence suggests that these systems remain stable for approximately 50 days when stored under a dynamic vacuum at room temperature. However, side reactions occurred beyond this period, forming static covalent bonds, and the system gradually nearly lost its dynamic character. The system remains fully stable when stored in a non-polar solvent (cyclohexane, benzene) under vacuum at  $-20$  °C. Additional experiments and studies are required to elucidate the long-term transformations of this complex system.

### 3.2 Dielectric study

The dielectric response of the DCB stars with a  $M_n$  of 5 kg  $\text{mol}^{-1}$  per arm at a temperature about 42 K above  $T_g$  is shown in Fig. 3. In this temperature range the main relaxation components are well within the experimental frequency window. Data corresponding to a linear PI of  $M_n = 6$  kg  $\text{mol}^{-1}$  ( $\text{LPI}_{6k}$ ) as well as those corresponding to the PI 3-arm star with static covalent bonds of the same  $M_n$  [ $(\text{PI}_{6k})_3$ ] are also included for comparison.



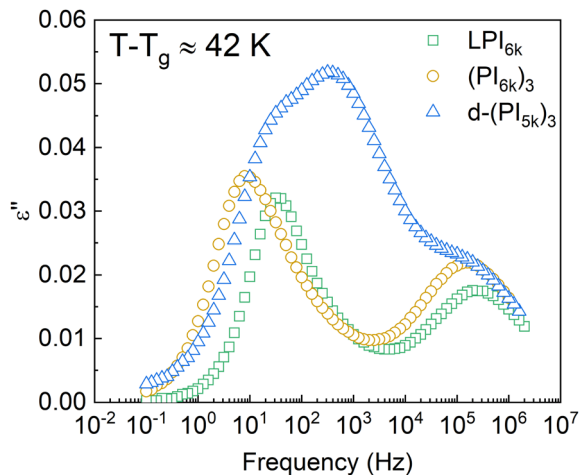


Fig. 3 Imaginary part of the dielectric permittivity of several PI samples: 6 kg mol<sup>-1</sup> linear PI (green squares), 6 kg mol<sup>-1</sup> static star (yellow circles), and d-(PI<sub>5k</sub>)<sub>3</sub> (blue triangles). For each sample, the represented temperature is about 42 K above its calorimetric  $T_g$ .

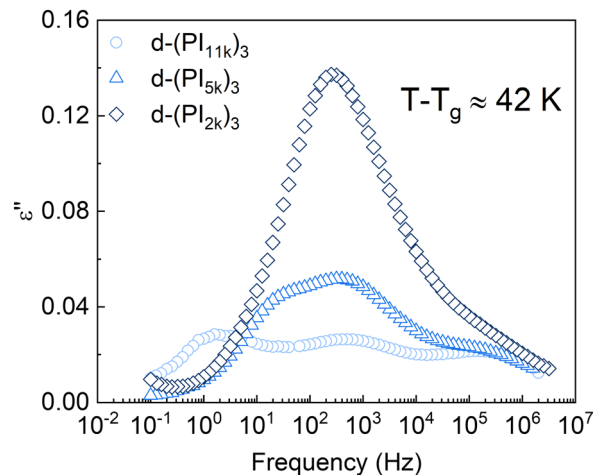


Fig. 4 Imaginary component of the dielectric permittivity for the different PI stars. For each sample, the selected temperature is about 42 K above its calorimetric  $T_g$ .

As can be observed, while the dielectric spectra of LPI<sub>6k</sub> and (PI<sub>6k</sub>)<sub>3</sub> show two well-resolved relaxation processes, the signal measured for the DCB stars is more complex. In the linear PI and statically bonded star, it is known that the high-frequency process is due to the segmental relaxation (also known as  $\alpha$ -relaxation) and the low-frequency one is attributed to the end-to-end vector reorientation of the PI chains (normal mode, NM),<sup>50,51</sup> and is related with the so-called arm retraction in the case of the stars. In the DCB stars, besides these two relaxation processes detected at similar frequencies, there is a pronounced increase in the intensity of the signal at intermediate frequencies, so large that it appears as a third peak in the spectra. This particularity in the spectra was also found in mono- and di-functionalized linear polyisoprenes bearing hydroxyl (OH-) end-group(s), where a third peak in the frequency range between the segmental process and the global chain relaxation was observed, attributed to the relaxation of segments in the vicinity of the H-bonded groups.<sup>52</sup>

In Fig. 4 we show a comparison of the DCB stars with different molecular weight per arm. It can be observed that the intensity of the mid-frequency relaxation process increases as the  $M_n$  of the arm decreases, that is, with the volume fraction of functional cores: the d-(PI<sub>11k</sub>)<sub>3</sub> spectrum shows 3 clear peaks of similar height, while in the d-(PI<sub>5k</sub>)<sub>3</sub> the intensity of the central peak increases and the normal mode one—which shifts toward higher frequencies as the chain shortens<sup>53</sup>—is visible as a low-frequency shoulder of that central peak; in the d-(PI<sub>2k</sub>)<sub>3</sub> the signal of the mid-frequency relaxation is even more intense, to the point that the NM and the  $\alpha$ -relaxation are both hidden by this peak. The correlation between the intensity of the mid-frequency process and the volume fraction of functional cores in the samples suggests that this relaxation mode is associated with the dipole reorientation of the functional cores.

To gain insight into the molecular origin of the relaxation components observed in these stars, we analyzed the dependence with the temperature of the characteristic frequencies

obtained from the maxima of the peaks by simple inspection. We selected the d-(PI<sub>11k</sub>)<sub>3</sub> since, as already mentioned, in this sample the peaks corresponding to the three relaxation processes are better resolved (see Fig. 4). The obtained frequencies are represented in Fig. 5a (empty symbols) as a function of the reciprocal temperature. The temperature dependence of the frequencies follows the Vogel-Fulcher-Tamman (VFT) law:<sup>54</sup>

$$f_{\max}(T) = f_{\infty} \exp\left(-\frac{DT_0}{T - T_0}\right) \quad (1)$$

with  $f_{\infty}$  a pre-exponential factor,  $D$  the so-called fragility parameter, and  $T_0$  the Vogel temperature. A good description of the characteristic frequencies of the  $\alpha$ -relaxation is obtained (without any fitting parameters) by using the value of the pre-exponential factor reported for linear PI of similar  $M_n$ ,<sup>44</sup> and the values of the fragility and the Vogel temperature obtained for the linear reference polymer LPI<sub>6k</sub> (see ESI,† Table S4), after taking into account the differences in  $T_g$  between the two polymers. Particularly, the VFT parameters for the linear PI are:  $f_{\infty} = 2.5$  THz,  $D = 7.8$  and  $T_0 = 167$  K, and thus, the values of  $T_0$  for the other samples were taken as  $167 \text{ K} + (T_g^{\text{d-(PI)}_3} - T_g^{\text{LPI}_{6k}})$ , with  $T_g^{\text{LPI}_{6k}} = 208$  K.

For the NM, the values of  $D$  and  $T_0$  were fixed to those used for the  $\alpha$ -relaxation, and  $f_{\infty}$  was allowed as a fitting parameter. This provides a good description of the main part of the data set. Finally, we have found that the same type of approach also delivers a reasonable description of the intermediate relaxation associated with the DCB fluctuations (see Fig. 5a). These results indicate that the time-temperature superposition would also work as a good approximation in this type of material, suggesting that the DCB exchange is slaved to the segmental mobility, which also controls the temperature dependence of the normal mode relaxation.

This analysis can be extended to the other DCB stars considering only those components showing a clear peak in the



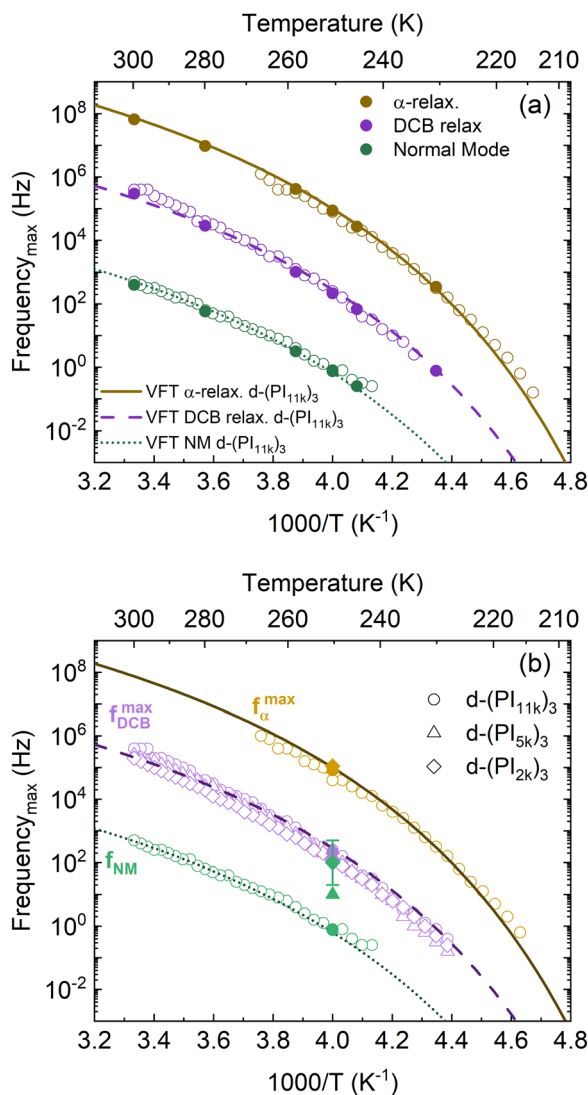


Fig. 5 Arrhenius plot of (a) the three peak maxima for the  $d\text{-(PI}_{11k})_3$  star and (b) the peak maxima for the main components of each recorded spectrum (see text for details). Empty symbols correspond to the values obtained from visual inspection of the loss curves. Solid symbols correspond to the results obtained from the BDS data analysis using eqn (2). Lines correspond to the VFT description of these frequencies (see legend).

recorded spectrum, meaning that in the case of  $d\text{-(PI}_{2k})_3$  and  $d\text{-(PI}_{5k})_3$  only a single peak is tracked. The values obtained in this way are shown in Fig. 5b. In this plot we have included as lines those used to describe the data already shown in panel a. An overall similar behavior is found for all the characteristic frequencies, confirming that the results obtained for  $d\text{-(PI}_{11k})_3$  can be extended to the whole set of samples investigated, at least within the present level of accuracy in the determination of the characteristic frequencies.

A complete description of the relaxation curves is required to properly resolve the characteristics of the three different relaxation contributions for each polymer and thus, go beyond the previous semi-quantitative analysis. To this end, the dielectric relaxation data have been described as a superposition of three

relaxation processes plus a term to account for DC conductivity,  $\sigma_{\text{DC}}$ , and other low-frequency effects:

$$\varepsilon^*(\omega) - \varepsilon_\infty = \varepsilon_{\text{NM}}^*(\omega) + \varepsilon_{\text{DCB}}^*(\omega) + \varepsilon_\alpha^*(\omega) - i \frac{\sigma_{\text{DC}}}{\omega \varepsilon_0}. \quad (2)$$

For the low-frequency mode, we used the Rouse-like description of the normal mode<sup>50</sup> where each mode contributes as a Cole–Cole relaxation process:<sup>55–58</sup>

$$\varepsilon_{\text{NM}}^*(\omega) = \Delta \varepsilon_{\text{NM}} \left( \sum_{k:\text{odd}} \frac{1}{k^2} \right)^{-1} \sum_{k:\text{odd}} \frac{1/k^2}{1 + (i\omega\tau_1/k^2)^{a_{\text{NM}}}}, \quad (3)$$

where  $\Delta \varepsilon_{\text{NM}}$  is the dielectric strength of the NM,  $\tau_1$  is the relaxation time of the first mode ( $f_{\text{NM}} = (2\pi\tau_1)^{-1}$ ) and  $a_{\text{NM}}$  describes the symmetric broadening of the chain-modes with respect to the Debye relaxation ( $a_{\text{NM}} = 1$ ). This broadening would reflect the effects of the dispersity  $\mathcal{D}$  of the arm sizes (see Table 1). Indeed, the relaxation mode distribution is broader for star-shaped polymers when compared to the linear counterparts,<sup>59</sup> as can be seen in Fig. 3 (green squares for linear PI and yellow circles for PI stars). Contributions from  $k \geq 9$  did not affect the description of our data.

The other two relaxation processes ( $\alpha$ -relaxation and DCB relaxation) have been described using the Havriliak–Negami (HN) function or its mirrored version (mHN),<sup>60–62</sup> depending on the direction of the asymmetrical broadening of the corresponding relaxation peak. In the case of the HN function, the peak may broaden asymmetrically toward higher frequencies, and it reads

$$\varepsilon_{\alpha,\text{DCB}}^*(\omega) = \frac{\Delta \varepsilon_{\text{HN}}}{[1 + (i\omega\tau_{\text{HN}})^{a_{\text{HN}}}]^{b_{\text{HN}}}}, \quad (4)$$

where  $\Delta \varepsilon_{\text{HN}}$  is the dielectric strength of the relaxation,  $\tau_{\text{HN}}$  is its HN time, and  $a_{\text{HN}}$  and  $b_{\text{HN}}$  are the symmetric and asymmetrical broadening of the process, respectively, and the condition  $0 < a_{\text{HN}} \leq 1$ ,  $a_{\text{HN}}b_{\text{HN}} < 1$  holds. The frequency of the maximum of the dielectric losses is related to the HN relaxation time by<sup>63</sup>

$$f_{\text{max}} = \frac{1}{2\pi\tau_{\text{HN}}} \left[ \sin\left(\frac{a_{\text{HN}}\pi}{2 + 2b_{\text{HN}}}\right) \right]^{1/a_{\text{HN}}} \left[ \sin\left(\frac{a_{\text{HN}}b_{\text{HN}}\pi}{2 + 2b_{\text{HN}}}\right) \right]^{-1/a_{\text{HN}}}. \quad (5)$$

The mirrored version of the HN equation can be written as<sup>62</sup>

$$\varepsilon_{\alpha,\text{DCB}}^*(\omega) = \Delta \varepsilon_{\text{mHN}} - \frac{\Delta \varepsilon_{\text{mHN}}}{[1 + (i\omega\tau_{\text{mHN}})^{-a_{\text{mHN}}}]^{b_{\text{mHN}}}}, \quad (6)$$

where the parameters have the same meaning as in eqn (4). In this case, the peak may extend asymmetrically to lower frequencies. The use of this less common HN-type functional form for the  $\alpha$ -relaxation can be justified by the different dynamic behavior between the chain segments close to the star core, and the rest of the PI segments: the reorientation of the former would be slower due to the additional constraints imposed by the relatively rigid core. On the contrary, the PI segments located far from the core in a PI-rich environment should experience a friction coefficient similar to that of linear PI and also exhibit a similar dielectric response. This has also



been observed in other systems, like block copolymers with high dynamical asymmetry, where segments of the component with lower  $T_g$  chains are attached to a rigid phase rich in a glassy component.<sup>64–67</sup> This results in a mobility gradient that reflects the different dynamics near and far from the rigid interfaces. The behavior described is also found in grafted polymers where the anchorage to a solid surface slows down and limits the segmental reorientation.<sup>68,69</sup>

In addition, some assumptions were made to limit the number of free parameters in the fitting process: (i) the relaxation time of the maximum of the  $\alpha$ -relaxation peak was fixed from the value determined in the linear PI after taking into account the differences in  $T_g$  values (see Table 1), as obtained from differential scanning calorimetry (DSC) (see ESI† for details); (ii) the ratio of the dielectric strengths  $\Delta\epsilon_{\text{NM}}/\Delta\epsilon_{\alpha}$  was fixed to the value obtained for the static star  $(\text{PI}_{6\text{k}})_3$ ; (iii) for each sample, the dielectric strength ratio  $\Delta\epsilon_{\text{DCB}}/\Delta\epsilon_{\alpha}$  was assumed to remain temperature independent.

The description obtained with these assumptions, together with the corresponding data at a given temperature, is shown in Fig. 6 for the three samples and, as can be seen, this fitting strategy provides a very good description of the rather complex relaxation curves. The parameters obtained from the fits for the data at 250 K are collected in Table 2.

The components contributing to the overall fitting curve obtained in this way allow a more accurate determination of the characteristics of each relaxation process, namely, peak frequencies and dielectric relaxation intensities. In particular, the peak frequencies determined from the fittings can be compared with those previously obtained from direct data inspection (see filled symbols in Fig. 5). This comparison shows that in the samples where the relaxation components are overlapping, there are some discrepancies. On the contrary, in the case of the  $\text{d}(\text{PI}_{11\text{k}})_3$  sample, when inspecting the values of the characteristic frequencies obtained by this type of fitting at several temperatures, the preliminary conclusions are fully confirmed (see Fig. 5a).

Regarding the dielectric strengths of the components obtained from the analysis, the data collected in Table 2 show that the relaxation intensities associated with the polymer dynamics are approximately the same for all the samples, within the experimental uncertainties. This could be expected due to the small amount of DCBs in all these systems (less than  $\approx 2\%$  wt). In this situation, the type and concentration of PI dipoles in the material remain essentially constant. On the contrary, important differences exist when considering the DCB component, with a clear correlation with the DCB concentration.

Fig. 7 shows the variation of the dielectric relaxation intensities of the DCB component as a function of the reciprocal of the arm mass, which is proportional to the volume fraction of DCB. A rather linear behavior with zero intersection is found, supporting the procedure used in the dielectric data fitting. From the slope of the fitting line, we can estimate the corresponding effective dipole moment  $\mu_{\text{DCB}}^{\text{eff}}$ , by assuming<sup>54,70</sup>  $\mu_{\text{DCB}}^{\text{eff}} \approx (\epsilon_0 k_{\text{B}} T \Delta\epsilon_{\text{DCB}}/n)^{1/2}$ , where  $\epsilon_0$  is the vacuum permittivity,

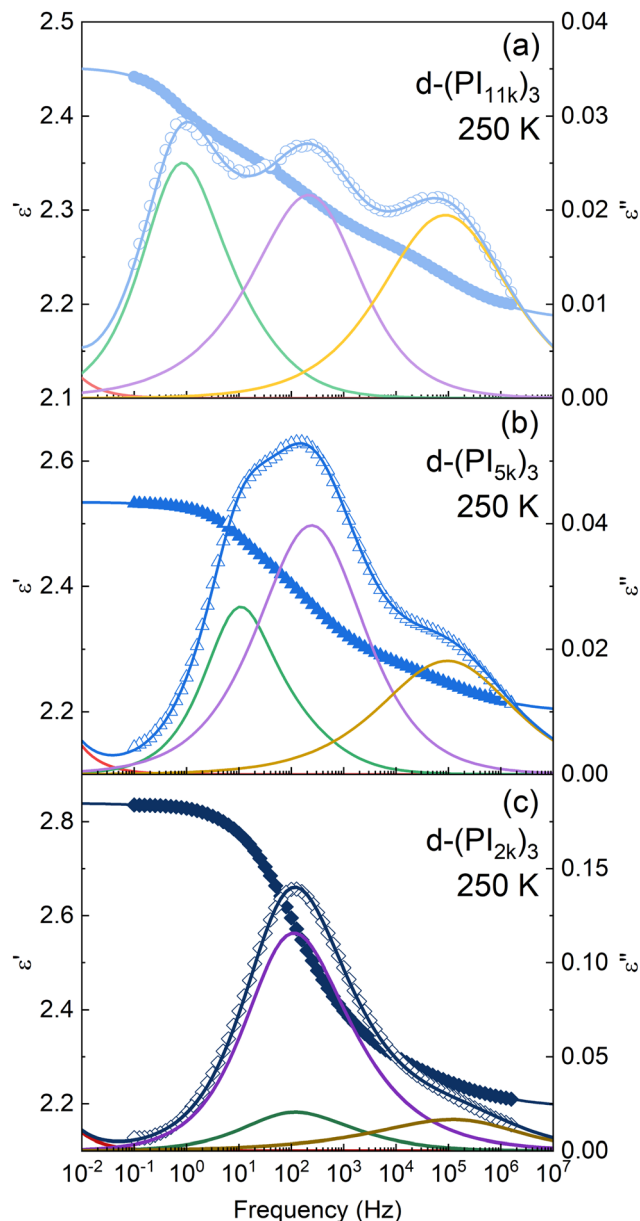


Fig. 6 Dielectric permittivity as a function of frequency for 3-arm stars with a molecular weight of (a)  $11 \text{ kg mol}^{-1}$ , (b)  $5 \text{ kg mol}^{-1}$ , and (c)  $2 \text{ kg mol}^{-1}$  per arm, at 250 K. Solid symbols account for the measured real component and open symbols for the imaginary one. Fittings to eqn (2) are represented by solid lines: blue lines for the whole dielectric response; the resolved relaxation components (only for the imaginary part of the dielectric permittivity) are also depicted: normal mode (green),  $\alpha$ -relaxation (yellow) and DCB-component (purple). Red lines account for the conductivity.

$n$  is the dipole number density and  $k_{\text{B}}$  is the Boltzmann constant. From this equation, we obtain  $\mu_{\text{DCB}}^{\text{eff}} \approx 2.0 \text{ D}$  for each dynamic covalent bond of the 3-arm stars. We can compare this dipole moment with that obtained for the two parts of the DCB, namely, the acetate moiety (1.72 D for methyl acetate<sup>71</sup>) and the amine one (0.92 D for dimethyl amine<sup>71</sup>). As can be seen, the value obtained is close to that expected for the DCB.



Table 2 Fitting parameters obtained at  $T = 250$  K using eqn (2) for the dielectric data description depicted in Fig. 6

Sample	$\alpha$ -relaxation				DCB-relaxation				Normal mode		
	$\Delta\epsilon_z$	$f_z^{\max}$ (Hz)	$a_z^a$	$b_z^a$	$\Delta\epsilon_{\text{DCB}}$	$f_{\text{DCB}}^{\max}$ (Hz)	$a_{\text{DCB}}$	$b_{\text{DCB}}$	$\Delta\epsilon_{\text{NM}}$	$f_{\text{NM}}$ (Hz)	$a_{\text{NM}}^a$
d-(PI <sub>2k</sub> ) <sub>3</sub>	0.094	111 950	0.53 <sup>b</sup>	0.57	0.47	112.95	0.67	0.66	0.085	100	0.62
d-(PI <sub>5k</sub> ) <sub>3</sub>	0.092	89 929	0.5 <sup>b</sup>	0.88	0.162	244.85	0.60 <sup>b</sup>	0.89	0.082	10	0.8
d-(PI <sub>11k</sub> ) <sub>3</sub>	0.094	81 774	0.5	1	0.091	215.10	0.64 <sup>b</sup>	0.68	0.085	0.75	0.74

<sup>a</sup> These parameters are constant with temperature, as well as the ratios  $\Delta\epsilon_z/\Delta\epsilon_{\text{NM}}$  and  $\Delta\epsilon_z/\Delta\epsilon_{\text{DCB}}$ . <sup>b</sup> The mirrored version of the HN function (eqn (6)) was used to describe this peak.

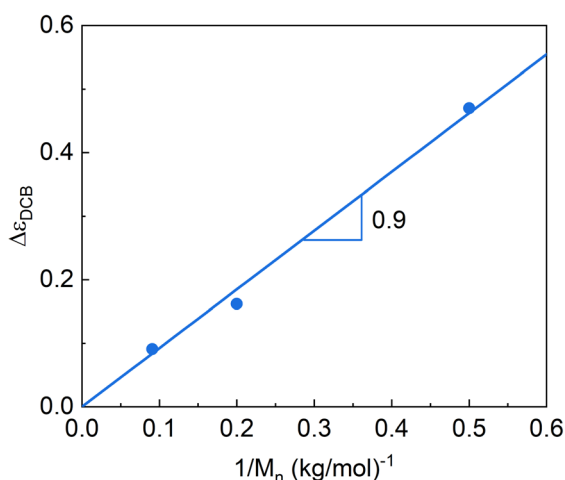


Fig. 7 Dielectric strengths of the DCB relaxation component as a function of the inverse of the arm  $M_n$ . The line corresponds to a simple proportionality law.

## 4 Discussion

To make a flawless comparison of the values of the frequencies corresponding to different samples, the small differences in the glass transition temperature are relevant and must be considered. Thus, using d-(PI<sub>11k</sub>)<sub>3</sub> as a reference, the frequency values of the other samples were corrected by a factor derived from the VFT equation, valid for small temperature changes in  $T_g$ :

$$f_{\text{corr}} \approx f_{\text{meas}} \exp[\Delta T_g D T_0 / (T - T_0)^2], \quad (7)$$

where  $\Delta T_g = T_g - T_g^{\text{d-(PI}_{11\text{k}})_3}$  (at 250 K this results in  $f_{\text{corr}} = f_{\text{meas}} \exp[0.216 \Delta T_g]$ ). In this way, the frequency values obtained in samples with higher  $T_g$  values (slower relaxation) are shifted to higher values, and *vice versa*. Fig. 8a shows the resulting values as a function of the molecular weight of the PI arm at 250 K. These results show that the frequency of  $\alpha$ -relaxation (yellow symbols) remains almost constant, as expected for the compensation for the  $T_g$  values.

Let's now start comparing how the characteristic frequencies of the other relaxation processes are modified as the molecular mass of the PI arms changes. Focusing the attention on the molecular weight dependence of the NM frequencies, we can observe in Fig. 8a (green symbols), that our high-molecular weight data follow a power law behavior with an exponent around 3.5, which has already been observed for conventional

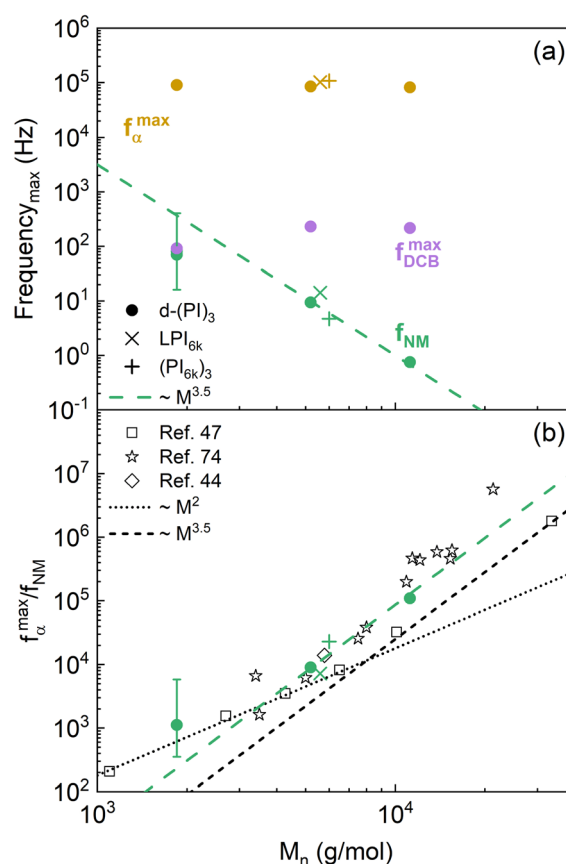


Fig. 8 (a) Characteristic frequencies of the relaxation components as a function of the arm  $M_n$  at 250 K. The dashed line corresponds to a power law with an exponent 3.5. (b) Comparison of the molecular weight dependence of the ratio of segmental relaxation and normal mode characteristic frequencies for different PI-based architectures: solid symbols for present work samples, open symbols for literature values (squares: linear chains;<sup>47</sup> diamond: 8-arm star;<sup>44</sup> stars: stars with various number of arms<sup>74</sup>).

PI star polymers,<sup>72,73</sup> and also for linear polymers above the critical molecular weight, which for PI is around  $7 \text{ kg mol}^{-1}$ .<sup>46,47</sup> Below that molecular weight, the NM relaxation time follows a power law with an exponent of 2, in agreement with the Rouse theory.<sup>50</sup> The present results have been compared with published ones from linear<sup>47</sup> and star<sup>44,74</sup> PI polymers using the  $\alpha$ -relaxation frequency as a reference, as depicted in Fig. 8b. For the high-molecular weight samples, no differences are observed in this comparison with respect to the behavior of conventional PI stars



within uncertainties. For the shortest arms investigated (d-(PI<sub>2k</sub>)<sub>3</sub> sample), we recall that the NM relaxation is masked (see Fig. 6c) by a much stronger DCB contribution to the dielectric relaxation, which gives rise to large uncertainties in the NM peak frequency determination. Within these uncertainties, the dynamics of these short arms—well below the entanglements threshold—is close to Rouse behavior, as reported for linear chains and other small stars.<sup>75</sup> In summary, from this comparison, we can conclude that the presence of DCB in the star polymers seems to have little effect on the arm retraction dynamics—the molecular mechanism associated with the normal mode relaxation of conventional stars.

Moving to the DCB-related dynamics, their characteristic frequencies are markedly slower than those of the PI  $\alpha$ -relaxation, but show a similar temperature dependence. This latter result suggests a direct link between the PI segmental dynamics and the DCB reorientation event. On the other hand, when comparing the DCB frequency values of different samples (see Fig. 8a, purple symbols), we found that they are essentially the same for the d-(PI<sub>5k</sub>)<sub>3</sub> and d-(PI<sub>11k</sub>)<sub>3</sub> samples, but for the d-(PI<sub>2k</sub>)<sub>3</sub> sample, the frequency is significantly lower. This difference is beyond uncertainty. It can be noticed already in the raw data, as observed in Fig. 6. Indeed, for d-(PI<sub>5k</sub>)<sub>3</sub> the DCB is the main peak of the three relaxation processes, with an intensity 5.5 times that of the NM relaxation. Therefore, the position of its maximum is well determined by the global spectrum. Given the difference in intensities between the NM and the DCB peaks (supported by the results shown in Fig. 7), the position of the former barely affects the maximum of the latter. Moreover, only in this sample, the NM frequency is close to that of the DCB. In principle, we do not see a clear connection between these two features. Motivated by these findings, we had a closer inspection into the calorimetric response of the three samples. In Fig. 9 the DSC curves obtained during cooling for all 3-arm stars are directly compared. Again in this observable, the different behavior of the sample with lowest molecular weight is manifested. The glass transition seems to be more extended; in particular, there are indications of vitrification starting at higher temperatures than in the other samples.

In all the systems we would expect that the PI segments close to the DCBs would have a slower dynamics than those further along the chain approaching the arm end, giving rise to a gradient of mobility along the arm. Since  $f_{\text{DCB}}^{\text{max}}$  and, in particular, the ratio  $f_{\text{DCB}}^{\text{max}}/f_{\alpha}^{\text{max}}$  are smaller for the d-(PI<sub>2k</sub>)<sub>3</sub> sample, these effects would be more pronounced for this sample. In this picture, we can assume that there is a local  $T_g$  associated with the slower PI segments with timescales close to those of the DCB relaxation. According to eqn (7), a reduction in frequency by about 3 decades, as observed in Fig. 8a, would correspond to a shift in  $T_g$  values of about 30 K. This corresponds well with the temperature range in which significant differences in the DSC trace are observed when comparing, for instance, d-(PI<sub>2k</sub>)<sub>3</sub> and d-(PI<sub>11k</sub>)<sub>3</sub> samples, as can be seen in Fig. 9. In the latter case, the number of PI segments involved in the mobility gradient would be relatively small and can be used as a good reference for the more homogeneous PI segmental dynamics. In addition, we note the minimal differences found between

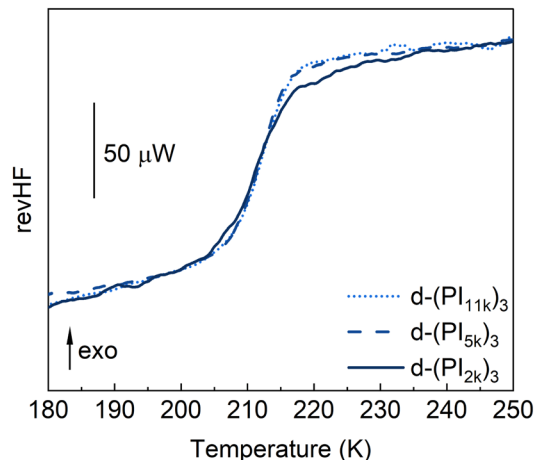


Fig. 9 Comparison of the reversing heat flow curves obtained by MDSC for the d-(PI)<sub>3</sub> stars during cooling at an average rate of 3 K min<sup>-1</sup>, a temperature oscillation amplitude of 0.5 K, and a period of 1 min.

d-(PI<sub>5k</sub>)<sub>3</sub> and d-(PI<sub>11k</sub>)<sub>3</sub> samples. Thus, the d-(PI<sub>2k</sub>)<sub>3</sub> sample presents significantly slower DCB dynamics and clearly more heterogeneous dynamics of the PI segments.

To look for a possible origin of this different behavior in the samples, we investigated their structural properties at the mesoscale. Clusterization of cross-linkers with DCBs has been reported for polyethylene vitrimers<sup>76</sup> and also for telechelic polymer vitrimers based on both PI and polybutadiene,<sup>40,42,77</sup> and could have an important impact on the dynamics of the system.

Small-angle X-ray diffraction (SAXS) results on the 3-arm stars (see Fig. 10) point toward significant clustering in the particular case of the d-(PI<sub>2k</sub>)<sub>3</sub> sample, with the presence of a broad but very clear low-angle diffraction peak. The peak position  $Q_{\text{max}} \approx 0.15 \text{ \AA}^{-1}$  corresponds to distances between clusters of about  $2\pi/Q_{\text{max}} = 4.2 \text{ nm}$ . This is in the range of the average end-to-end distance of linear PI with the mass of the arm.<sup>78</sup> A coincidence between the inter-cluster distance and the bulk chain dimension was also found in the PI telechelic vitrimers case.<sup>40,42</sup> In those materials it would be the consequence of the conservation of Gaussian conformation of the chains despite being connected to clusters at their ends, emphasizing the role of conformational entropy. However, this condition would not necessarily predetermine the inter-cluster distance in the present systems, with one end of each arm free. Experiments at different temperatures showed no significant dependence on the temperature of this distance. A simple model to describe the situation would consider the material as an ensemble of effective micelles, each of the micelle composed of  $N$  stars, where the core containing the  $N$  triamines is nano-segregated from the PI arms. This could be considered as an equivalent star with a larger core and more arms. In a crude approach to estimating  $N$ , we can assume a cubic lattice where each cube of side  $L$  ( $L$  would be the inter-cluster distance) has the volume of one of these micelles, *i.e.*,  $L^3 = N(\nu_{\text{cross}} + n\nu_{\text{arm}})$ . Here,  $\nu_{\text{cross}} \approx 0.24 \text{ nm}^3$  and  $\nu_{\text{arm}} \approx 3.4 \text{ nm}^3$  are the



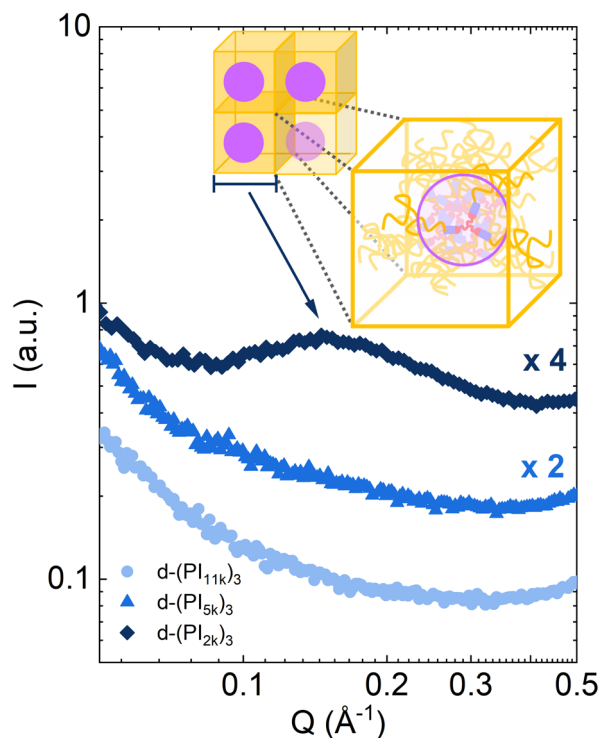


Fig. 10 X-ray intensity scattered by the DCB stars investigated at 300 K. For clarity, some data were vertically shifted multiplying by the factors indicated in the graph. The proposed model of effective micelles is sketched in the graph.

estimated volumes of a cross-linker molecule and a PI-arm, respectively, and  $n = 3$  is the number of arms in the  $d\text{-(PI}_{2k})_3$  sample. This yields about 7 stars/micelle, *i.e.*, we would have an effective melt of 21-arm stars with dynamically active cores. For the other two samples, signatures of nanostructuring are not evident. Thus, cross-linkers would not be aggregated—or, at least, would be associated in a much lesser extent—in  $d\text{-(PI}_{5k})_3$  and  $d\text{-(PI}_{11k})_3$ .

This structural peculiarity of  $d\text{-(PI}_{2k})_3$  could explain the differences observed regarding the DCB dynamics and the calorimetric traces. In this sample, the crosslinkers would be confined within nanodomains. This would cause more hindered (and thereby slower) mobility of the crosslinkers and consequently slower reorientations of the DCBs than in the other samples. Nanostructuring would thus enhance the gradient of mobility in  $d\text{-(PI}_{2k})_3$ . On the other hand, let us remind that the concentration of crosslinkers—and thereby also of slowed-down PI segments linked to them—is highest in this sample. Thus, the contribution of the motions of these entities to the specific heat is also the largest. As argued above, these contributions would be slower if the entities are in the nanodomain cores than if they are more randomly distributed in the sample. This would rationalize the observed significant extension of the calorimetric glass transition to higher temperatures, most likely due to confined dynamics of entities inside the inner regions of the clusters.

We now discuss the nature of the DCB relaxation. The fact that the values of the effective dipole moments obtained for the

intermediate relaxation components are close to those expected for the complete reorientation of the dipolar entities involved in the DCB would suggest that a complete reorientation of the polar group at the core of the stars can occur on timescales that can be several orders of magnitude faster than those corresponding to normal mode relaxation, particularly in the case of the bigger stars. Interestingly, the ratio between the DCB and  $\alpha$ -relaxation peak frequencies is around 400, a value similar to that reported for PI-based telechelic vitrimers<sup>42</sup> (see Fig. S15, ESI†). In such systems, imine DCBs were present instead of the vinylogous urethane bonds linking the moieties in the present samples but the same TAEA triamine was used as crosslinker. In light of these results, one could consider that dynamic bond exchange is already active at temperatures a few degrees above  $T_g$  and does not involve the whole arm fluctuations. The fact that the DCB peak frequencies observed in Fig. 5 are similar in all samples, and equal in the samples where no clusterization is resolved, suggests that the bond exchange reaction could take place within the core of each star, *i.e.*, it is an intra-molecular process. This would explain why the NM relaxation of the longest arms is essentially insensitive to the presence of DCB at the core. According to this interpretation, the dynamic bond exchange in the core of the stars would be limited only by the hindered mobility of the directly attached PI chain-portion, so dynamic bond exchange would take place as long as the motions of these PI chain-portions are possible. The timescale difference between the DCB and the segmental dynamics reorientation corresponds to that expected between the end-to-end fluctuations and the segmental dynamics for an entire linear PI chain of about 20 repeat units, suggesting that this could be the size of such a chain portion. On the other hand, apparently, in the close vicinity of other cores—within the nanodomains—the DCB exchange slows down probably due to confined dynamics of the crosslinkers.

Last, we compare the present results on the stars with those obtained on model PI vitrimers,<sup>42</sup> where all the chain ends are connected to trifunctional crosslinkers, forming networks. Noteworthy, despite the DCB chemistry not being the same, the timescale of the DCB relaxation in the vitrimers is comparable to that in the stars (see Fig. S15, ESI†), and also shows a temperature dependence similar to that of the segmental dynamics. In fact, the larger dipole associated with the vinylogous urethane bond in the stars enhances the dielectric signal of the DCB-related relaxation and allows establishing this coincidence beyond uncertainties. On the contrary, the slower relaxation detected in the vitrimers showed a distinct temperature dependence with respect to the other two processes, consistent with that found in other dynamic covalent network systems. This suggests that the validity of the time-temperature superposition for the normal mode in the stars is due to the fact that we are not dealing with networks but with polymers with star architecture. In addition, the slowest process observed in the vitrimers is extremely broad—much broader than the stars' normal mode—reflecting the complexity and variety of processes involved in the chain end-to-end relaxation within the clustered network.



## Conclusions

In this study, we successfully synthesized three well-defined dynamic 3-arm PI stars (PI-arm 2, 5, and 11 kg mol<sup>-1</sup>) for the first time *via* vinylogous urethane bonding. Tris(2-aminoethyl)-amine (TAEA) served as the core, with three linear PI-AcAc arms attached through a condensation reaction between the three primary amino groups of the core and the acetoacetate groups of the PI arms. The synthesis was confirmed using SEC, <sup>1</sup>H NMR, and FT-IR. The dynamic behavior of these stars was further evaluated through a transamination reaction with an excess of aniline at elevated temperatures, revealing their adaptability and dynamic nature.

Comparing the dielectric relaxation of dynamic 3-arm PI stars with that of conventional (static) ones, we observed that, in addition to the usual  $\alpha$ - and NM relaxation processes, a new intermediate and relatively strong relaxation mode emerges, whose intensity increases linearly with the concentration of dynamic bonds in the core of the stars. The peak frequency of this component is about 400 times lower than that characterizing the PI segmental dynamics. In the particular case of the stars with shorter arms, the frequency of this relaxation process—associated with the DCB dipole fluctuation—is 2.5 times slower than in the other stars with longer arms. This difference could be related to the presence of a segregated clustering of the cores for the shortest arm stars, as inferred from the SAXS experiments. Probably for the same reason, the glass transition range as observed by MDSC extends to higher temperatures in this sample, indicating a greater dynamic heterogeneity of structural arrest in this case. Finally, the larger scale chain dynamics detected by the NM relaxation in the dynamically bonded 3-arm stars is similar to that of conventional stars. This means that the arm retraction dynamics is not affected by the dynamic character of the bonds, and consequently the bond exchanges that take place below room temperature would be restricted to those that occur in the core, *i.e.* the would be intramolecular (or intracluster) events.

## Author contributions

Conceptualization: N. H., J. C., A. A., A. A.; investigation: B. R., A. A., A. A., N. P., K. N., S. B.; analysis: B. R., A. Alegría, N. P., K. N., S. B.; methodology: A. A., A. A., J. C., N. H.; supervision: A. A., A. A., J. C., N. H.; writing – original draft: B. R., A. Alegría, N. P., K. N., S. B.; writing – review and editing: N. H., J. C., A. Arbe funding acquisition: N. H., J. C., A. A., A. A.

## Data availability

The data that support the findings of this study will be available upon request to the corresponding authors.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

B. R., A. A., A. A., and J. C. gratefully acknowledge the Grant PID2021-123438NB-I00 funded by MCIN/AEI/10.13039/501100011033 and by ERDF A way of making Europe, the Grant IT-1566-22 from Eusko Jaurlaritz (Basque Government) and the Open Access funding from the University of the Basque Country. N. P., K. N., S. B., and N. H. gratefully acknowledge support from the King Abdullah University of Science and Technology (KAUST) (BAS/1/1342-01-01).

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