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Mass and mole fractions in calibration-free LIBS

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This technical note highlights the fact that CF-LIBS algorithms work in mole fractions, while results of spectrochemical analysis are usually reported in mass fractions or mass percent. Ignoring this difference and not converting mole fractions to mass fractions can lead to errors in reported concentrations determined by the CF-LIBS method and inadequate comparison of these concentrations with certified concentrations. Here, the key points of the CF-LIBS algorithm are reproduced and the formulae for converting a mole fraction to a mass fraction and *vice versa* are given. Several numerical examples are also given, which show that the greater the difference between the molar mass of an individual element in a sample and the average molar mass, the greater the discrepancy between the mole and mass fractions.

1 Introduction

Calibration-free LIBS (CF-LIBS) has received considerable attention as an alternative approach to analysis using reference samples because it does not require a laborious calibration procedure. The element concentrations are found directly from the measured spectrum using a simplified laser-induced plasma model. This approach was first proposed by Ciucci *et al.*[1] using the assumptions of stoichiometric ablation and homogeneous optically thin plasma in local thermodynamic equilibrium (LTE). Special efforts have been made to investigate the accuracy of the method by analyzing errors associated with plasma inhomogeneity, line overlap, noise, spectral resolution, self-absorption, or inaccurate path length.[2,3] It was shown that the CF-LIBS method is not error-free even for synthetic spectra that fully correspond to the mathematical model.[3]

The purpose of this technical note is to eliminate another potential error in the presentation of CF-LIBS results that can occur if the fact that CF-LIBS algorithms work with mole fractions rather than mass fractions is neglected. Since mass percentages (mass fractions) are more commonly used when reporting spectrochemical analysis data, CF-LIBS results assume conversion of mole fractions to mass fractions. The importance of such a conversion was emphasized in ref. 4, however, most publications on CF-LIBS avoid mentioning it, leaving the impression that work with mass percent is taken for granted. Meanwhile, the lack of conversion of mole fraction to mass fractions can lead to overestimations or underestimations of concentrations. Here we discuss this issue by highlighting the difference between the mole and mass fractions and estimating errors due to misassignment of concentrations.

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2 Relative concentrations in the Boltzmann plot method

The most used expression for the Boltzmann plot in the CF-LIBS application is

$$\ln\left(\frac{I_{ki}^{\lambda}\lambda_{ki}}{g_k A_{ki}}\right) = \ln\left(\frac{\Phi c_s^z}{U_s^z(T)}\right) - \frac{E_k}{k_B T} \quad (1)$$

where I_{ki}^{λ} is the spectral radiance integrated over the line profile and full solid angle, λ_{ki} is the transition wavelength, g_k and E_k are the degeneracy and energy of the upper transition state, A_{ki} is the Einstein coefficient for spontaneous emission, $U_s^z(T)$ is the partition function, k_B is the Boltzmann constant, and T is the temperature. All physical quantities in eqn (1) are normalized to the chosen system of units.[5] The factor $\Phi = F \cdot hcn_{\Sigma}$ is the product of the experimental coefficient F, which takes into account the collection angle and path length, and the combination of physical (the speed of light and Planck contant) and plasma (total number density) constants. The concentration $c_s^z = n_s^z/n_{\Sigma}$ of the particle s in the charge state z denotes the fraction of its number density relative to the total number density $n_{\Sigma} = \Sigma_{s,z}n_s^z$, that is, the mole fraction. After plotting dependence (1) in coordinates $x = E_k$ and $y = \ln(I_{ki}^{\lambda}\lambda_{ki}/(g_k A_{ki}))$, the mole fraction c_s^z is found from its point of intersection $b_s^z \equiv \ln(\Phi c_s^z/U_s^z(T))$ with the y-axis at $E_k = 0$

$$c_s^z = \frac{U_s^z(T)}{\Phi}\exp\left(b_s^z\right) \quad (2)$$

The unknown factor Φ is found from the requirement that all mole fractions add up to one, $\Sigma_{s,z}c_s^z = 1$.

It should be emphasized again that the above equations work with number densities, so that relative concentrations of elements are expressed in mole fractions. Since the concentrations in standard reference samples are usually given in mass fractions, the results of the CF-LIBS analysis cannot be directly

compared with these reference values. For a correct comparison, either the CF-LIBS results should be converted from mole fractions c_s to mass fractions w_s via

$$w_s = \frac{c_s M_s}{\Sigma_s c_s M_s} \qquad (3)$$

or, *vice versa*, the reference values should be converted from mass fractions w_s to mole fractions c_s via

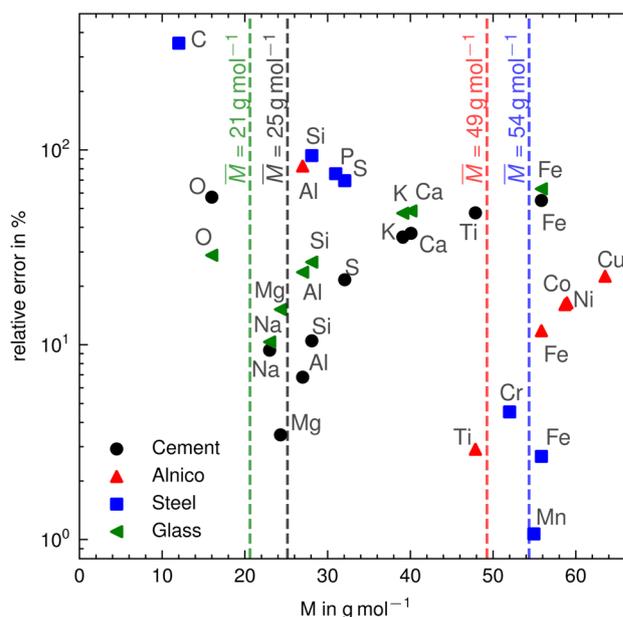$$c_s = \frac{w_s/M_s}{\Sigma_s w_s/M_s} \qquad (4)$$

here, M_s is the molar mass in kg mol^{-1}.

3 Mass fraction *versus* mole fraction examples

Table 1 shows the relative concentrations of elements in Portland cement, stainless steel, alnico, and soda-lime glass. The mass percentage are sourced from the literature,[6–9] and the

Fig. 1 Comparison between molar mass and relative error of mass and mole fraction for different materials.

Table 1 Comparison between mass and mole percentage for different materials

Element	M g mol^{-1}	w wt%	c mol%	RE %
Portland cement ($\bar{M}$ = 25 g mol^{-1})				
Al	26.98	2.51	2.34	7
Ca	40.08	47.37	29.72	37
Fe	55.84	1.77	0.80	55
K	39.10	0.74	0.47	36
Mg	24.31	1.38	1.43	3
Na	22.99	0.15	0.17	9
O	16.00	35.46	55.72	57
S	32.06	1.07	0.84	22
Si	28.09	9.45	8.46	10
Ti	47.87	0.11	0.06	47
Alnico ($\bar{M}$ = 52 g mol^{-1})				
Al	26.98	13.96	25.49	83
Co	58.93	36.09	30.17	16
Cu	63.55	2.50	1.94	22
Fe	55.84	28.50	25.14	12
Ni	58.69	11.75	9.86	16
Ti	47.87	7.20	7.41	3
Stainless steel ($\bar{M}$ = 54 g mol^{-1})				
C	12.01	0.20	0.90	353
Cr	52.00	13.00	13.59	5
Fe	55.84	84.25	81.99	3
Mn	54.94	1.50	1.48	1
P	30.97	0.04	0.07	75
S	32.06	0.01	0.03	70
Si	28.09	1.00	1.94	94
Soda-lime glass ($\bar{M}$ = 21 g mol^{-1})				
Al	26.98	0.74	0.57	24
Ca	40.08	5.62	2.89	49
Fe	55.84	0.04	0.02	63
K	39.10	0.12	0.06	47
Mg	24.31	1.44	1.22	15
Na	22.99	11.77	10.56	10
O	16.00	46.48	59.89	29
Si	28.09	33.79	24.80	27

mole percentage are calculated according to eqn (4). For Portland cement, the relative error (RE = $|c - w|/w \cdot 100\%$) between the mass fractions and the mole fractions falls in the range of about 3–57%, with an average relative error about 35%. The largest error is observed for iron and titanium due to the largest deviations of their molar masses (respectively 56 and 48 g mol^{-1}) from the average molar mass $\bar{M} = (\Sigma_i w_i/M_i)^{-1} \approx 25$ g mol^{-1}. In contrast, sodium, magnesium, and aluminum with molar masses close to the average molar mass (respectively 23, 24, and 27 g mol^{-1}) show the smallest error. For the Alnico sample, which is composed of aluminum, cobalt, copper, iron, nickel and titanium, the latter five have close molar masses, while aluminum has a molar mass of almost less than half that. Therefore, the relative error of aluminum is the highest, about 83%, and the relative errors of the remaining elements are within 3–22%. A similar analysis can be carried out for the other two samples shown in Table 1: stainless steel and soda-lime glass. Wherever the molar mass of an element differs significantly from the average molar mass, a deviation between mole and mass concentration becomes apparent. This is also illustrated in Fig. 1.

4 Conclusion

An important feature of the CF-LIBS algorithms is that element concentrations are expressed in mole fractions rather than mass fractions, as opposed to the typical representation of concentrations in mass percentages or mass fractions. For an adequate presentation of CF analysis results, the conversion of mole fractions to mass fractions should not be overlooked, otherwise errors in reported concentrations and incorrect comparisons with certified concentrations will occur. If elements with close molar masses are analyzed, such as

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transition metals in steel, the difference between mole fraction and mass fraction is small. However, it becomes larger the greater the difference between the molar masses of the individual elements in the sample.

Author contributions

Tobias Völker: conceptualization, methodology, formal analysis, visualization, writing – original draft, writing – review & editing, Igor B. Gornushkin: validation, writing – review & editing.

Conflicts of interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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