

Why copper catalyzes electrochemical reduction of nitrate to ammonia†

Mohammadreza Karamad,^{*a} Tiago J. Goncalves,^{id c} Santiago Jimenez-Villegas,^{id c} Ian D. Gates^{*b} and Samira Siahrostami^{id *c}

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Electrochemical reduction of nitrate (NO₃RR) has drawn significant attention in the scientific community as an attractive route for ammonia synthesis as well as alleviating environmental concerns for nitrate pollution. To improve the efficiency of this process, the development of catalyst materials that exhibit high activity and selectivity is of paramount importance. Copper and copper-based catalysts have been widely investigated as potential catalyst materials for this reaction both computationally and experimentally. However, less attention has been paid to understanding the reasons behind such high activity and selectivity. Herein, we use Density Functional Theory (DFT) to identify reactivity descriptors guiding the identification of active catalysts for the NO₃RR, establish trends in activity, and explain why copper is the most active and selective transition metal for the NO₃RR to ammonia among ten different transition metals, namely Au, Ag, Cu, Pt, Pd, Ni, Ir, Rh, Ru, and Co. Furthermore, we assess NO₃RR selectivity by taking into account the competition between the NO₃RR and the hydrogen evolution reaction. Finally, we propose various approaches for developing highly active catalyst materials for the NO₃RR.

Introduction

Ammonia is an important chemical in human life with a wide range of agricultural and pharmaceutical applications.^{1,2} It is mainly used as a fertilizer for large scale commercial food production. The mass production of ammonia has mainly relied on the Haber–Bosch process; that is, the reaction between atmospheric nitrogen and H₂ at high temperature and pressure.^{3,4} Currently, heterogeneous iron-based catalysts are used in the Haber–Bosch process.^{5,6} This process is energy

^aDepartment of Physics & Astronomy, University of Calgary, 2500 University Drive NW, Calgary, Alberta T2N 1N4, Canada. E-mail: Mohammadreza.karamad@ucalgary.ca

^bDepartment of Chemical and Petroleum Engineering, University of Calgary, 2500 University Drive NW, Calgary, Alberta T2N 1N4, Canada. E-mail: idgates@ucalgary.ca

^cDepartment of Chemistry, University of Calgary, 2500 University Drive NW, Calgary, Alberta T2N 1N4, Canada. E-mail: samira.siahrostami@ucalgary.ca

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intensive with undesirable environmental impact: it currently accounts for 2–5% of the world's energy demand and causes about 1% of total global energy-related CO₂ emission.⁷ This urges the development of sustainable alternatives for ammonia synthesis that can alleviate these concerns.^{4,7–10}

Electrochemical reduction of nitrate (NO₃RR) and nitric oxide (NORR) have emerged as attractive routes for ammonia synthesis.^{11–13} Due to its abundance in water resources and soil, nitrate (NO₃) represents a promising source of nitrogen for ammonia synthesis.¹⁴ When coupled with renewable energy sources, the NO₃RR can be used to produce a variety of products such as NH₃, NO, N₂O, and N₂ at ambient conditions. The nitric oxides (NO and N₂O) produced during the NO₃RR can also be further reduced to ammonia. In addition, both the NO₃RR and NORR, when coupled, can address one of the grand challenges of the 21st century, that is the high nitrate level in groundwater and soil with its deteriorating effect on the environment and human health. Despite its promise, one of the key challenges for developing large-scale implementation of NO₃RR technology are efficient electrocatalysts that exhibit high activity and selectivity towards the desired product, *i.e.*, ammonia.

In the search for efficient NO₃RR electrocatalysts, transition metals such as Cu, Ag, Au, Ru, Rh, Ir, Pd, and Pt, as well as bimetallic alloys, have been frequently considered as potential candidates.^{2,15–31} Among transition metals, copper and copper-based catalysts have shown great promise for the selective and active NO₃RR to ammonia. This has sparked immense interest in modulating the Cu active site through various strategies, such as metal doping, exposed facet manipulation, and nanostructuring of the catalyst.^{32–34} For example, Qin *et al.* investigated the reactivity of different exposed facets of Cu₂O electrocatalysts.³⁵ They found higher ammonia yields for the (100) facet when compared to the (111). Wang *et al.* reported nanowire arrays (NWAs) of CuO as an electrocatalyst for the reduction of nitrate.³³ Interestingly, they unveiled a reconstruction of the NWAs during catalysis. This reconstruction was found to suppress the competing HER, producing a highly selective Cu/Cu₂O NWA catalyst with a faradaic efficiency of 95.8% towards ammonia. More recently, Chen *et al.* demonstrated an extraordinarily active and selective catalyst for nitrate to ammonia.³⁶ They reported reduction currents of 1 A cm⁻² at low overpotentials (−0.13 V vs. RHE) with over 99% of nitrate being converted into ammonia using a Ru dispersed on Cu nanowire (Ru-CuNW) catalyst.

Fig. 1a summarizes the reported FEs for the NO₃RR to ammonia on a number of Cu-based catalysts reported in the literature. As can be seen, almost all reported FEs are above 80% for Cu-based catalysts. The high FE can be attributed to lower activity towards the competing hydrogen evolution reaction (HER) at negative potentials.^{18,37,38} Fig. 1b displays the measured current density, applied potential and FE at the same time. Other than high FE, the most successful copper-based catalysts would have a high current density at low applied potentials. This analysis shows that Ru-CuNW is the most active catalyst reported.

To unravel the reasons behind such high activity and selectivity for the NO₃RR to ammonia on Cu-based catalysts, we need to establish an understanding about the mechanism of the NO₃RR to ammonia on transition metals. Several efforts have already been made in the literature to understand the NO₃RR mechanism.^{18,33,48–53} Depending on the catalyst material, different reaction mechanisms have been proposed for the NO₃RR to ammonia.^{14,19,54,55} Liu



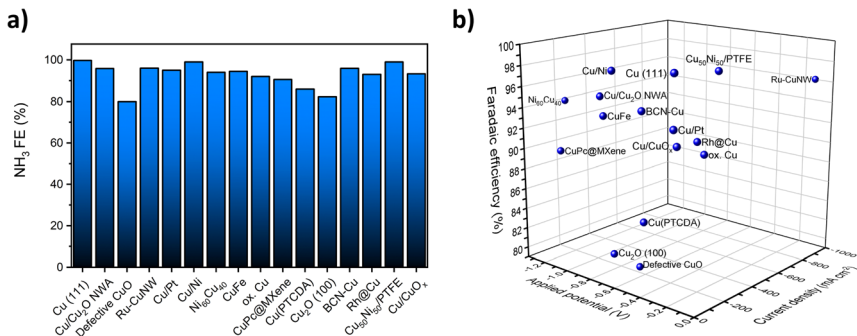


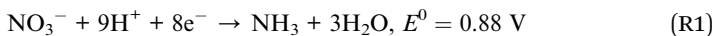
Fig. 1 (a) Previously reported FEs for the NO₃RR over selected Cu and Cu-based electrocatalysts. (b) Reported FEs and measured current densities at applied potentials for selected Cu and Cu-based electrocatalysts. Data extracted from ref. 20, 21, 32–36 and 39–47.

et al. studied the trends in NO₃RR catalytic activity and selectivity by using DFT-based microkinetic modelling on transition metals through a direct electrocatalytic nitrate reduction mechanism at moderate nitrate concentrations and showed that the NO₃RR proceeds through deoxygenation and hydrogenation steps at the catalyst surface.¹⁹ They proposed binding energies of oxygen and nitrogen atoms as descriptors for the catalytic activity and selectivity of nitrate reduction on transition metals and transition metal alloys. A similar mechanism has been used to study the NO₃RR on Cu–Ni alloys and Ru surfaces.²⁰ It has been widely accepted that nitrite (NO₂) and NO are the key intermediates in the NO₃RR.² Therefore, a large body of research in the literature has focused on the NORR and NO₂RR.^{2,15,49,56–59} In particular, the catalytic activity and selectivity of Pt for both the NORR and NO₂RR to ammonia through sequential electrochemical steps where possible intermediates form only in proton and electron transfer reactions have been probed.^{49,60–62} The NO₃RR, through sequential electrochemical steps, has also been suggested as the reaction mechanism and used to study the catalytic activity of transition metals and transition metal oxides.⁶³ In this study, using Density Functional Theory (DFT) we investigate the trends in the catalytic activity of the NO₃RR to ammonia through sequential electrochemical steps on different transition metal surfaces. We elucidate reaction paths for the NO₃RR on different transition metals by performing a mechanistic study and developing activity descriptors for the NO₃RR to ammonia using scaling relations between binding energies of NO₃RR intermediates. This descriptor-based analysis leads to an understanding of the high activity and selectivity for copper among other transition metals and provides a guide to developing novel catalyst materials with enhanced activity for the NO₃RR to ammonia.

Results and discussion

The overall electrochemical conversion of NO₃[−] to NH₃ involves the transfer of nine protons and eight electrons at a potential of 0.88 V *versus* the reversible hydrogen electrode (RHE):⁴⁸





En route to the formation of NH_3 , the reduction of NO_3^- can follow multiple reaction pathways as outlined in Fig. 2, producing byproducts such as NO , N_2O and N_2 .⁶³ In one of the pathways that has been reported frequently in the literature, the NO_3RR occurs in a sequence of deoxygenation and hydrogenation steps (pathway 1 in Fig. 3).^{20,50,64} In this pathway, the NO_3RR proceeds through the $^*\text{NO}_3 \rightarrow ^*\text{NO}_2 \rightarrow ^*\text{NO} \rightarrow ^*\text{N}$ deoxygenation steps followed by the $^*\text{NH} \rightarrow ^*\text{NH}_2 \rightarrow ^*\text{NH}_3 \rightarrow \text{NH}_3(\text{g})$ hydrogenation steps. In the second pathway (pathway 2 in Fig. 3), the NO_3RR proceeds through $\text{NO}_3^- \rightarrow ^*\text{NO}_3 \rightarrow ^*\text{NO}_2 \rightarrow ^*\text{NO} \rightarrow ^*\text{NOH} \rightarrow ^*\text{NHOH} \rightarrow ^*\text{NH}_2\text{OH} \rightarrow ^*\text{NH}_2 \rightarrow ^*\text{NH}_3 \rightarrow \text{NH}_3(\text{g})$. These two pathways share similar deoxygenation steps until the formation of NO^* . In pathway 1, NO^* reduction proceeds through formation of N^* through dehydrogenation of NO^* , followed by formation of $\text{NH}_3(\text{g})$ from N^* *via* four subsequent hydrogenation steps. On the other hand, N^* does not appear as an intermediate in pathway 2 and further reduction of NO^* occurs through hydrogenation of NO^* to form NOH^* followed by five subsequent hydrogenation steps to the formation of $\text{NH}_3(\text{g})$. Recently, by performing a systematic thermodynamic and kinetic analysis on the $\text{Cu}(111)$ and $\text{Cu}(100)$ surfaces, Hu *et al.* reported a high activation barrier for N^* formation through the NO^* dehydrogenation step, making pathway 2 more favorable in the NO_3RR .⁵⁰ They proposed a new pathway for the NO_3RR that is a combination of pathways 1 and 2 (pathway 3 in Fig. 3). Their study, however, is limited to the Cu surface which is known as the most promising catalyst among transition metals for the NO_3RR due to its high catalytic activity. It is desirable to understand the trends in NO_3RR catalytic activity among other transition metals.⁵⁴ Similar approaches have been used in the past for other electrochemical reactions where different descriptors have been developed to understand the trends in catalytic activities for these reactions by developing activity descriptors.^{65–68} These descriptors have been used to identify promising catalysts. In the present study, we aim to develop such descriptors to understand the trends for NO_3RR catalytic activity among different transition metals.

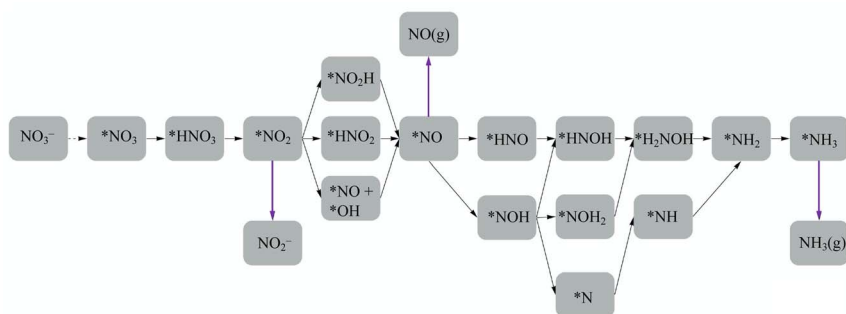


Fig. 2 Reaction paths and possible intermediates for the electrochemical reduction of NO_3^- to NH_3 are considered in this work. Magenta arrows indicate the formation of nitric oxide (NO), nitrite (NO_2^-), and ammonia ($\text{NH}_3(\text{g})$). The dashed arrow indicates a reaction with a proton transfer, and the solid arrows indicate reactions with a proton/electron pair transfer.



Fig. 5 displays the free energy diagram for the lowest free energy path on the Cu(111) surface. Moreover, the free energy diagram containing the NO₃RR intermediates reported by Hu *et al.* based on both thermodynamic and kinetic analysis is provided (in blue) for comparison. Fig. 5 shows that the NO₃RR on Cu(111) follows a similar pathway to the one reported by Hu *et al.*, that is NO₃[−] → *NO₃ → *NO₂ → *NO → *NOH → *NHOH → *NH₂OH → *NH₂ → *NH₃ → NH₃(g). We, however, found that two intermediates involved in the NO₃RR pathway to ammonia are different from the ones reported by Hu *et al.*, as shown in the inset of Fig. 5. In particular, we found that the reduction of *NO₂ results in the formation of *NO + *OH due to dissociation of *NO₂H. In addition, while Hu *et al.* reported that the reduction of *NOH results in the formation of *NHOH, we found that the reduction of *NOH results in the formation of *N. Although Hu *et al.* have not reported the energetics as well as the kinetic barriers for the formation of *NO + *OH from *NO₂H, the small differences that exist between the pathways presented in this work and reported by Hu *et al.* are presumably because of the slightly different settings used in our DFT calculations. We would like to emphasize that despite these slight differences, in both pathways the potential limiting step is the reduction of NO* to NOH*. The free energy diagrams for the most favorable pathways for the other transition metals considered in this study are provided in the ESI (see Fig. S2†).

With the potential limiting step identified for all metals, the theoretical limiting potential for the electrochemical reaction to occur (*i.e.*, the lowest potential, at which all the reaction steps are downhill in free energy) is obtained. The calculated limiting potentials range from −0.19 V to −0.72 V *versus* RHE, in order of Ir > Cu > Pt > Co > Ni > Rh > Ru > Pd, where Ag and Au are excluded since they are not expected to fully reduce nitrate to NH₃ (Table 1). It is interesting to compare NO₃RR catalytic activity over transition metals with previous experimental reports. Dima *et al.* describe a comparative study to determine the catalytic activity and selectivity of eight different polycrystalline electrodes, namely Pt, Pd, Rh, Ru, Ir, Cu, Ag, and Au for the NO₃RR in acidic solution.¹⁷ They showed that the NO₃RR catalytic activity decreases in the order Rh > Ru > Ir > Pd and Pt for the transition metals and in the order Cu > Ag > Au for the coinage metals. We note that the trends in catalytic activity shown in Table 1 are different from the ones reported by Dima *et al.* This is due to the fact that the catalytic activities reported by Dima *et al.* correspond to all NO₃RR products including ammonia and

Table 1 Calculated potential limiting steps with the corresponding limiting potentials for all transition metals considered in this study, except Au and Ag

Metal	Potential limiting step	Limiting potential (V vs. RHE)
Cu	*NO → *NOH	−0.23
Pt	*NO → *NOH	−0.33
Ni	*NO → *NOH	−0.37
Rh	*NO → *NOH	−0.39
Pd	*NO → *NOH	−0.72
Ir	*NO ₃ → *HNO ₃	−0.19
Co	*NO ₃ → *HNO ₃	−0.34
Ru	*NO ₃ → *HNO ₃	−0.46



hydroxylamine. In addition, our DFT calculations were performed on single facets, whereas Dima *et al.* used polycrystalline electrodes in their experiments.

NO₃RR activity volcanos

To investigate the NO₃RR catalytic activity over transition metals, we employ the well-established volcano framework following the Sabatier principle. We first consider the linear scaling relations between different intermediates involved in the NO₃RR to ammonia (Fig. 6). The NO₃RR mechanism includes two sets of adsorbates. The first set are adsorbates that interact with the catalyst surface through the nitrogen atom and the second set interact *via* an oxygen atom. We use *NO and *OH as descriptors for the first and second sets of adsorbates due to the fact that the calculated adsorption energies of *N and *O intermediates over transition metals scale linearly with those of NO* and *OH, respectively.^{49,54,73} Fig. 6a and b show the linear scaling relations for the first and second set of adsorbates, respectively. Fig. 6a shows that the binding energies of nitrogen bound species correlate to the binding energies of *NO (ΔG_{*NO}). Similarly, the binding energies of oxygen bound species correlate to the binding energies of *OH (ΔG_{*OH}). These correlations can be rationalized through the d-band model and the position of the d-band center.⁷⁴ We would also like to emphasize that Au and Ag have been excluded when constructing the scaling relations. This is because Au and Ag do not bind several key intermediates such as *NO₃, *NO₂ and *NO. Therefore, the full NO₃RR to ammonia does not occur on these metals.¹⁷

Using the scaling relation between the adsorbates that bind through nitrogen and oxygen, we construct a volcano-type relationship between the limiting potential and binding energies of NO*(ΔG_{NO^*}) and the binding energies of *OH (ΔG_{*OH}), as shown in Fig. 7a and b. Each line in these volcano plots corresponds to an elementary reaction in the reaction network. Moreover, in constructing the volcano plots different reaction pathways were considered to take into account that the NO₃RR may proceed through different reaction pathways on transition metals.

These volcano plots provide insights into the electrocatalytic activity of the transition metals. The potential limiting step (PLS) for the NO₃RR corresponds to the elementary reaction with the most negative limiting potential, U_L . The difference between the most negative limiting potential U_L and the equilibrium

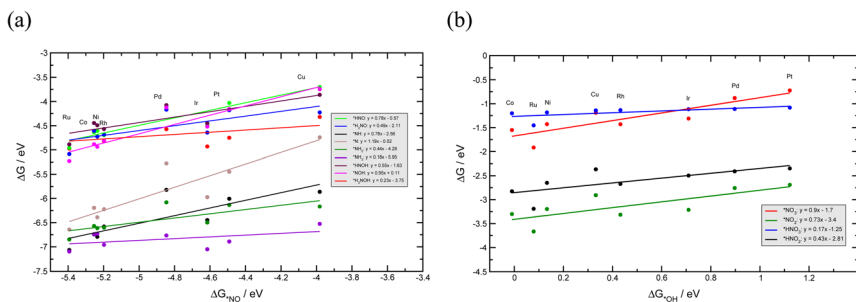


Fig. 6 Linear scaling relations between NO₃RR reaction intermediates that bind *via* (a) a nitrogen atom, and (b) *via* an oxygen atom.



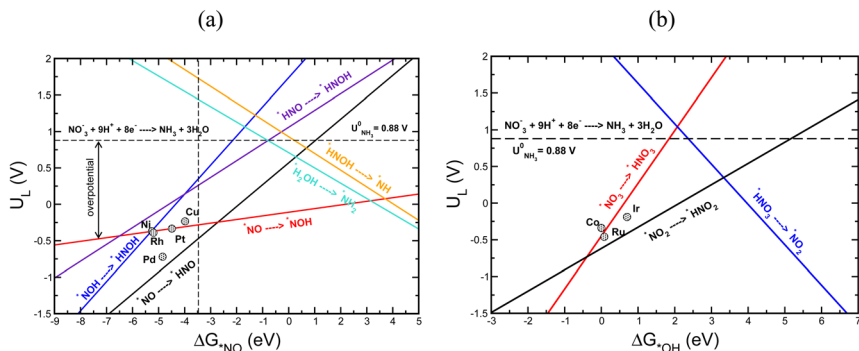


Fig. 7 Volcano plot showing limiting potentials for (a) Ni, Rh, Pt, Pd and Cu based on binding energies of NO and (b) Co, Ru and Ir based on binding energies of OH. The horizontal dashed lines in (a) and (b) depict the equilibrium potential for the NO₃RR to ammonia. The vertical dashed line in (a) depicts the Gibbs free energy of NO(g).

potential (shown by horizontal dashed lines in Fig. 7a and b) defines the overpotential required to drive the NO₃RR. This analysis shows that NO* → NOH* or NO* → HNO* are the PLS steps. For Cu, Pt, Ni, Rh, and Pd, the PLS is NO* → NOH*. Fig. 7a shows that the trends in catalytic activity obtained from the free energy diagrams agree well with the activity volcano analysis. The only outlier is Pd. This is because both the *NO → *NOH and *NO → *HNO lines in Fig. 7a are derived from linear scaling relations. More outliers are observed along the linear correlation for NOH* when constructed against HNO*. These outliers affect the accuracy of the linear fit. Nonetheless, both of those linear correlations are close to each other and are the lowest line with maximum distance from the equilibrium potential. Therefore, the formation of either NOH* or HNO* could well be the PLS, and both warrant consideration. The volcano plot in Fig. 7a shows that Cu is close to the cusp of the NO* → NOH* and NO* → HNO* lines, suggesting a superior catalytic activity over the rest of the studied transition metal surfaces. This explains why Cu has been repeatedly reported experimentally as an efficient catalyst for the NO₃RR to ammonia. Note that Cu still has 1.11 V overpotential for the NO₃RR to ammonia. Higher activities over Cu can be achieved by finding a catalyst material that has a weaker *NO binding energy. However, weaker *NO binding energies may result in the desorption of *NO in which case the full NO₃RR to ammonia does not occur or NO(g) forms as the final NO₃RR product. Ultimately, there is a ~0.5 eV window for decreasing *NO binding energy and therefore increasing NO₃RR catalytic activity. Another important feature in Fig. 7a is that the slope for the NO* → NOH* line is 0.05, indicating that the NO₃RR catalytic activity is barely affected by changing the *NO binding energy. This mild slope originates from the fact that the *NOH and *NO binding energies scale linearly with a slope of 0.95 meaning that they are strongly coupled. This makes it almost impossible to change the binding energy of *NO without affecting the binding of *NOH. Interestingly, a similar feature has been observed as one of the limiting factors for catalyst development in the CO₂ reduction reaction by Peterson *et al.* where the *CO → *CHO step was identified as the PLS with a slope of ~0.15. They suggested several strategies for decoupling the binding energies of



*CO and *CHO that could lead to catalysts with superior catalytic activity over Cu.^{66,75} The above results allude to two possible directions that should be considered in the design of improved NO₃RR electrocatalyst systems with superior NO₃RR catalytic activity over Cu:

(1) The catalyst material must break the scaling relations between *NO and *NOH/*HNO intermediates. This can be achieved by stabilization of NOH*/HNO* adsorbates relative to NO*. To this end, similar strategies that have been proposed for catalyst development for the CO₂ reduction reaction can be applied for decoupling the binding energies of *NO and *NOH/*HNO, therefore leading to better performing catalyst materials (Fig. 7). We note that the above-mentioned limitations and the following suggested strategies to improve NO₃RR catalytic activity are only applied to catalysts for which the NO₃RR proceeds through the pathways where NO* → NOH*/*HNO is the PLS.

(2) Switching to new classes of materials that exhibit different scaling relations between *NO and *NOH/*HNO.

In the following we discuss possible strategies for breaking the scaling relations between *NO and *NOH/*HNO intermediates as depicted in Fig. 8.⁷⁶

(i) Alloying: by alloying with an element that has higher affinity towards oxygen, the *NOH and *HNO adsorbates with tilted adsorption structures may bind to the surface through both the nitrogen and oxygen atoms, causing the *NOH or *HNO adsorbates to bind more strongly to the surface than *NO. This strategy, however, should be taken with care. Although the element that has higher affinity towards oxygen does not influence the vertical adsorption structure of *NO, it may change the binding energy of *NO due to the change in adsorption site or modification of the electronic structure of the parent metal which could lead to stabilization of *NO, thus resulting in similar scaling relations to those of the parent metal. In addition, the presence of an element with higher affinity toward oxygen on the surfaces of the alloys facilitates water decomposition, which may give rise to *OH poisoning. If OH* binds too strongly to the surface, its reduction to water may become the potential limiting step rather than *NO reduction to *NOH/*HNO.

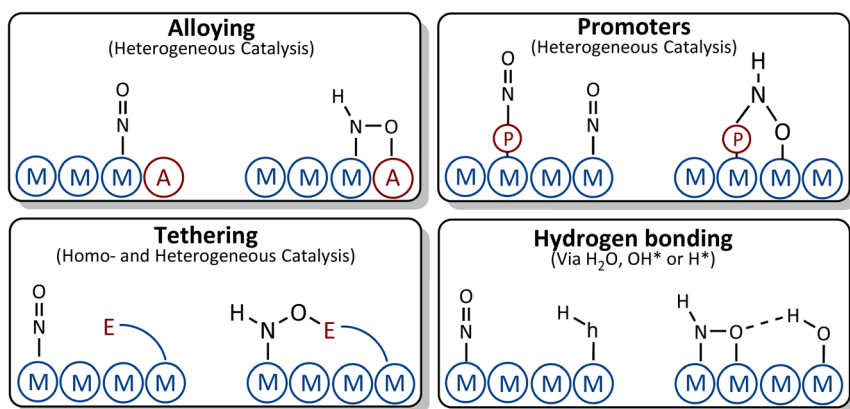


Fig. 8 Suggested strategies for breaking the scaling relations between *NO and *NOH/*HNO adsorbates.



(ii) Tethering and ligand stabilization: ligands are tethered to the surface or designed in such a way that they can geometrically interact with *NO and *HNO . The oxygen tail of *HNO makes another bond with the ligand which could result in *HNO stabilization, while the binding energy of *NO is less influenced by the ligand due to its vertical adsorption structure.

(iii) Promoters: the presence of a promoter on the surface can change the binding energies of *NO , *NOH and *HNO by introducing new adsorption sites, modifying the electronic structure of adsorption sites, or a combination of both.

(iv) Hydrogen bonding: *NHO and *NOH are geometrically more suitable for interacting with H-containing ligands through hydrogen bonds. This leads to a stronger stabilization of $^*NOH/^*HNO$ compared to *NO .

Fig. 7b shows a similar volcano plot to Fig. 7a constructed based on the linear scaling relationships for the intermediates bound through an oxygen atom. The two left legs of this volcano correspond to the $^*NO_3 \rightarrow ^*HNO_3$ and $^*NO_2 \rightarrow ^*HNO_2$ steps, and the right leg corresponds to the $^*HNO_3 \rightarrow ^*NO_2$ step. As discussed above, for Co, Ru and Ir the PLS was determined to be the formation of *HNO_3 from adsorbed *NO_3 . Fig. 7b shows that the trends in catalytic activity obtained from the free energy analysis agree well with the volcano-type analysis. In addition, by comparing Fig. 7b with Fig. 7a, we can see that the slopes for the elementary reactions corresponding to the most negative limiting potentials, U_L values, for the $^*NO_3 \rightarrow ^*HNO_3$ and $^*NO_2 \rightarrow ^*HNO_2$ steps are steeper than the one for the $^*NO \rightarrow ^*NOH$ step. This indicates that high NO_3RR catalytic activity can be achieved by tuning the oxygen affinities of transition metals for which $^*NO_3 \rightarrow ^*HNO_3$ is the PLS. This agrees with the recent theoretical-experimental study by Wang *et al.* on the NO_3RR over ultrathin CoO_x nanosheets where they showed that $^*NO_3 \rightarrow ^*HNO_3$ is the potential limiting step and suggested surface modification by surface oxygen atoms as an approach to tune the surface reactivity.⁷⁷

In addition, we would like to note that the PLS for Ir, Co, and Ru is different from the ones for the Cu, Pt, Ni, Rh, and Pd transition metals. This is presumably because these two groups of materials have different affinities for nitrogen and oxygen, rendering different potential limiting steps. This may also be the rationale behind the fact that transition metal oxides exhibit different NO_3RR catalytic activity than transition metals.^{43,78} For example, Wang *et al.* have reported a faradaic efficiency of 95.5% and selectivity of 81.2% for the NO_3RR to ammonia over Cu/ Cu_2O .³³ By comparing NO_3RR catalytic activity and selectivity on Cu/ Cu_2O with that of Cu, they found that CuO facilitates the formation of the *NOH intermediate compared with Cu, resulting in enhanced NO_3RR catalytic activity and selectivity. The latter might open new avenues for designing efficient catalysts for the NO_3RR .

So far, we have only considered activity criteria for designing efficient catalysts. Catalytic selectivity is one of the key criteria in determining the overall performance of catalysts. At negative potentials, the hydrogen evolution reaction (HER) competes with the NO_3RR . Therefore, in the following, further consideration will be given to the competing hydrogen evolution reaction.

Selectivity versus the HER

Beyond activity criteria, high selectivity towards the desired reaction products is a key factor in developing efficient catalysts for the NO_3RR . At negative potentials,



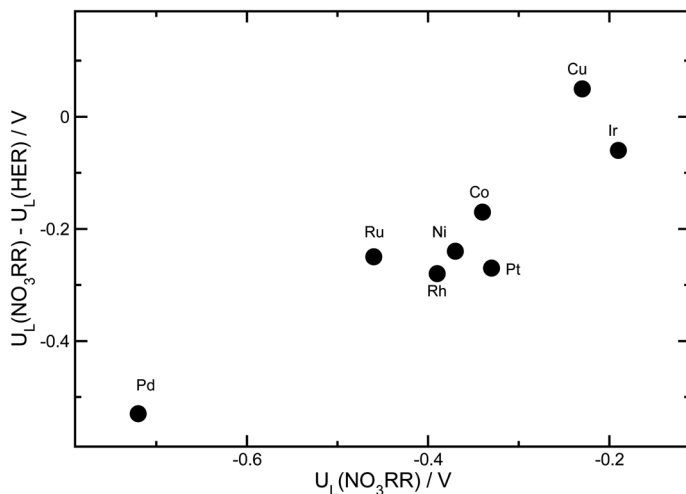


Fig. 9 The differences between the limiting potentials for the NO_3RR and HER, *i.e.*, $U_L(\text{NO}_3\text{RR}) - U_L(\text{H}_2)$, are plotted against the limiting potentials for the NO_3RR , $U_L(\text{NO}_3\text{RR})$, for different transition metals. $U_L(\text{NO}_3\text{RR}) - U_L(\text{H}_2)$ shows the trend in selectivity for the NO_3RR over the HER, and $U_L(\text{NO}_3\text{RR})$ reflects the trend in NO_3RR activity. The most promising catalysts lie in the upper-right corner of the plot.

the hydrogen evolution reaction (HER) strongly competes with the NO_3RR . The binding energy of $^*\text{H}$ has been shown to be a reasonable descriptor of hydrogen evolution activity for a wide variety of catalyst materials.^{79–81} To consider the trends in selectivity for the NO_3RR for transition metals, we follow a similar approach that has been used for the electrochemical reduction of CO_2 .^{82–84} It has been shown that the difference between the limiting potentials for CO_2 reduction and the HER captures the trends in selectivity. In Fig. 9, the difference between the limiting potentials for the NO_3RR reduction and HER, *i.e.*, $U_L(\text{NO}_3\text{RR}) - U_L(\text{H}_2)$, is plotted against the limiting potential for the NO_3RR , *i.e.*, $U_L(\text{NO}_3\text{RR})$, for different transition metals. More positive $U_L(\text{NO}_3\text{RR}) - U_L(\text{H}_2)$ corresponds to higher selectivity toward the NO_3RR over the HER. This implies that the catalysts that are in the upper right region exhibit simultaneous high activity and selectivity towards the NO_3RR . We would like to emphasize that this analysis does not evaluate the NO_3RR selectivity towards NH_3 or N_2 , rather it evaluates selectivity for the NO_3RR over the HER. The results, displayed in Fig. 9, suggest that Cu is the most active and selective catalyst for the NO_3RR . This agrees with previous experimental findings that reported Cu as one of the most promising catalysts for the NO_3RR . Fig. 9 also shows that Ir stands out as the next most promising transition metal for the NO_3RR . However, although Ir has higher catalytic activity than Cu, it exhibits lower selectivity towards NO_3RR products, making H_2 the dominant product under NO_3RR conditions.

Conclusions

Given the high emission intensities of conventional ammonia production from the Haber–Bosch reaction, methods such as the electrochemical reduction of



nitrate (NO_3RR) to ammonia appear attractive. Transition metals and transition metal oxides have been widely studied as potential catalyst materials for this reaction. However, the trends in the catalytic activity of the NO_3RR for different transition metals have remained unclear. Herein, we investigate the underlying reaction mechanisms of the NO_3RR to ammonia over different transition metal catalysts by calculating the binding energies of various reaction intermediates *via* Density Functional Theory (DFT). The binding energies of $^*\text{NO}$ and $^*\text{OH}$ adsorbates are identified as the reactivity descriptors using which we construct activity volcano plots and describe the trends in NO_3RR catalytic activity across different transition metals. This analysis shows that the protonation of either $^*\text{NO}$ or $^*\text{NO}_3$ is the bottleneck step causing large overpotentials for the NO_3RR to ammonia. In addition, we evaluated the selectivity toward NO_3RR products by considering the competition between the NO_3RR and HER. Our analysis explains why Cu is the most active and selective catalyst for the NO_3RR to ammonia. Ultimately, we suggest possible approaches for designing catalyst materials with reduced overpotential by tuning the binding energies of $^*\text{NO}$ and $^*\text{OH}$.

Computational details

Density Functional Theory (DFT) calculations using the QUANTUM ESPRESSO package were conducted to determine the adsorption energies of various adsorbates.⁸⁵ The Perdew–Burke–Ernzerhof (PBE) functional was used as the exchange correlation functional.⁸⁶ The ion–electron interaction is described by ultrasoft pseudopotentials.⁸⁷ For bulk metal nitrides, the Kohn–Sham wave functions were expanded in series of plane waves with a converged energy cut off of 550 eV and density cut off of 5500 eV. We investigate the NO_3RR on 8 transition metal surfaces: namely, the close-packed facets of Au, Ag, Cu, Pt, Pd, Ni, Ir, and Co. The surfaces were modeled using a periodic 2×2 unit cell with four layers of metal atoms for each slab repeated in a supercell geometry with at least 17 Å of vacuum between successive slabs (see the ESI† for various convergence tests). For face-centered cubic metals, namely Au, Ag, Cu, Pt, Pd, Ni, and Ir, the (111) facet is used. For Co metal with a hexagonal-close-packed crystal structure, the (0001) surface is used. Adsorption was allowed on only one side of the slabs. In all calculations, the bottom two layers were fixed in their bulk structure whereas the top two layers and adsorbates on them were allowed to relax in all directions until the convergence criterion of an energy difference of 10^{-4} eV was met on the self-consistent field (SCF) cycle and forces on all atoms were converged to be lower than $0.025 \text{ eV \AA}^{-1}$. We use a Monkhorst–Pack grid with dimensions of $4 \times 4 \times 1$ for sampling the first Brillouin zones.⁸⁸ All adsorption sites were considered and only the most stable ones are reported here. The computational hydrogen electrode (CHE) method introduced by Nørskov *et al.*⁶⁵ was used to calculate the free energy levels of all adsorbates. In this model, the free energy change of each electrochemical reaction step that involves an electron–proton transfer is calculated using the reversible hydrogen electrode (RHE), where the chemical potential of an electron–proton pair is equal to that of half of the hydrogen in the gas phase at standard conditions. The electrode potential is taken into account by shifting the electron energy by $-eU$ where e and U are the elementary charge and the electrode potential, respectively. The limiting potential is defined as the negative of the maximum free energy difference between any two successive



electrochemical steps. We applied a 1.12 eV correction to compensate for the DFT error of calculated formation energy of HNO₃. The free energies of adsorption are calculated from $\Delta G = \Delta E_{\text{DFT}} + \Delta(\text{ZPE} - TS)$, where ΔE_{DFT} is the calculated electronic adsorption energy at zero Kelvin, ZPE is the zero-point energy, S is the entropy, and T is the temperature. Adsorption free energies are calculated by using HNO₃ as a reference as suggested by Calle-Vallejo *et al.* taking into account zero-point energy and entropy corrections at $T = 300$ K.⁷² Zero-point energies and entropies were calculated using the finite difference scheme, within the rigid rotator/translator and harmonic oscillator approximation implemented in the Atomic Simulation Environment (ASE).⁸⁹ As noted above, throughout this paper, we restrict our investigation to possible intermediates occurring in proton and electron transfer reactions. Moreover, all free energies are calculated relative to HNO₃(g), H₂O(g), and H₂(g).

Conflicts of interest

There are no conflicts to declare.

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