

Cite this: *Chem. Sci.*, 2020, **11**, 2934

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Electron spin polarization generated by transport of singlet and quintet multiexcitons to spin-correlated triplet pairs during singlet fissions†

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Singlet fission (SF) is expected to exceed the Shockley–Queisser theoretical limit of efficiency of organic solar cells. Transport of spin-entanglement in the triplet–triplet pair state via one singlet exciton is a promising phenomenon for several energy conversion applications including quantum information science. However, direct observation of electron spin polarization by transport of entangled spin-states has not been presented. In this study, time-resolved electron paramagnetic resonance has been utilized to observe the transportation of singlet and quintet characters generating correlated triplet–triplet (T + T) exciton-pair states by probing the electron spin polarization (ESP) generated in thin films of 6,13-bis(triisopropylsilyl)ethynylpentacene. We have clearly demonstrated that the ESP detected at the resonance field positions of individual triplet excitons is dependent on the morphology and on the detection delay time after laser flash to cause SF. ESP was clearly explained by quantum superposition of singlet–triplet–quintet wavefunctions via picosecond triplet–exciton dissociation as the electron spin polarization transfer from strongly exchange-coupled singlet and quintet TT states to weakly-coupled spin-correlated triplet pair states. Although the coherent superposition of spin eigenstates was not directly detected, the present interpretation of the spin correlation of the separated T + T exciton pair may pave new avenues not only for elucidating the vibronic role in the de-coupling between two excitons but also for scalable quantum information processing using quick T + T dissociation via one-photon excitation.

Received 1st October 2019
Accepted 30th December 2019

DOI: 10.1039/c9sc04949e

rsc.li/chemical-science

Introduction

Recent remarkable advances in organic materials of organic semiconductors have achieved power conversion efficiencies (PCE) close to 17% (ref. 1–3) for single junction organic solar cells (OSCs), although the PCE is still lower than the recent developments of 22–23% in solar cells employing organolead halide perovskites.⁴ Solid-state organic thin films composed of electron donor (D) and acceptor (A) organic materials have been utilized for generating photocarriers from the photoactive layer of OSCs.⁵ Singlet fission (SF)⁶ is expected to exceed the Shockley–Queisser theoretical limit⁷ with PCE ~ 33% because two separated triplet excitons (T + T) can be produced from one excited singlet state (S_1S_0) sharing its excitation energy with a neighboring ground-state chromophore.⁸ Subsequent two charge-separation (CS) processes⁹ at the D:A domain interface

after individual triplet-exciton diffusion may boost the photocurrent density of OSCs in the solid state. Application of SF-induced triplet generation is also promising for boosting the organic light emitting diode (OLED) efficiency.¹⁰ Several studies clarified the initial multiexciton (TT in Fig. 1) generation mechanism from the S_1S_0 state.^{8,11–17} More importantly, elucidation of the $TT \rightarrow T + T$ dissociation mechanism is highly



Fig. 1 Schematic representation of the spin-correlated triplet pair (SCTP) state of $^{1,3,5}(T + T)$ generated by the SF in thin films of TIPS-Pn by the triplet energy transfer via the TT state.

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† Electronic supplementary information (ESI) available: Details on the simulations of time-dependent EPR data and on the modeling of sequential ESPT analysis based upon the SLE. See DOI: 10.1039/c9sc04949e

desired. Dissociation time constants ranging from sub-picosecond to microsecond regions are reported.^{16–25} However little is known about how the T + T dissociation or the decoupling^{12,16,24} occurs from the strongly coupled TT state.

In Fig. 1, the strongly coupled singlet TT state is known to be initially generated from the S_1S_0 state. Generation of the quintet state in the triplet–triplet pair^{17,22,23,25–28} has been reported and is thought to be essential for preventing the loss of the SF-born multiexciton through the singlet channels. Using the time-resolved electron paramagnetic resonance (TREPR) method for TIPS-tetracene thin films, Weiss *et al.*²⁶ characterized the SF-induced strongly-coupled quintet of $^5(TT)$ in Fig. 1. Quintet electron spin polarization (ESP) was detected as the microwave absorption (A) and emission (E) in $^5(TT)$ for frozen aggregates of SF-materials.²⁵ ESP was interpreted using the sublevel-selective quintet conversion by the zero-field splitting (ZFS) interaction at the singlet–quintet level-crossing in the presence of negative exchange coupling (J) during triplet exciton-diffusion and subsequent re-encounter in the highly disordered region, causing modulation of the J -coupling to result in spontaneous $^5(TT)$ generation.²⁵ Interestingly, transport of spin-entangled multiexcitons^{20,29–31} by the dissociative exciton diffusion has been observed using ultrafast transient absorption imaging of pentacene crystals³² and by the magnetic field effect on the fluorescence time-profiles. Although such transportation of spin-entanglements is key to elucidate the dissociation mechanism and to apply in quantum information science,^{33–35} no direct evidence for the transportation of spin-entanglements has been found in the separated T + T state with the singlet and quintet characters.

The present study thus focuses on how spin-entanglements develop and affect the direct TREPR detection of the T + T state. As shown in Fig. 1, when the triplet excitons are separated from each other to result in a negligible magnitude of exchange coupling ($J \approx 0$), spin correlations in the triplet–triplet pair may occur to induce diagonalized nine spin-states as the quantum superpositions of the singlet–triplet–quintet character through the spin–spin dipolar couplings of individual triplet species. This is quite similar to the spin-correlated radical pair (SCRPP) model^{33,34,36–42} in the photoinduced long-range charge-separation system generated by singlet or triplet precursors, causing the superpositions of the singlet–triplet characters when the J -coupling is small in the radical pairs. We herein demonstrate that the transportations of the SF-induced $^5(TT)$ and $^1(TT)$ characters can be distinguished on the T + T dissociation using the ESP of the correlated T–T state by applying TREPR spectroscopy to thin films of 6,13-bis-(triisopropylsilyl)ethynyl)pentacene (TIPS-Pn).

Methods

Chemicals and sample preparation

TIPS-Pn (Sigma-Aldrich) was used as received without further purification. 60 μ L of 60 mM TIPS-Pn solution in chloroform was spin-coated on thin cover-glasses of 1 cm² size using a spin coater (Mikasa MS-A100) with two different spinning rates of 300 rpm and 2000 rpm for 120 and 30 seconds, respectively.

Each fabricated thin film was manually cut within a medicine paper to produce many small films of *ca.* 0.3 mm³ and they were placed in EPR sample tubes with a 5 mm diameter. EPR tubes containing small pieces of films produced with different spinning rates are shown in Fig. S1 of the ESI.†⁴¹ This quantity of powder-like samples ensured an optical density of *ca.* 1 by the 532 nm laser and powder-pattern EPR analyses for the fabricated thin films, because the laser irradiation spot area was *ca.* 10 mm² which is much larger than one cut piece of the film. The films were then deaerated using a vacuum line under a vacuum pressure of 10^{−3} Pa to remove solvent and oxygen in the films. Nitrogen gas was then introduced into the tube through the vacuum line to ensure the film temperature for the EPR measurements.

Time-resolved EPR measurements

The X-band TREPR measurements were carried out using a Bruker EMX Plus system without using field modulation, as reported previously.⁴¹ The microwave power was 1.0 mW. Light excitations were performed by the second harmonic (532 nm) of a Nd:YAG laser (Continuum, Minilite II, fwhm \sim 5 ns with 0.5 mJ mm^{−2}). A laser de-polarizer (SIGMA KOKI, DEQ 1N) was placed between the laser exit and the microwave cavity. Temperature (80 K) was controlled by a cryostat system (Oxford, ESR900) using liquid nitrogen as the cryogen with a temperature controller (Oxford, ITC5035S).

Results and discussion

TIPS-Pn film morphology

Fig. 2 shows ground-state absorption spectra of the as-spun blend films. The absorbance obtained for each film was normalized by the strongest band intensity in the spectrum. When the spinning rate was high at 2000 rpm, the spectrum shape was similar to a TIPS-Pn solution spectrum, although the band widths were slightly broader in the film than in solution, indicating a weak chromophore interaction to form disordered morphology. On the other hand, the 300 rpm film (red line in Fig. 2) exhibits broader band shapes with an additional 700 nm

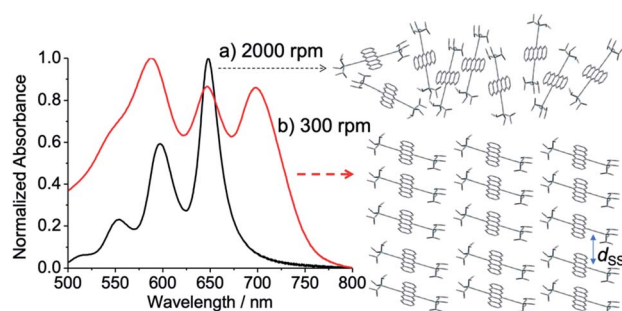


Fig. 2 Ground-state absorption spectra of as-spun TIPS-Pn thin films prepared with the spinning rates of (a) 2000 rpm (black) and (b) 300 rpm (red), representing that disordered and self-organized morphologies are dominant, respectively. d_{ss} represents site-to-site separation for the stepwise energy transfer.



band. This was explained by a strong chromophore coupling originating between the TIPS-Pn molecules indicating that the self-organized crystalline phase of TIPS-Pn is predominant, as reported previously.^{25,43–45}

TREPR spectra

Fig. 3 shows the TREPR data obtained by the 532 nm-laser excitation of the TIPS-Pc films at $T = 80$ K. At $0.2 \mu\text{s}$ after the laser irradiation, an A/E/A/E spin polarization was detected at the resonance field positions from the fine structures for the isolated triplet excitons of TIPS-Pn in Fig. 3a and b. As for the film spun at 2000 rpm, an additional E/A polarized splitting was imposed on the broad A/E/A/E pattern, as marked by asterisks and is explained by the strongly exchange-coupled $^5(\text{TT})$ signals, as reported previously^{25–27} (*vide infra*).

The broad A/E/A/E pattern was explained along with the T + T separation^{25,46} from $^5(\text{TT})$ in Fig. 1 to cause a dominant sublevel population at $m_s = 0$ among $m_s = +1, 0$ and -1 sublevels in the isolated triplet exciton. This is probably because $^5(\text{TT})_{m_s=0}$ may initially be populated during the modulation of the J -coupling; the initial geminate triplet-dissociation to $J = 0$ in T + T and the subsequent re-encounter to a large J with the spin decoherence by the exciton migration result in the $^5(\text{TT})_{m_s=0}$ populations.^{25,26} However, the A/E/A/E signals immediately disappeared, while the inverted ESP pattern of E/A/E/A polarization emerged after delay times larger than $0.4 \mu\text{s}$ in Fig. 3. Notably, the contribution from the E/A/E/A polarization in Fig. 3b is stronger when the self-organized crystalline phase is predominant for the film spun at 300 rpm (Fig. 2b) than in the disordered film in Fig. 3a. In our previous report, the absorptive ESP in the strongly exchange-coupled $^5(\text{TT})$ state was explained by sublevel-selective quintet populations and decoherences at $^5(\text{TT})_{-2}$,

$^5(\text{TT})_{-1}$ and $^5(\text{TT})_0$ by the singlet–quintet mixing through the zero-field splitting interaction (H_{TTZfs}) in the presence of the negative J during triplet exciton-diffusion and subsequent re-encounter in highly disordered regions.^{25,28} Thus, the strong absorptive feature in the initial A/E/A/E signals in Fig. 3a is consistent with T + T dissociation from $^5(\text{TT})_{-2}$ and $^5(\text{TT})_{-1}$ in the disordered film spun at 2000 rpm, because these sublevels possess the $\beta\beta$ -spin characters while the $\alpha\alpha$ -characters are absent (see eqn (4) and (5) below). The minor initial A/E/A/E contribution in Fig. 3b denotes the existence of such a disordered area in the as-spun sample for the high crystalline film. It is reported that the triplet exciton migration is significantly quick after the SF in pentacene crystals,³² suggesting that $^1(\text{T} + \text{T})$ dissociation may occur before the $^1(\text{TT}) \rightarrow ^5(\text{TT})_{m_s}$ decoherences in the crystalline film. Thus, the singlet character would be preserved as the transport of the spin-entanglement of the $^1(\text{TT})$ in the high crystallinity sample (Fig. 2b), while $^5(\text{T} + \text{T})$ characteristics may also be transported from $^5(\text{TT})$ in the disordered film (Fig. 2a). Therefore, in the following, we consider the spin correlation in the (T + T) state, as the spin-correlated triplet pair (SCTP).

Modeling electron spin polarization of the T + T state

To interpret the ESP (A/E/A/E and E/A/E/A polarizations) in the T + T dissociated character, spin eigenfunctions were obtained. The quintet, triplet and singlet basis functions of the triplet–triplet states are represented, as follows at the high field limit,⁴⁷

$$|^5(\text{TT})_{+2}\rangle = |++\rangle \quad (1)$$

$$|^5(\text{TT})_{+1}\rangle = \frac{1}{\sqrt{2}}(|+0\rangle + |0+\rangle) \quad (2)$$

$$|^5(\text{TT})_0\rangle = \frac{1}{\sqrt{6}}(2|00\rangle + |+-\rangle + |-+\rangle) \quad (3)$$

$$|^5(\text{TT})_{-1}\rangle = \frac{1}{\sqrt{2}}(|-0\rangle + |0-\rangle) \quad (4)$$

$$|^5(\text{TT})_{-2}\rangle = |--\rangle \quad (5)$$

$$|^3(\text{TT})_{+1}\rangle = \frac{1}{\sqrt{2}}(|+0\rangle - |0+\rangle) \quad (6)$$

$$|^3(\text{TT})_0\rangle = \frac{1}{\sqrt{2}}(|+-\rangle - |-+\rangle) \quad (7)$$

$$|^3(\text{TT})_{-1}\rangle = \frac{1}{\sqrt{2}}(|-0\rangle - |0-\rangle) \quad (8)$$

$$|^1(\text{TT})_0\rangle = \frac{1}{\sqrt{3}}(|00\rangle - |+-\rangle - |-+\rangle) \quad (9)$$

where $|+\rangle$, $|0\rangle$, and $|-\rangle$ are the triplet basis spins of $|\alpha\alpha\rangle$, $(|\alpha\beta\rangle + |\beta\alpha\rangle)/\sqrt{2}$, and $|\beta\beta\rangle$, respectively.

Under a very strong magnetic field, the energy levels of these wavefunctions are depicted as shown in Fig. 4a in the absence of zero-field splitting (ZFS) interactions of triplet excitons. As was



Fig. 3 Delay time dependence of the TREPR spectra after the 532 nm laser irradiation of the as-spun TIPS-Pn thin films prepared with the spinning rates of (a) 2000 rpm and (b) 300 rpm. Detection temperature was 80 K. Computed EPR spectra (red lines) were obtained by spin polarization calculations of the correlated T + T (Fig. 4 and 5) by the electron spin polarization transfer with the quintet and singlet precursors causing A/E/A/E and E/A/E/A patterns (Fig. S2†), respectively.





Fig. 4 Schematic representation of the sublevels of SCTP, as the weakly coupled multiexciton in (b) caused by the ZFS interactions ($D_1 = D_2 = 1080$ MHz) of $^3\text{TIPS-Pn}$. The energy shifts in the SCTP levels in (b) are shown with respect to the levels in (a) with $D_1 = D_2 = 0$ in the presence of the external magnetic field (340 mT) for highly separated T + T ($D_{\text{SS}} = 0$ and $J = 0$). The wavefunctions were computed for the field direction (B_0) parallel to the out-of-plane axes of the aromatic rings.

previously performed to obtain the eigenfunctions for strongly J -coupled multiexcitons,²⁵ the nine spin eigenvalues can be computed in the presence of the Zeeman interaction and of the ZFS interactions of triplet excitons to obtain the quintet, triplet and singlet TT states. Concerning the T + T dissociation, one may also obtain the nine eigen energies and corresponding eigenfunctions as shown by $|1\rangle, |2\rangle, \dots, |9\rangle$, in Fig. 4b.

The numerical computations of the nine eigenvalues were performed by diagonalizing²⁵ the spin Hamiltonian (H_{TT}) composed of the Zeeman interaction (H_{TTZ}), the spin-spin dipolar couplings (H_{TTZfs}) in the individual triplets, the spin-spin dipolar coupling between the triplets represented by $H_{\text{TTss}} = D_{\text{SS}}(\cos^2 \theta_D - 1/3)(3S_{1Z}S_{2Z} - S_1S_2)$,⁴⁸ and the exchange interaction ($H_{\text{TTee}} = -2J\mathbf{S}_1\mathbf{S}_2$). In H_{TTZfs} ($=S_1D_1S_1 + S_2D_2S_2$), S_i is the i -th ($i = 1, 2$) triplet spin operator in T + T and in TT, and D_i represents the zero-field splitting tensor of the individual triplet. Because the matrix of the H_{TTZfs} tensor is dependent on the orientation of the principal axes in the D_2 tensor (X_2, Y_2, Z_2) with respect to the principal axes in the D_1 tensor (X_1, Y_1, Z_1), the geometries of the second TIPS-Pn groups were generated by using Euler rotation angles (α, β, γ) with respect to the principal axes in D_1 . The D_2 principal axes were set to be collinear; i.e. (α, β, γ) = ($0^\circ, 0^\circ, 0^\circ$) with respect to (X_1, Y_1, Z_1). Direction ($d_{\text{S-S}}$) for the second triplet-state position in TT was set by the polar angles ($\theta_2 = 40^\circ, \phi_2 = 30^\circ$) with respect to the (X_1, Y_1, Z_1) principal axes. The direction of the external magnetic field (B_0) was set by the polar angles (θ, ϕ).²⁵ Thus, $\cos^2 \theta_D$ in H_{TTss} is defined for each B_0 direction, as reported previously.⁴⁹ Because the anisotropy in H_{TTZ} is much smaller, we assumed isotropic g -tensors ($g = 2.002$) for an external magnetic field strength around 340 mT in Fig. 3. When the B_0 direction is set to be parallel to both the Z_1 and Z_2 principal axes for the collinear T + T ($Z_1 \parallel Z_2$), the nine eigenvalues were obtained together with the wavefunctions, as shown in Fig. 4b. These levels are influenced by the anisotropic H_{TTZfs} causing energy shifts depending on the field direction (dotted arrows), and thus may produce the fine structure by the EPR transitions. For small J , sixteen of the allowed EPR transitions ($|1\rangle \leftrightarrow |2\rangle, |1\rangle \leftrightarrow |3\rangle, |2\rangle \leftrightarrow |4\rangle, |2\rangle \leftrightarrow$

$|5\rangle, |2\rangle \leftrightarrow |6\rangle, |3\rangle \leftrightarrow |4\rangle, |3\rangle \leftrightarrow |5\rangle, |3\rangle \leftrightarrow |6\rangle, |4\rangle \leftrightarrow |7\rangle, |4\rangle \leftrightarrow |8\rangle, |5\rangle \leftrightarrow |7\rangle, |5\rangle \leftrightarrow |8\rangle, |6\rangle \leftrightarrow |7\rangle, |6\rangle \leftrightarrow |8\rangle, |7\rangle \leftrightarrow |9\rangle$, and $|8\rangle \leftrightarrow |9\rangle$ in Fig. 4b and 5e) may contribute to the TREPR spectrum.

EPR line-shape analysis using the TT \rightarrow T + T jump dissociation model

Details on the computation method of the 9×9 matrices of the spin Hamiltonians were reported previously.²⁵ The wavefunction $|i\rangle$ ($i = 1, 2, \dots, 9$) of the diagonalized T + T state ($J = 0$) is represented as follows,

$$|i\rangle = \sum_j c_{ij} |\text{TT}\rangle_j \quad (10)$$

In eqn (10), j ($=1, 2, \dots, 9$) represents an eigenstate in the presence of the strong J coupling shown in eqn (1)–(9) where each equation number corresponds to the number of j . The transformation matrix can be described as,

$$U_{\text{T+T}} = \begin{pmatrix} c_{11} & c_{21} & c_{31} & c_{41} & c_{51} & c_{61} & c_{71} & c_{81} & c_{91} \\ c_{12} & c_{22} & c_{32} & c_{42} & c_{52} & c_{62} & c_{72} & c_{82} & c_{92} \\ c_{13} & c_{23} & c_{33} & c_{43} & c_{53} & c_{63} & c_{73} & c_{83} & c_{93} \\ c_{14} & c_{24} & c_{34} & c_{44} & c_{54} & c_{64} & c_{74} & c_{84} & c_{94} \\ c_{15} & c_{25} & c_{35} & c_{45} & c_{55} & c_{65} & c_{75} & c_{85} & c_{95} \\ c_{16} & c_{26} & c_{36} & c_{46} & c_{56} & c_{66} & c_{76} & c_{86} & c_{96} \\ c_{17} & c_{27} & c_{37} & c_{47} & c_{57} & c_{67} & c_{77} & c_{87} & c_{97} \\ c_{18} & c_{28} & c_{38} & c_{48} & c_{58} & c_{68} & c_{78} & c_{88} & c_{98} \\ c_{19} & c_{29} & c_{39} & c_{49} & c_{59} & c_{69} & c_{79} & c_{89} & c_{99} \end{pmatrix} \quad (11)$$

The EPR transverse magnetizations represented by $\text{Tr}(\mathbf{S}_y\rho)^{49,50}$ are proportional to factors determined by $S(S+1) \pm m_S(m_S \mp 1)$. Thus, the EPR intensities are proportional to 4, 6, and 2 for the transitions of $^5\text{TT}_{\pm 2} \leftrightarrow ^5\text{TT}_{\pm 1}$, $^5\text{TT}_0 \leftrightarrow ^5\text{TT}_{\pm 1}$, and $^3\text{TT}_{\pm 1} \leftrightarrow ^3\text{TT}_0$, respectively. Additionally, the transverse magnetizations are proportional to probabilities of finding the corresponding allowed transition characters³⁶ of $^5\text{TT}_{\pm 2} \leftrightarrow ^5\text{TT}_{\pm 1}$, $^5\text{TT}_0 \leftrightarrow ^5\text{TT}_{\pm 1}$, and $^3\text{TT}_{\pm 1} \leftrightarrow ^3\text{TT}_0$ in the mixed wavefunctions of eqn (10). Therefore, the EPR-transition intensity of $\text{Int}(i,k)$ between the $|i\rangle \leftrightarrow |k\rangle$ eigenstates (Fig. 5e) is formulated as follows:

$$\text{Int}(i,k) = 4|c_{i1}|^2|c_{k2}|^2 + 4|c_{i2}|^2|c_{k1}|^2 + 6|c_{i2}|^2|c_{k3}|^2 + 6|c_{i3}|^2|c_{k2}|^2 + 6|c_{i3}|^2|c_{k4}|^2 + 6|c_{i4}|^2|c_{k3}|^2 + 4|c_{i4}|^2|c_{k5}|^2 + 4|c_{i5}|^2|c_{k4}|^2 + 2|c_{i6}|^2|c_{k7}|^2 + 2|c_{i7}|^2|c_{k6}|^2 + 2|c_{i7}|^2|c_{k8}|^2 + 2|c_{i8}|^2|c_{k7}|^2 \quad (12)$$

Consequently, the EPR line-shape (SP) of the SCTP is computed as a function of the external magnetic field strength, as,

$$\text{SP}(i,k) = -\text{Int}(i,k) \frac{(\rho_{ii}^{\text{T+T}} - \rho_{kk}^{\text{T+T}})T_2}{1 + (\varepsilon_i - \varepsilon_k - \varepsilon_{\text{MW}})^2 T_2^2} \quad (13)$$

where T_2 represents the phase memory time. ε_{MW} denotes the angular frequency of the microwaves. The density matrix ($\rho^{\text{T+T}}$) of the T + T state will be detailed below. The spectrum computations can be performed by the powder pattern integration of $\sum_{ik} \text{SP}(i,k)$ from all possible field directions (θ, ϕ) to obtain the EPR spectra of T + T in Fig. 5.

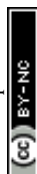




Fig. 5 Computed EPR spectra after the powder-pattern integrations of the T + T states (Fig. 4b) with $D_{SS} = 0$ and $J = 0$ in (a–c) and of the strongly-coupled $^5(TT)$ in (d) using the ZFS interaction of $^3TIPS-Pn$. (a) $^5(TT)_0$ -precursor SCTP showing the A/E/A/E pattern and (b) $^1(TT)$ -precursor case (Fig. 4b) resulting in the E/A/E/A pattern by the sequential ESPT model (green line in Fig. 7). (c and d) SCTP and strongly coupled $^5(TT)$ polarization computed with eqn (13) from the spin-state populations $\rho_{00}^{TT} = 0.75$, $\rho_{-1-1}^{TT} = 0.19$, and $\rho_{-2-2}^{TT} = 0.07$ in $^5(TT)$ in (e). (e) Computed T + T populations by eqn (15) are shown by red circles to explain the absorptive ESP in (c) and (d) corresponding to the 0.2 μs -spectrum in Fig. 3a. Sixteen allowed EPR transitions are shown to obtain the T + T spectra in (b) and (c) with the sublevel populations by the $^1(TT)$ precursor (green) and by the $^5(TT)$ precursor (red) from the blue circles, respectively.

When the spin-entangled $^1(TT)$ character is immediately transported to $^1(T + T)$ in Fig. 1 by the dissociation, one can expect that the populations occur in $|4\rangle$, $|5\rangle$, and $|6\rangle$ with $\rho_{44} = \rho_{55} = \rho_{66} = 0.33$ (green populations in Fig. 4b) as the singlet characters from the corresponding coefficients of the wavefunctions. Therefore, the state mixings in Fig. 4b would enable the ESP detection as SCTP polarization even if the EPR-silent singlet TT is the precursor, as was observed in the singlet-precursor SCRPP after the photoinduced charge-separation.³⁶ When the $^5(TT)_0$ state dissociates to form $^5(T + T)$ in Fig. 1, on the other hand, one expects overpopulation in $\rho_{66} = 0.66$ while $\rho_{44} = \rho_{55} = 0.17$ in Fig. 4b, resulting in different ESP from the singlet-precursor polarization.

We performed powder pattern integrations of the polarized EPR transitions to obtain the EPR spectra with the $^5(TT)_0$

precursor. For this, the density matrix (ρ^{T+T}) of the multiexciton was computed for the T + T system (Fig. 4b), as follows. H_{TT} ($=H_{TTZ} + H_{TTZfs} + H_{TTee} + H_{TTss}$) was first diagonalized to obtain the nine eigenfunctions of the strongly-coupled TT using $J = -60$ GHz, the ZFS parameters²² of $D = +1080$ MHz with $E = -18$ MHz for TIPS-Pn molecules with the collinear TT conformation, and $D_{SS} = -280$ MHz from an inferred contact T–T separation⁵¹ of 0.6 nm for the disordered regions (Fig. 2a). $J = -60$ GHz is one assumed value to compute the EPR spectrum for the strongly coupled TT state. Another input parameter of $J = -30$ GHz, as an example, will not affect the computation results. On the basis of the diagonalized quintets ($|TT\rangle_{j=1} = ^5TT_{+2}$, $|TT\rangle_{j=2} = ^5TT_{+1}$, $|TT\rangle_{j=3} = ^5TT_0$, $|TT\rangle_{j=4} = ^5TT_{-1}$, $|TT\rangle_{j=5} = ^5TT_{-2}$), triplets ($|TT\rangle_{j=6} = ^3TT_{+1}$, $|TT\rangle_{j=7} = ^3TT_0$, $|TT\rangle_{j=8} = ^3TT_{-1}$) and singlet ($|TT\rangle_{j=9} = ^1TT$), the density matrix ρ^{TT} was considered, as the initial conditions. Using this basis system, $H_{T+T} = H_{TTZ} + H_{TTZfs}$ was then diagonalized to obtain the 9×9 diagonal eigenvalues matrix and the eigenvectors matrix (U_{T+T}) in the absence of J , so that the following relation is satisfied:

$$\begin{pmatrix} \varepsilon_1 & & \\ & \varepsilon_2 & \\ & & \ddots \end{pmatrix} = U_{T+T} H_{T+T} U_{T+T}^T \quad (14)$$

For the diagonal system in Fig. 4b, the following density matrix is thus obtained as

$$\rho^{T+T} = k_{ESPT} U_{T+T} \rho^{TT} U_{T+T}^T \quad (15)$$

and is thus used to describe the spin-state populations (ρ_{ii}^{T+T}) in eqn (13) where $i = 1, 2, \dots, 9$ in the dissociated multiexciton, when the $TT \rightarrow T + T$ dissociation is treated to be a jump with rate constant represented by k_{ESPT} from $J = -60$ GHz to $J = 0$. This treatment is the same as the model of electron spin polarization transfer (ESPT).⁴⁰ In ρ^{TT} , $\rho_{SS}^{TT} = 1$ (where S represents 1TT in Fig. 6) can be set as the singlet population while the other 80 elements were set to be zero for the singlet-dissociation. In the $^5(TT)_0$ -precursor case, $\rho_{00}^{TT} = 1$ was considered where subscript 0 represents 5TT_0 . In the previous report, the quintet-state EPR spectrum was explained by isotropic sublevel populations at 5TT_0 , $^5TT_{-1}$, and $^5TT_{-2}$ in the disordered TIPS-Pn aggregates.²⁵ Thus, we also computed the quintet EPR spectrum of 5TT and the spectrum of the T + T state by using common quintet populations of $\rho_{00}^{TT} = 0.75$, $\rho_{-1-1}^{TT} = 0.19$, and $\rho_{-2-2}^{TT} = 0.07$ (blue populations in Fig. 5e) generated by the spin-conversion by the exciton-diffusion and the subsequent TT re-encounter.

Fig. 5a–c show the calculated SCTP polarization spectra obtained by the powder-pattern integration for the field directions in Fig. 4b. In Fig. 5a and b, $\beta = 0^\circ$ was assumed, while $\beta = 82^\circ$ is set in Fig. 5c. $\beta = 82^\circ$ reflects that the molecular conformation of the second triplet exciton (D_2 tensor in H_{TTZfs}) is changed by the T + T dissociation after SF because of the disordered morphology in Fig. 2a, while $D_1 = D_2$ is preserved upon the T + T dissociation in the crystalline region when $\beta = 0^\circ$. Thus, Fig. 5c is applicable for the 2000 rpm film (Fig. 3a). When the T + T dissociation mainly



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including the SQ_i coherences by numerically solving coupled stochastic-Liouville equations (SLE) to obtain the populations for the nine diagonalized eigenstates in Fig. 4e. We thus finally computed the diagonal elements ρ_{ii}^{T+T} as the populations in the SCTP levels by $\dot{\rho}^{T+T} = k_D U_{T+T} \rho_B^{TT} U_{T+T}^\dagger$,^{52,53} $\theta_2 = 90^\circ$ and $\phi_2 = -5^\circ$ were considered in the intermediate $T\cdots T$ as shown by geometry in Fig. S3[†] based upon the crystal structure.⁵⁸ $J = -11$ MHz was assumed for the $T\cdots T$ state. See ESI[†] for more details. Fig. 7 shows the dependence of the sequential triplet energy transfer rate constant (k_D) on the SCTP polarization by the triplet diffusion. Since D and J are both in the range of 10^{10} rad s^{-1} in the intermediate $T\cdots T$ in Fig. 6, it is anticipated that the SQ_0 coherences can be generated when the residence lifetime of the $T\cdots T$ state is larger than 10 ps and thus be transferred to the sublevel populations in the SCTP levels by the unitary transform of $U_{T+T} \rho_B^{TT} U_{T+T}^\dagger$. As expected, the ESP is stronger when the residence time ($\tau_T = 1/k_D$) becomes longer in Fig. 7. This E/A/E/A effect is relevant to the ESP by the chemically induced dynamic electron polarization^{54,55} in radical pairs creating the multiplet patterns (A/E and E/A, depending on J and D_{SS})⁵⁶ by the development of the $S-T_0$ coherences (ρ_{ST_0} and ρ_{T_0S}) in the singlet-triplet radical-pair system.⁵⁹

The experimental E/A/E/A antiphase spectra in Fig. 3 agreed with the sequential model as shown in Fig. S2[†]. Because the green spectrum (Fig. 7) computed with $k_D = 5 \times 10^{10}$ s $^{-1}$ only explains the experimental results τ_T of the $T\cdots T$ state is concluded to be short ($1/k_D = 20$ ps). In the crystalline phase of the TIPS-Pn film, the site-to-site separation (d_{SS}) between the TIPS-Pn molecules was estimated to be 0.4 nm from the crystal structure in Fig. 2a. The one-step site-to-site energy transfer rate constant may correspond to $k_D (=1/\tau_T)$ in Fig. 6. Thus, τ_T can be related to the diffusion constant (D_T) assuming that one-dimension diffusion⁵⁷ through the π -stacking

interaction is dominated by the Dexter-type energy transfer in Fig. 1, as follows,⁵⁸

$$D_T = \frac{d_{SS}^2}{\tau_T} \quad (16)$$

From eqn (16), $D_T \approx 10^{-4}$ cm 2 s $^{-1}$ is estimated from $\tau_T = 20$ ps to explain the antiphase ESP in Fig. 3b at 80 K. In a previous report, the triplet diffusion motion was investigated in the TIPS-Pn films by monitoring the triplet-triplet annihilation (TTA) kinetics.¹⁹ In this, $D_T = 2.7 \times 10^{-5}$ cm 2 s $^{-1}$ was obtained for a high crystallinity film at room temperature. The TTA rate constant may become smaller at 80 K to result in $D_T < 10^{-5}$ cm 2 s $^{-1}$.⁵⁷ One should note however that the geminate $T + T$ dissociative diffusion (Fig. 1) *via* the SF is quicker than the diffusion for the encounter of the free excitons in the TTA process. This is because, for the TTA, the exciton migration occurs *via* three-dimensional motion and thus is hindered in the minor disordered area during the long-distance diffusion ($L_D > 30$ nm, as the diffusion length).¹⁹ In contrast, the exciton-exciton separation (*ca.* 1 nm) in the primary $T\cdots T$ state (Fig. 6) is much shorter than L_D and thus exciton migration is free from the exciton-trapping³¹ in the crystalline phase. The above SF-induced $^1T\cdots T \rightarrow T + T$ spin-transportation with $\tau_T = 20$ ps is compatible with the previous reports of the corresponding dissociation dynamics (3.2 ps) in the crystalline TIPS-Pn film observed by the ultrafast spectroscopic measurements^{18,19} and with a recent magnetic field effect studied by Yago and co-workers²⁰ on SF-induced geminate triplet hopping kinetics (9 ps) in the fluorinated diphenyl-hexatriene crystals that form parallel stacking structures. From these reported picosecond dissociations at room temperature and from the present ps-dissociation at 80 K, the SF-induced geminate hopping dynamics is roughly temperature independent.³² Note that the hopping dynamics does not correspond to the initial dissociation kinetics k_f but k_D in Fig. 6.

Conclusion

We have established SF-induced electron spin polarization models for the weakly-coupled $T + T$ state as the quantum superposition (Fig. 4) of singlet-triplet-quintet wavefunctions by ZFS *via* the jump from the strongly coupled TT and *via* the sequential ESPT through the intermediate $T\cdots T$ state (Fig. 6) in TIPS-Pn thin films. From the ESP analysis, it is concluded that the SF-induced singlet TT character is transferred to the separated $T + T$ spin-state as quick transport of spin-entanglements with preserving the $S-Q_0$ coherence by picosecond jumps in the crystalline TIPS-Pn film, generating the E/A/E/A antiphase EPR spectra. Both of the singlet and quintet entanglements are revealed to be transported even in the amorphous film denoting the coexistence of ordered and disordered regions. This result is in line with the detection of the SF-induced quintet EPR signal at 0.2 μ s in Fig. 3a, because a minor crystalline region is required to generate quintet multiexcitons in amorphous aggregates, as reported in our previous study.²⁵



Fig. 7 k_D dependence of the EPR spectra for the $T + T$ state with $J = 0$ computed by the sequential ESPT model (Fig. 6) *via* the intermediate $T\cdots T$ state. k_f was fixed to be 10^{11} s $^{-1}$.



From the present data and the reported optical studies,^{18,19,32} the primary T + T hopping dynamics (k_D in Fig. 6) is suggested to be temperature independent. The picosecond-dynamics in the respective $^1T \cdots T \rightarrow T + T$ step in Fig. 6 strongly indicates that de-coupling of the J in the $^1T \cdots T$ state (Fig. S3)[†] plays a role in the T + T separation. From the temperature-independent dissociation kinetics,²² it is found that quick nuclear reorganization in $T \cdots T$ by high-frequency vibration motions²⁴ may play a role in the de-coupling, as previously proposed for pentacene dimers,¹² resulting in significant reduction of the orbital overlap between the triplet chromophores. This mechanism is also relevant to our recent low-temperature TREPR study for charge-separation geometries (distance ≈ 3 nm) in the bulk-heterojunction interfaces of organic solar cells; it was concluded that the high-frequency in-plane stretching reorganization within aromatic polymer backbones promoted 1D charge-dissociation at the D:A domain interfaces.⁴¹ The present SCTP spin polarization mechanism may thus pave new avenues to understand the nature of ultimate de-coupling and dissociation of two excitons for energy conversion. Although the coherent superposition of spin eigenstates was not directly detected, the present SCTP may be applicable to scalable quantum information processing *via* one-photon excitation because the sixteen possible EPR transitions from the nine sublevels (Fig. 5e) can be taken into account, which is significantly more scalable than the four EPR transitions³⁴ in SCRP.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

The work was supported by a Grant-in-Aid for Scientific Research (No. JP19H00888 and JP17K19105) from the Ministry of Education, Culture, Sports, Science and Technology (MEXT), Japan. We appreciate the support by Dr Hiroki Nagashima (Saitama University) in the TREPR measurements using the cryostat system. YK thanks Professor Tomoaki Yago (Saitama University) and Professor Tadaaki Ikoma (Niigata University) for fruitful discussions on the triplet diffusion dynamics.

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