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## Size-dependent photophysical properties of individual halide perovskite nanocrystal quantum dots

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Lead halide perovskites are unique semiconductor materials synthesized via low-temperature solution methods. They are expected to play a crucial role in next-generation optoelectronics, particularly in the advancement of solar cells and light-emitting devices. Lead halide perovskite nanocrystals exhibit luminescence properties not found in conventional cadmium selenide nanocrystals, which have been the subject of the most detailed studies to date. Consequently, these new material nanocrystals show great potential for innovative light-emitting device applications. This review paper summarizes the recent works of our group at Kyoto University on the low-temperature photoluminescence spectra of single perovskite nanocrystal quantum dots, emphasizing the size-dependent optical phenomena of excitons, trions, and biexcitons.

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### 1. Introduction

It is a great honor and a joyous occasion to celebrate the 65th birthday of Professor Nam-Gyu Park, a towering figure and pioneer in the field of high-efficiency perovskite solar cells. To commemorate this significant milestone and recognize his profound contributions, *Nanoscale* is organizing a special collection of papers. We are particularly pleased to have contributed to the fundamental physical and chemical understanding of this new class of perovskite materials and are delighted to

participate in this special review collection. This brief review summarizes the recent research achievements of the research group at Kyoto University focusing on halide perovskite nanocrystals (NCs) and discusses their intriguing properties and potential applications.

Lead halide perovskites (APbX<sub>3</sub>, where A = Cs, MA (CH<sub>3</sub>NH<sub>3</sub>), or FA (CH(NH<sub>2</sub>)<sub>2</sub>), and X = Cl, Br, or I) have been known for a long time, with the existence of CsPbX<sub>3</sub> first reported in 1893.<sup>1</sup> In the 1950s, it was discovered that CsPbX<sub>3</sub> possesses a perovskite structure and is photoconductive.<sup>2,3</sup> In 1979, MAPbX<sub>3</sub> was synthesized using an organic methylammonium (MA) ion as the A-site cation.<sup>4</sup> By 2009, MAPbI<sub>3</sub> was demonstrated as a viable light-absorbing material in dye-sensitized solar cells.<sup>5</sup> The potential of halide perovskites as

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solar cell materials are also suggested.<sup>6</sup> These halide perovskite materials truly entered the spotlight in 2012, when all-solid-state solar cells utilizing halide perovskites were reported with power conversion efficiencies of around 10%.<sup>7–9</sup> Even today, research on these materials is booming worldwide.<sup>10–15</sup> These ionic crystal semiconductors exhibit outstanding material properties for optoelectronic device applications; a direct bandgap structure,<sup>16,17</sup> defect tolerance nature,<sup>18,19</sup> high photoluminescence quantum yields (PLQYs),<sup>20,21</sup> and so on. Their material properties differ from those of conventional compound semiconductors. Our group at Kyoto University has also reported numerous achievements on halide perovskites, including: the direct bandgap determination of MAPbI<sub>3</sub> (1.61 eV),<sup>17</sup> band structures and polaron masses determined by non-linear and magneto-optical spectroscopy,<sup>22–26</sup> recombination dynamics of free carriers and free excitons,<sup>27–29</sup> the photon recycling effect,<sup>28–33</sup> the hot phonon bottleneck effect,<sup>34</sup> strong coupling between phonons and vacuum photons,<sup>35</sup> higher harmonic generation,<sup>36–38</sup> the photorefractive effect,<sup>39,40</sup> and non-linear optical responses in ferroelectric perovskites.<sup>41–43</sup> It is believed that our achievements also have contributed to elucidating the power-generation mechanisms of perovskite solar cells and to providing insights for further improving their photovoltaic efficiencies.<sup>44,45</sup> In addition, we have demonstrated the potential of halide perovskites for applications such as broadband light sources, optical phase modulators, and optoelectronic functional devices that integrate light emission with ferroelectricity. By employing advanced spectroscopic techniques, our research provides profound insights into the intrinsic carrier and exciton dynamics of unique halide perovskite semiconductors.

The study of NC quantum dots originated with Ekimov *et al.*, who synthesized semiconductor NCs within glasses and crystals, and successfully explained their optical properties through the quantum confinement effect.<sup>46,47</sup> Concurrently, Brus *et al.* explored colloiddally synthesized NCs in solution, observing size-dependent optical spectra.<sup>48,49</sup> Following this pioneering research, the photophysical properties of semiconductor NCs, including those of CuCl,<sup>50</sup> CdS,<sup>51</sup> Ge,<sup>52</sup> and Si,<sup>53–55</sup> have been actively investigated. A significant advancement in NC quantum dot research came in 1993 with Bawendi *et al.*'s successful hot-injection synthesis of high-quality cadmium chalcogenide (CdS, CdSe, and CdTe) NCs.<sup>56</sup> Core-shell CdSe NCs, with precisely controllable structure and composition *via* colloidal methods,<sup>57–59</sup> have since become pivotal materials in NC research. Their electronic structure and photoluminescence (PL) properties have been elucidated in detail, establishing them as one of the most extensively studied material groups in nanoscience.<sup>60</sup> More recently, halide perovskite NCs—novel semiconductor materials exhibiting unique optical properties not found in conventional inorganic semiconductors—have emerged as the focus of intense research, leading to new developments in their photophysics.

NCs of halide perovskite exhibit superior semiconductor properties while retaining the excellent optical properties of bulk crystals. They demonstrate almost 100% PLQYs, making

them particularly promising as practical luminescent materials.<sup>61,62</sup> Like compound semiconductor NCs such as CuCl and CdS, CsPbX<sub>3</sub> NCs were initially prepared by forming them in CsX crystal matrices, and their optical spectra were reported in the early stages of perovskite NC research.<sup>63–65</sup> However, few studies were conducted on these materials until the syntheses of high-quality perovskite NCs by the colloid chemistry method were reported around 2015.<sup>66–70</sup> As with CdSe NCs, the colloidal method, which synthesizes NCs in solutions, yields high-quality and luminescent materials. The development of a versatile solution synthesis method has enabled the production of NCs with controlled size and shape. Similarly, note that significant progress has been made in perovskite NC research. In addition to high PLQYs,<sup>67–73</sup> these perovskite NCs exhibit superior optical properties, such as a high radiative recombination rate at low temperatures.<sup>74,75</sup> These features are expected to be utilized in solar cells,<sup>76</sup> photodetectors,<sup>77</sup> light-emitting diodes (LEDs),<sup>78,79</sup> lasers,<sup>80,81</sup> and single-photon sources.<sup>82,83</sup> We have therefore clarified the fundamental properties of excitons, trions, and biexcitons, as well as the size dependence of exciton–phonon couplings, which are essential for these applications.<sup>84–90</sup>

This paper summarizes our recent advances in low-temperature PL measurements of single NCs, conducted to elucidate the optical properties of perovskite NCs. To ascertain the intrinsic properties of NCs—unaffected by size inhomogeneity and/or surrounding environment—it is crucial to perform measurements on numerous single NCs under consistent experimental conditions. Additionally, low-temperature measurements offer the benefit of sharpened PL spectra, which enables the clear observation of excitons, trions, and biexcitons,<sup>91–93</sup> as well as phonon sidebands arising from exciton–phonon couplings.<sup>94,95</sup> Through PL measurements of varying NC sizes, we have successfully determined the size dependence of fundamental properties of perovskite NCs, including trion and biexciton binding energies and exciton–phonon coupling constants. Here, we present our recent data and discuss the size dependence of the excited states of perovskite NCs.

## 2. Size dependence of PL peak energy

We synthesized solution-dispersed perovskite NCs of varying average sizes using the hot-injection method. CsPbBr<sub>3</sub> and CsPbI<sub>3</sub> NCs were synthesized as described in ref. 67, and FAPbBr<sub>3</sub> NCs as in ref. 70. Surface treatment was performed using ammonium thiocyanate (NH<sub>4</sub>SCN),<sup>96–98</sup> and perovskite NCs exhibiting nearly 100% PLQYs. We acquired the low-temperature PL spectra and size distributions of ensemble NC samples. Subsequently, we derived equations relating PL peak energy and size by fitting these experimental data to the formula in ref. 99, utilizing parameters listed in ref. 100–102. Fig. 1 illustrates the relationships between PL peak energy and size for CsPbBr<sub>3</sub>, FAPbBr<sub>3</sub>, and CsPbI<sub>3</sub> NCs at 5.5 K.<sup>84,85,87</sup>





**Fig. 1** PL peak energy vs. size for perovskite NCs of different compositions at 5.5 K. Numerical data are taken from ref. 85 for CsPbBr<sub>3</sub>, ref. 84 for FAPbBr<sub>3</sub>, and ref. 87 for CsPbI<sub>3</sub>.

Using these relationships, we determined the NC size from the PL peak energy obtained *via* single NC spectroscopy, thereby establishing the size dependence of the PL properties of individual perovskite NCs.

### 3. Fine structures of PL peak

Multiple peaks are in the low-temperature PL spectra of individual perovskite NCs. Fig. 2 presents representative PL spectra from single (a) CsPbBr<sub>3</sub>, (b) CsPbI<sub>3</sub>, and (c) FAPbBr<sub>3</sub> NCs at 5.5 K, with peaks attributed to excitons (Ex), trions (T), and biexcitons (Bx).<sup>87</sup> Their identification will be detailed subsequently. The experimental methodology for all PL spectral data within this paper is thoroughly described in ref. 84–88.

First, let us discuss the exciton peak, which is the most intense peak in Fig. 2. Fig. 3(a) shows that the exciton peaks observed in single CsPbBr<sub>3</sub> NCs exhibit two or three fine structure peaks,<sup>85</sup> with splitting widths of approximately 1 meV.<sup>103,104</sup> This phenomenon occurs because triplet excitons with three energy levels are bright in CsPbX<sub>3</sub>, and the orthorhombic crystal structure below room temperature allows these energy degeneracies to be resolved by the crystal field.<sup>75,105–108</sup> The bright triplet excitons at each of these energy levels possess transition dipoles in orthogonal directions, and the number of observed peaks depends on the orientation of the NCs relative to the detection side. Fig. 3(b) illustrates the polarization dependence of the exciton peak of a single CsPbBr<sub>3</sub> NC

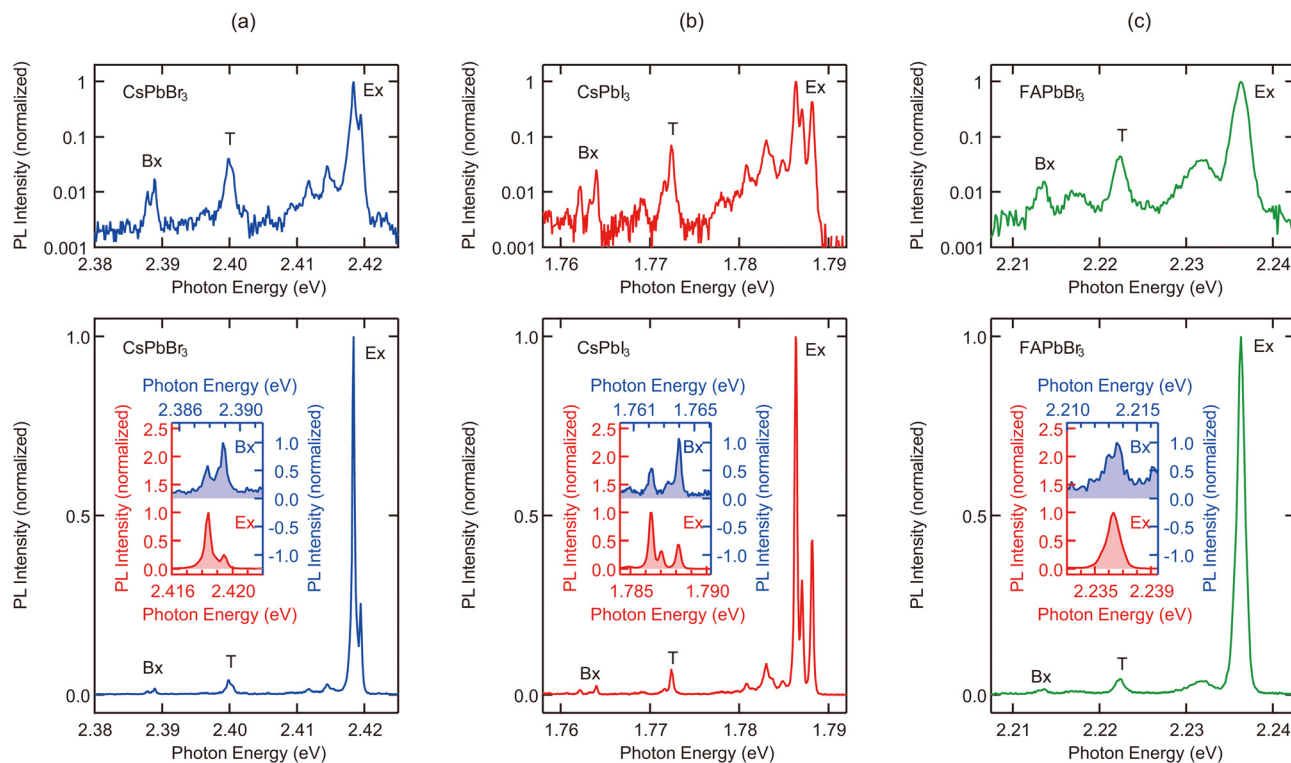
displaying two fine structure peaks.<sup>85</sup> Theoretically, the Rashba effect is predicted to raise the dark exciton level above the bright exciton level;<sup>75,99,109</sup> however, experimentally, PL peak from the dark exciton appears on the lower energy side of the bright exciton peak under a magnetic field.<sup>106–108</sup> There has been debate, both theoretical and experimental, regarding whether the lowest energy excitons are bright or dark.<sup>75,99,106–110</sup> In recent years, the crystal structure of halide perovskites has been revisited, and some studies have reported that they possess a polar monoclinic structure at low temperature.<sup>111</sup> Based on this structural model, several papers have also discussed the Rashba effect.<sup>112</sup> Our measurements on CsPbBr<sub>3</sub> NCs do not provide sufficient information to conclusively determine the crystal structure. How this difference in crystal symmetry influences phenomena such as exciton fine structure splitting remains an open question and will likely require further high spectral resolution measurements.

The fine structures observed in exciton peaks prove instrumental in identifying the origin of multiple peaks in perovskite NCs. As summarized in Fig. 2, the PL spectra of all-inorganic perovskite NCs are sharp, and their origins can be understood by analyzing the shapes of the peaks. Single peaks without any fine structures are trions. Since two holes have antiparallel spins to each other, no energy splitting due to electron–hole exchange interaction is observed in trion peaks. Conversely, as shown in the inset of Fig. 2, peaks with antisymmetric shapes to the exciton peaks are biexcitons, induced by biexciton–exciton cascade emission *via* the exciton fine structure levels. Other peaks, which have the same shape as the exciton peaks, are longitudinal optical (LO) phonon replicas, resulting from the coupling between excitons and LO phonons. Consequently, it is clear that trion and biexciton peaks, along with multiple LO phonon replicas (four for CsPbBr<sub>3</sub><sup>85</sup> and two for FAPbBr<sub>3</sub>,<sup>84</sup> to be discussed further), are present in the low-temperature PL spectra of single perovskite NCs. The insights derived from spectral shapes align with findings from the excitation power dependence of each peak's PL intensity and the LO phonon energy shift upon halide exchange.<sup>84</sup> With the origin of these multiple peaks now established, a detailed discussion of perovskite NC PL properties can proceed, as outlined below.

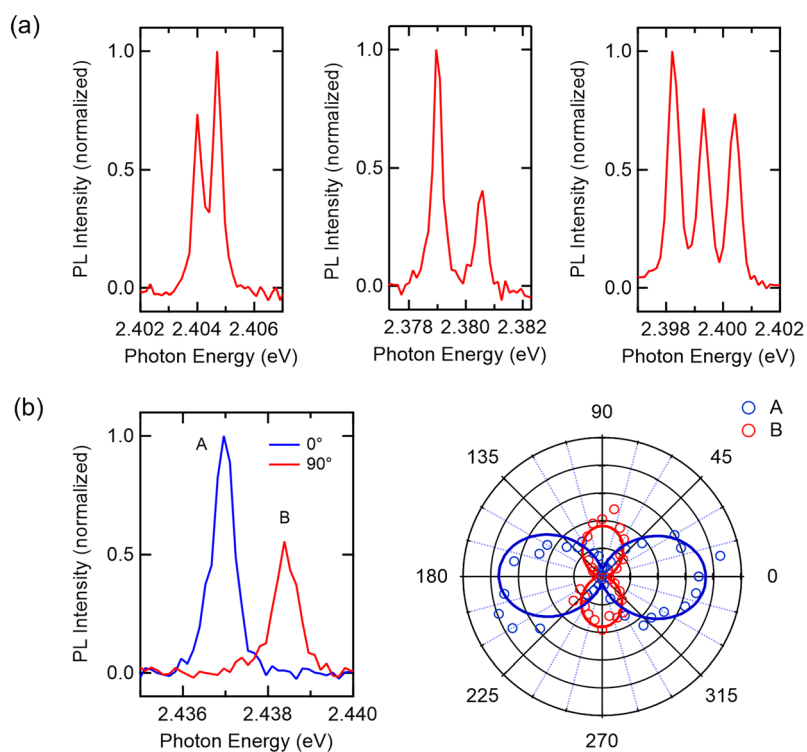
### 4. Trion and biexciton binding energies

Electron–electron and exciton–exciton interactions hold significant importance for applications, as they critically impact multiexciton generation (MEG),<sup>113–115</sup> laser gain,<sup>116</sup> blinking,<sup>117,118</sup> and single-photon purity.<sup>119–121</sup> A thorough understanding of these phenomena is therefore essential for practical utility. Regarding perovskite NCs, MEG,<sup>122,123</sup> low-threshold amplified spontaneous emission and lasing,<sup>124–129</sup> and high-purity single-photon generation<sup>130,131</sup> have been successfully demonstrated in connection with exciton complexes. To advance our comprehension of the exciton many-body





**Fig. 2** Representative PL spectra of single (a) CsPbBr<sub>3</sub>, (b) CsPbI<sub>3</sub>, and (c) FAPbBr<sub>3</sub> NCs at 5.5 K. Upper and lower panels are shown in logarithmic and linear scales, respectively. Inset shows comparison of the fine structure splitting of the exciton (red) and biexciton (blue) peaks. Reproduced with permission from ref. 87, © American Chemical Society 2024.



**Fig. 3** (a) Two or three exciton fine structure peaks in single CsPbBr<sub>3</sub> NCs. (b) Polarization dependence of the exciton peak with two fine structure peaks. Here, the maximum PL intensity of peak A is set to 0° (180°). Reproduced with permission from ref. 85, © American Chemical Society 2022.



effects in perovskite NCs, our investigation focused on the size dependence of trion and biexciton binding energies, along with a discussion of their underlying physical mechanisms.

In addition to excitons, trions (specifically, positive trions<sup>132</sup>) and biexcitons are generated in perovskite NCs, where they dominate the PL spectra and dynamics.<sup>133–135</sup> As depicted in Fig. 2, trion and biexciton peaks become observable at low temperatures. These PL peaks appear at lower energies than exciton peaks due to their binding energies. Consequently, the size dependence of trion and biexciton binding energies can be derived from the PL spectra. While numerous studies have explored the many-body effects of excitons, measurements of binding energies in conventional nanomaterials have been scarce. Reported examples include the diameter dependence for trions in carbon nanotubes<sup>136</sup> and the size dependence for biexcitons in CuCl<sup>137</sup> and CdSe/ZnS<sup>138</sup> NCs. In addition, no systematic measurements have been conducted on perovskite NCs.<sup>135</sup> Therefore, we measured and evaluated the size dependence of trion and biexciton binding energies in perovskite NCs of different compositions (CsPbBr<sub>3</sub>, CsPbI<sub>3</sub>, and FAPbBr<sub>3</sub>). Fig. 4 demonstrates that both trion and biexciton binding energies are independent of the A-site cations and X-site halide anions. Comparing our findings with theoretical calculations using the effective mass approximation highlights the importance of dynamic screening effects on the carrier many-body effect in perovskite NCs.

We discuss briefly the size dependence of the binding energies summarized in Fig. 4.<sup>87</sup> Using the elementary charge  $e$ , the Dirac constant  $\hbar$ , and the dielectric constant in the material  $\epsilon$ , the bulk exciton binding energy can be defined as  $\Delta_{\text{Ex,bulk}} = \frac{\mu e^4}{2\epsilon^2 \hbar^2}$  and the bulk exciton Bohr radius as  $a_{\text{B}} = \frac{\epsilon \hbar^2}{\mu e^2}$ . We normalized the trion and biexciton binding energies by the bulk exciton binding energy, and the NC size by the bulk

exciton Bohr radius. Fig. 4(a) and (b) show the normalized size dependence of the trion and biexciton binding energies, respectively. Following normalization, the data points for all compositions converge onto a single curve. This indicates that the eigenvalues of the trion and biexciton energies, when scaled by  $\Delta_{\text{Ex,bulk}}$ , in the many-body Hamiltonian are determined solely by the size scaled by  $a_{\text{B}}$ .<sup>108</sup> This suggests that the size dependence of the trion and biexciton binding energies of perovskite NCs follows universal scaling laws independent of composition. The binding energies exhibit minimal compositional dependence, being primarily governed by the quantum confinement effect. While theoretical discussions on binding energy size dependence have predominantly focused on CsPbBr<sub>3</sub> NCs,<sup>139–143</sup> this normalization method facilitates a discussion of the composition-independent, intrinsic size dependence of trion and biexciton binding energies in perovskite NCs.

To elucidate the physical properties underlying these binding energies, we conducted theoretical calculations. Nevertheless, the calculated trion and biexciton binding energies derived from the effective mass approximation were considerably smaller than our experimental observations. While dielectric screening is known to enhance binding energies,<sup>144–149</sup> our calculations reveal that this enhancement is insufficient to account for the experimental discrepancies. Indeed, the dielectric functions of bulk lead halide perovskites exhibit a strong dependence on the electric field frequency.<sup>150</sup> This substantial mismatch between experimental and theoretical results suggests that screening effects based on the static dielectric constant are inadequate. Instead, the dynamic screening effect,<sup>151,152</sup> which incorporates the frequency-dependent dielectric function, plays a pivotal role in perovskite NCs. Some previous studies have discussed the screening effect in the context of the polaron effect.<sup>140–143</sup> These compo-



Fig. 4 Size dependence of the normalized (a) trion and (b) biexciton binding energies. Reproduced with permission from ref. 87, © American Chemical Society 2024.



sition-independent binding energies offer vital insights for comprehending carrier many-body effects in perovskites.<sup>87</sup>

## 5. Exciton–phonon couplings

Due to their ionic crystal nature, lead halide perovskites possess more flexible lattices and larger phonon–phonon and electron–phonon couplings than other semiconductor materials.<sup>102,153</sup> Consequently, bulk samples exhibit polarons,<sup>25,154,155</sup> hot phonon bottleneck effects,<sup>34,156,157</sup> and strong anti-Stokes PL.<sup>158,159</sup> Electron–phonon couplings are also significant in perovskite NCs, profoundly impacting the relaxation lifetime of hot carriers,<sup>160–164</sup> the efficiency of optical cooling,<sup>165–172</sup> and the exciton coherence time.<sup>173–175</sup> Therefore, a deep understanding of exciton–phonon couplings is crucial for applying perovskite NCs in solar cells, optical refrigeration, and single-photon sources. The LO phonon replicas observed in the low-temperature PL spectra of single perovskite NCs are particularly useful for studying LO phonon energies and exciton–phonon coupling strengths.

Lead halide perovskites possess extremely complex phonon structures due to their numerous constituent elements and lattice softness.<sup>176</sup> Many phonon sideband peaks, specifically LO phonon replicas, appear in the low-temperature PL spectra of single perovskite NCs. Fig. 5(a) displays the phonon sideband PL of excitons (LO phonon replicas) in single CsPbBr<sub>3</sub> and FAPbBr<sub>3</sub> NCs at 5.5 K.<sup>85</sup> In CsPbBr<sub>3</sub>, four LO phonon replicas are observed, each mirroring the shape of the exciton peaks (labeled LO<sub>1</sub> to LO<sub>4</sub> from the low-energy side, respec-

tively). Conversely, in FAPbBr<sub>3</sub>, no exciton fine structure was observed; instead, only two broad LO phonon replicas were present.

To identify the origin of these LO phonon replicas, we compared them with theoretical calculations<sup>84,85,177</sup> and measured the energy shift of LO phonons induced by halide exchange.<sup>84</sup> According to the density functional theory calculations of phonon dispersions, incorporating the anharmonic approximation for bulk orthorhombic CsPbBr<sub>3</sub>, LO<sub>1</sub> corresponds to the collective vibration of the Cs atoms in the *xy* plane and a rotation of the PbBr<sub>6</sub> octahedra. LO<sub>2</sub> is attributed to the PbBr<sub>6</sub> rotation. LO<sub>3</sub> represents the in-plane motion of the Cs and two Br atoms in the same *xy* plane. Finally, LO<sub>4</sub> is the stretching mode of the Pb–Br bond in the PbBr<sub>2</sub> plane. The comparison of LO phonon replicas in single FAPbBr<sub>3</sub> and FAPbI<sub>3</sub> NCs reveals shifts in LO phonon energies that are consistent with the Br/I mass ratio. Therefore, the LO phonon replicas observed in the low-temperature PL spectra of individual perovskite NCs are generated by LO phonon modes involving the PbX<sub>6</sub> octahedra.

Unlike all-inorganic CsPbX<sub>3</sub> NCs, FAPbX<sub>3</sub> exhibits a broad exciton peak that lacks fine structure. Additionally, its phonon sidebands are broad. The lower-energy side (phonon energy: 4.5 meV) of the two LO phonon replicas in FAPbBr<sub>3</sub> is spectrally indistinguishable from the LO phonon replicas of the phonon modes corresponding to LO<sub>1–3</sub> in CsPbBr<sub>3</sub>. FAPbX<sub>3</sub> NCs exhibit such broad PL spectra because the FA cation possesses a significantly larger ionic radius than the Cs cation. This stronger interaction with the PbX<sub>6</sub> octahedron, coupled with the presence of random dipoles arising from anisotropy,



**Fig. 5** (a) Comparison of LO phonon replicas of single CsPbBr<sub>3</sub> and FAPbBr<sub>3</sub> NCs; four LO phonon replicas are observed in addition to exciton fine structure in CsPbBr<sub>3</sub>, while no fine structure is observed in FAPbBr<sub>3</sub> and two broad LO phonon replicas are observed. Reproduced with permission from ref. 85, © American Chemical Society 2022. (b) Size dependence of the LO phonon energies for single CsPbBr<sub>3</sub>. Reproduced with permission from ref. 85, © American Chemical Society 2022. (c) Size dependence of the LO phonon energies for single FAPbBr<sub>3</sub>. Reproduced with permission from ref. 84, © American Chemical Society 2021.



results in strong exciton–phonon coupling and large PL broadening compared to CsPbBr<sub>3</sub>. Single CsPbBr<sub>3</sub> NCs offer the advantage of very narrow PL spectra, enabling detailed analyses of the exciton fine structure peak and the exciton–phonon coupling for each LO phonon mode.

Fig. 5(b) and (c) show the energy difference between the exciton and phonon sideband peaks for CsPbBr<sub>3</sub> and FAPbBr<sub>3</sub> NCs, respectively.<sup>84,85</sup> This indicates the size dependence of the LO phonon energies. However, the phonon energies themselves do not depend on size. This is likely because the optical phonon dispersion curves around the  $\Gamma$  point of halide perovskites are nearly flat,<sup>178</sup> rendering the phonon confinement effect ineffective.<sup>54</sup> Conversely, as illustrated in Fig. 4, both trion and biexciton binding energies become larger for smaller NCs. This is because stronger confinement leads to larger Coulomb interactions.

To discuss the exciton–phonon coupling strengths, we obtained the Huang–Rhys factors from the relative PL intensity of the LO phonon replicas to the exciton peaks. Here, we focused on CsPbBr<sub>3</sub>, which exhibits narrow PL spectra, and evaluated the Huang–Rhys factors for the LO<sub>1</sub> and LO<sub>2</sub> modes. Additionally, we determined the Huang–Rhys factors for NCs with two exciton fine structure peaks. Fig. 6(a) shows these two peaks, labeled A and B, and the Huang–Rhys factors were evaluated for each peak.<sup>85</sup> Fig. 6(b) illustrates the dependence of the Huang–Rhys factor for peak B on exciton peak energy or size.<sup>85</sup> The Huang–Rhys factor increases with decreasing size. There was no significant difference between the Huang–Rhys factors for peaks A and B within the same NCs.

In general, the Huang–Rhys factor for exciton PL is greatly influenced by the spatial overlap of electron and hole wave

functions. As this overlap decreases, the Huang–Rhys factor increases.<sup>179</sup> An internal electric field present in the NCs may be responsible for enhancing the exciton–phonon couplings.<sup>180,181</sup> While an internal electric field has been demonstrated in perovskite NCs through the measurement of the quantum-confined Stark effect under an electric field,<sup>182,183</sup> its relationship with the Huang–Rhys factor has remained unclear.

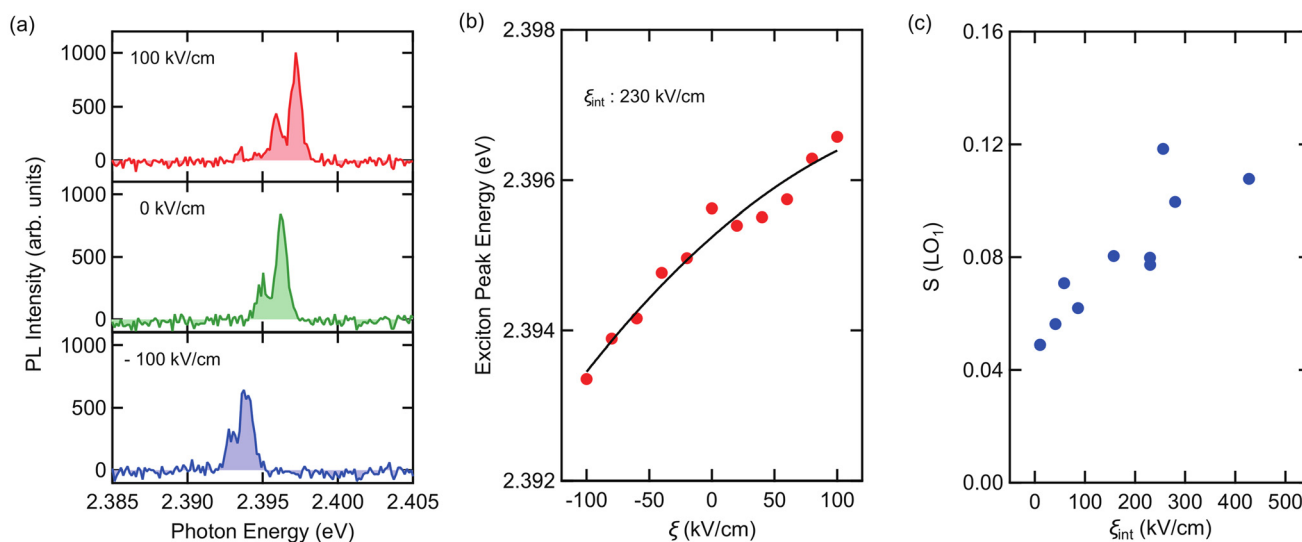
We observed the quantum-confined Stark effect by applying an electric field to single perovskite NCs and measuring the magnitude of their internal electric field.<sup>88</sup> Then, we examined the correlation with the Huang–Rhys factor when no external electric field was applied. Fig. 7(a) shows the response of the exciton peak of a single CsPbBr<sub>3</sub> NC when an external electric field was applied in the range of  $-100$  to  $100$  kV cm<sup>-1</sup>.<sup>88</sup> The direction of the energy shift differs for positive and negative biases, implying the presence of an internal electric field, like conventional CdSe NCs. We analyzed this energy shift in more detail. Stark shifts due to an applied external electric field generally exhibit parabolic shifts.<sup>180,182,183</sup> Fig. 7(b) shows the shift in exciton PL peak energy for the NC in Fig. 7(a) with respect to the applied electric field.<sup>88</sup> The closer the electrons and holes are to each other, the more the PL peak energy shifts toward higher energy. The electrons and holes are closest to each other at the vertex of the parabolic curve. This corresponds to the point at which the internal electric field is minimized, indicating the magnitude of the internal electric field.

Next, we examined the relationship between the internal electric field and the Huang–Rhys factor. As depicted in Fig. 7(c), the modulated internal electric field further influ-



**Fig. 6** (a) Exciton peaks and two LO phonon replicas (LO<sub>1</sub>, LO<sub>2</sub>) for single CsPbBr<sub>3</sub> NCs. The peaks are labeled A and B. (b) Exciton peak energy or size dependence of the Huang–Rhys factor in peak B ( $S_B$ (LO<sub>1,2</sub>)). The black dashed lines are the eye guides. Reproduced with permission from ref. 85, © American Chemical Society 2022.





**Fig. 7** (a) Exciton peak of a single CsPbBr<sub>3</sub> NC under 100 kV cm<sup>-1</sup> (red), 0 kV cm<sup>-1</sup> (green), and -100 kV cm<sup>-1</sup> (blue) electric fields. Exciton peak energies are different for positive (100 kV cm<sup>-1</sup>) and negative (-100 kV cm<sup>-1</sup>) biases. (b) Dependence of the average exciton peak energy of the two peaks of the NC shown in (a) on the applied electric field ( $\xi$ ). The solid line is the result of fitting by using parabolic curve. This NC shows an internal electric field ( $\xi_{\text{int}}$ ) of 230 kV cm<sup>-1</sup>. (c) Correlation between the internal electric field ( $\xi_{\text{int}}$ ) and the Huang-Rhys factor of LO<sub>1</sub> at 0 kV cm<sup>-1</sup> ( $S(\text{LO}_1)$ ) for single CsPbBr<sub>3</sub> NCs. Reproduced with permission from ref. 88, © American Chemical Society 2024.

ences the spatial distribution of electrons and holes, consequently altering the Huang-Rhys factor.<sup>88</sup> We observed that the internal electric field tends to be more pronounced in smaller NCs, attributable to their larger surface-to-volume ratio. The size-dependent internal electric field can originate from two primary mechanisms: (1) Surface charges: charges located on or around the NC surface.<sup>180,184–186</sup> In this scenario, for smaller NCs, the reduced distance between surface charges and charge carriers (electrons and holes) may enhance their separation. (2) Lattice distortion: distortions within the NC surface lattice.<sup>58,187</sup> Recent studies have reported changes in Cs–Cs bond lengths near the surface of CsPbX<sub>3</sub> NCs, potentially leading to surface polarization.<sup>188</sup> If this lattice distortion intensifies with the size-dependent surface strain of the NCs,<sup>189</sup> it could account for the amplified internal electric field observed in smaller NCs. Furthermore, the significant weakening of exciton–phonon couplings in perovskite NCs with a core-shell structure provides additional support for our finding that these couplings are highly sensitive to the NC surface.<sup>88,190</sup> These results suggest that exciton–phonon couplings can be effectively manipulated through the application of an electric field or by modifying surface structures.<sup>88</sup>

## 6. Temperature dependence of PL spectra

Lead halide perovskites exhibit three primary crystal structures: orthorhombic, tetragonal, and cubic. These structures are temperature- and A-site cation-dependent.<sup>191–193</sup> A notable observation in bulk samples is a significant band gap energy shift during the orthorhombic-to-tetragonal phase

transition.<sup>22,194,195</sup> Thus far, research on the PL properties of single perovskite NCs has mainly been performed at room temperature or liquid-helium temperatures, and there are few studies on the temperature dependence of PL properties over a wide temperature range.<sup>196–199</sup> Analyzing the temperature dependence of the exciton PL linewidth offers a valuable approach to investigate the impact of crystal phase transitions on exciton–phonon couplings. Furthermore, single NC spectroscopy is crucial for accurately determining the size dependence of the transition temperature and for eliminating the confounding effects of broad PL spectra caused by size inhomogeneity, which is a common issue in ensemble NC measurements.

Our study primarily investigated FAPbBr<sub>3</sub> NCs, which exhibit an orthorhombic-to-tetragonal phase transition between liquid-helium temperature and room temperature. Fig. 8(a) shows the temperature dependence of the PL spectrum of a single FAPbBr<sub>3</sub> NC up to 200 K.<sup>86</sup> For this NC, there is a temporal redshift of the PL spectrum around 130 K. A temporal redshift of the PL spectrum was observed around 130 K for this specific NC. To analyze these PL spectra, we performed multi-peak fitting using Gaussian or Lorentzian functions to extract the peak energies and linewidths, focusing solely on the exciton peak. Fig. 8(b) and (c) show the temperature dependence of the exciton peak energy and linewidth obtained by the fitting, respectively.<sup>86</sup> The solid line in Fig. 8(c) is the result of fitting using the formula in ref. 200. Although a shift in peak energy was noted around the phase transition temperature, there was no dramatic change in the linewidth. Our analysis of the temperature dependence of the PL linewidth indicates that the PL linewidth of single FAPbBr<sub>3</sub> NCs is predominantly determined by exciton–LO phonon coupling, specifi-





**Fig. 8** (a) Temperature dependence of PL spectrum of a single FAPbBr<sub>3</sub> NC. For this NC, a redshift of the PL peak energy is observed around 130 K (red arrow), which is the phase transition from orthorhombic to tetragonal. The solid line is the fitting result, with multiple Gaussian up to 40 K and double Lorentzian above 50 K. (b) Temperature dependence of the PL peak energy of a single NC shown in (a). The error bars are sufficiently small compared to the energy shift due to the phase transition around 130–170 K. (c) Temperature dependence of PL linewidth of a single NC shown in (a). (d) Size dependence of the orthorhombic-to-tetragonal phase transition temperature ( $T_{OT}$ ) of FAPbBr<sub>3</sub> NCs. Here the red circles are the data obtained in ref. 86 and the red open circle is the data obtained in ref. 199. The red dashed line is the phase transition temperature of FAPbBr<sub>3</sub> microcrystals ( $L > 100$  nm). The black dashed line is the eye guide. Reproduced with permission from ref. 86, © AIP Publishing 2023.

cally the Fröhlich interaction, with an LO phonon energy of 16 meV. Importantly, this coupling appears rarely affected by the crystal phase transition. It is worth noting that FAPbBr<sub>3</sub> possesses numerous LO phonon modes; therefore, the LO phonon energy and coupling coefficients derived in this study represent effective values. These findings align well with previous studies on single crystals and thin films of materials like MAPbX<sub>3</sub>,<sup>150,201</sup> where reported effective LO phonon energies and coupling coefficients are independent of crystal structure.

Fig. 8(d) summarizes the size dependence of the crystal phase transition temperature in single FAPbBr<sub>3</sub> NCs.<sup>86</sup> Here, the crystal phase transition temperature is defined as the point at which a redshift begins. As the NC size decreases, the crystal phase transition temperature also decreases. Generally, the Gibbs free energy of a crystal increases with decreasing NC size (*i.e.*, as the surface-to-volume ratio increases).<sup>202</sup> Consequently, the Gibbs free energy of the entire NC is inversely proportional to its size. This implies that, below a certain NC size, the tetragonal phase becomes more stable when its free energy is smaller than that of the orthorhombic phase. Like other semiconductor NCs where phase transition temperatures (such as melting point and crystal structure transition points) have been reported to decrease with decreasing size,<sup>203,204</sup> perovskite NCs also exhibit different crystal structures depending on their size and other factors.<sup>76,189,205,206</sup> Our study, utilizing single NC spectroscopy, clarifies the size

dependence of the crystal phase transition temperature in these perovskite NCs.<sup>86</sup>

## 7. Conclusions

This review paper summarizes the size-dependent PL spectra of perovskite NCs, obtained *via* low-temperature single NC spectroscopy, with a focus on exciton–exciton and exciton–phonon interactions. We demonstrate that trion and biexciton binding energies and exciton–phonon couplings increase as size decreases. Additionally, we found that the crystal phase transition temperature also decreases with decreasing size. The underlying physics for this size dependence remains poorly understood, lacking quantitative discussion and requiring robust theoretical support, particularly because conventional theoretical calculations fail to capture the combined effects of strong quantum confinement, lattice softness, dynamic disorder, and surface state in perovskite NCs. A deeper understanding of exciton many-body effects and exciton–phonon couplings in perovskite NCs has been instrumental in developing: highly efficient solar cells that use MEG and hot carriers for power generation,<sup>122,123,160–164</sup> low-threshold lasing,<sup>124–129</sup> high-efficiency LEDs and high-purity single-photon generation by manipulating nonradiative Auger recombination,<sup>130,131</sup> optical cooling by up-conversion



PL,<sup>165–172</sup> and quantum light sources with high monochromaticity and long exciton coherence time.<sup>173–175</sup> Moreover, carrier separation induced by the internal electric field contributes to the prolongation of the spin relaxation time,<sup>44</sup> thereby offering potential advantages for applications in optospintronic devices.<sup>207</sup> In this context, quantitative theoretical frameworks that can treat Coulomb interactions and exciton–phonon couplings simultaneously are critically needed. Moreover, not only the precise control of the NC size and shape but also the manipulation of the spatial electron wavefunction profiles *via* an electric field and surface treatment is essential for tuning Coulomb interactions and exciton–phonon couplings. Therefore, elucidating the size-dependent optical phenomena of perovskite NCs is crucial for the precision design and development of the devices that leverage their unique properties. Single NC spectroscopy enabled us to elucidate the fundamental photophysical properties of perovskite NCs which are difficult to observe with ensemble NCs. Moreover, the insights obtained from single NCs can inform the understanding and design of optical properties of ensemble NCs.<sup>208–212</sup> For example, they will lead to an understanding of novel optical functions of superlattices of perovskite NCs and their applications.<sup>213,214</sup> In particular, the size dependence of exciton many-body effects and exciton–phonon couplings revealed at the single NC level are expected to serve as key design parameters for engineering collective excitonic states and emergent optical functionalities in ordered NC superlattices. Perovskite NCs, synthesized *via* the colloidal method, are highly promising materials that possess the potential to create a wide range of functionalities.

## Author contributions

Kenichi Cho: visualization; writing – original draft; writing – review & editing. Yoshihiko Kanemitsu: funding acquisition; project administration; supervision; validation; writing – original draft; writing – review & editing.

## Conflicts of interest

There are no conflicts to declare.

## Data availability

No datasets were generated or analyzed during the current study. All relevant data are included in the cited literature.

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