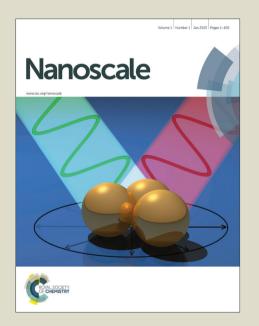
## Nanoscale

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## Resistive switching in metallic Ag<sub>2</sub>S memristors due to a local overheating induced phase transition

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Resistive switchings in nanometer-scale metallic junctions formed between an inert metallic tip and an Ag film covered by a thin Ag<sub>2</sub>S layer are investigated as a function of temperature at different biasing conditions. The observed switching threshold voltages along with the ON and OFF state resistances are quantitatively understood by taking the local overheating of the junction volume and the resulting structural phase transition of the Ag<sub>2</sub>S matrix into account. Our results demonstrate that the essential characteristics of the resistive switching in Ag<sub>2</sub>S based nanojunctions can be routinely optimized by suitable sample preparation and biasing schemes.

Self-assembled nanostructures with tunable electrical properties are intensively studied as potential candidates to replace nowadays CMOS devices. Conducting nanofilaments formed by reversible solid state electrochemical reactions between metallic electrodes have been demonstrated to be suitable for logical and non-volatile resistance switching random access memory (ReRAM) 1-15 operations at dimensions which are inaccessible for present day's silicon based technology. 16 The resistance of such a two-terminal device, called memristor, <sup>17</sup> is modified at higher bias voltages  $(V > V_{th})$ , while readout is performed at  $V \ll V_{\text{th}}$  without altering the stored informa-

Oxidation, activated ionic transport and reduction were identified as the leading mechanisms of nanofilament formation and rupture in solid state electrolytes 4,7,15,18-35 giving rise to resistive changes in the tunneling regime between insulating  $R_{\rm OFF} >> 10 \ {\rm M}\Omega$  and  $R_{\rm ON} \approx h/2e^2 = 12.9 \ {\rm k}\Omega$  resistance values, the latter often considered as the hallmark of atomic sized contacts. Such devices, however, could only be operated at reduced switching speeds due to their fundamental RC limitations. Intensive studies of the metallic regime with electrical conduction taking place via 10-15 nm wide filaments have been started recently in metal oxide based memristive systems

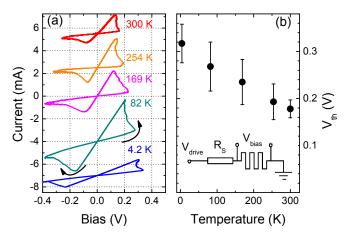
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where Joule heating assisted activated ion and/or oxygen vacancy migration have been found to play a key role in the observed resistive switchings. 36–38

Our previous experiments <sup>39,40</sup> based on the ionic conductor Ag<sub>2</sub>S have demonstrated reproducible, nanosecond timescale resistive switchings and a robustness against low voltage readout operations at room temperature exhibiting  $R_{\text{OFF}}/R_{\text{ON}}$  1 tios of 2-10. Resistive switching is attributed to metallic conduction channels with changing diameter in the range 2-5 nm while they are exposed to current densities as high as  $10^{10} \text{ A/cm}^2$ .

Here we report on extensive measurements and a thorough statistical analysis performed in order to explore the effect of the environment's temperature, the series resistance of the biasing circuit and the amplitude of the biasing signal on the technologically most relevant parameters, the ON and OFF switching threshold voltages,  $R_{ON}$  and  $R_{OFF}$ . We discuss the role of a highly non-equilibrium mechanism characteristic to the metallic regime. We demonstrate that our data is in quantitative agreement with a model taking pronounced power dissipation released at the nanojunction's length scale into account, giving rise to a local overheating of the junction up to the superionic phase transition of the Ag<sub>2</sub>S layer even at cryogenic ambient temperatures. This accelerates the field driven, thermally activated ionic migration processes as well as electro reactions. The observed resistive switchings are attributed to an enhanced filament reconfiguration accompanying the structural phase transition of the Ag<sub>2</sub>S matrix.

During sample fabrication a 80 nm thick Ag layer was deposited onto a Si substrate followed by a 5 minutes long sulfurisation resulting in a 30 nm thick stoichiometric Ag<sub>2</sub>S layer on top of the Ag electrode. 41 Nanometer-scale junctions were created between the Ag<sub>2</sub>S surface and a mechanically sharpened PtIr tip in an STM geometry. The  $V_{\text{drive}}$  triangular voltage output of a low output impedance data acquisition card was acting on the memristive junction and on a variable series resistor  $R_S$  as shown in the inset of Fig. 1(b). The device's current was monitored by a current amplifier operated at a typical gain of  $10^4$ . The  $V_{\text{bias}}$  voltage drop on the junction was determined numerically as  $V_{\text{bias}} = V_{\text{drive}} - I \cdot R_{\text{S}}$  where the 50  $\Omega$  in-

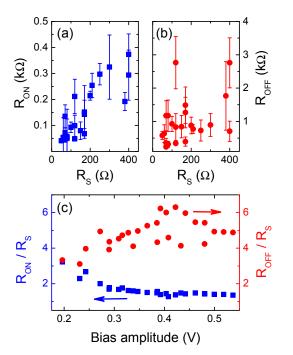


**Fig. 1** (a) Representative I-V traces of metallic PtIr-Ag<sub>2</sub>S-Ag junctions recorded at various temperatures from T = 4.2 K to room temperature. The direction of the loops indicated by the arrows was identical for all curves. The traces are vertically shifted for clarity. (b) The OFF to ON switching threshold voltage  $V_{\rm th}$  as a function of temperature. The dots and the error bars correspond to the average and standard deviation as evaluated for  $\sim 10^3$  traces at each temperature, respectively. The inset shows the electrical circuit diagram of the biasing setup.

put impedance of the current amplifier was also accounted for in  $R_{\rm S}$ . By convention, a positive bias corresponds to positive voltage applied to the Ag layer with respect to the PtIr electrode. The measurements were performed in the variable temperature insert of a standard <sup>4</sup>He cryostat between 4.2 K and room temperature. Approximately  $10^3$  stable current-voltage (I-V) traces were acquired at each temperature at various  $R_{\rm S}$  values ranging from 50 to 400  $\Omega$ .

Typical I-V traces recorded within 300 ms (corresponding to a typical, low bias sweep rate of 5-10 V/s) at selected temperatures are illustrated in Fig. 1(a). At low bias voltages the initial OFF state resistance  $R_{\rm OFF}$  is measured. Increasing  $V_{\rm bias}$  to a temperature dependent switching threshold  $V_{\rm th}=180-320$  mV a reconfiguration takes place resulting in a drop of the junction's resistance from  $R_{\rm OFF}\approx 10^3~\Omega$  to  $R_{\rm ON}\approx 10^2~\Omega$ . Decreasing  $V_{\rm bias}$  preserves  $R_{\rm ON}$  until a negative threshold of 80-250 mV is reached where the onset of the transition from the ON to the *initial* OFF state occurs. The direction of the resulting hysteresis loops was identical for all curves and is indicated by the arrows in Fig. 1(a). The monotonic decrease in  $V_{\rm th}$  with increasing temperature is emphasized by the statistical analysis of the  $\sim 10^4$  stable I-V traces (approximately 2000 at each temperature) as shown in Fig. 1(b).

The influence of  $R_{\rm S}$  on  $R_{\rm ON}$  and  $R_{\rm OFF}$  is shown in Fig. 2(a) and (b), respectively. The initial OFF state resistances are determined to a great extent by the controlled approach procedure of the STM tip and thus are not expected to exhibit any dependence on the biasing scheme. Consequently, a sys-



**Fig. 2** Average and standard deviation of the ON (a) and OFF (b) state resistances  $R_{\rm ON}$  and  $R_{\rm OFF}$  acquired at various temperatures at 4.2 K< T <300 K and at  $V_{\rm drive}^0$  = 0.6 V as a function of the series resistance  $R_{\rm S}$ . Note the different scale on (a) and (b). (c)  $R_{\rm ON}/R_{\rm S}$  (blue squares) and  $R_{\rm OFF}/R_{\rm S}$  (red dots) as a function of the bias voltage amplitude measured in a single junction at T = 300 K and  $R_{\rm S}$  = 50  $\Omega$ .

tematic  $R_{\rm S}$  dependence of  $R_{\rm OFF}$  was not observed, either, as demonstrated by the uniformly scattered red dots in Fig. 2(b). On the other hand,  $R_{\rm ON}$  is seen to be proportional to  $R_{\rm S}$  as indicated by the blue squares in Fig. 2(a). The latter behavior is attributed to the decreasing voltage drop on the junction as its resistance is decreasing toward  $R_{\rm S}$  upon an OFF to ON transition resulting in a rate limitation for a further resistanthange as discussed in Ref. 40. This is also in agreement with the observed dependence of  $R_{\rm OFF}$  and  $R_{\rm ON}$  on the bias voltage amplitude as displayed in Fig. 2(c) for a representative single junction measured at room temperature, i.e.  $R_{\rm ON}$  saturates at the scale of  $R_{\rm S}$  as the driving amplitude is increased.

Next we investigate the self-heating effect characteristic to nanometer-scale metallic junctions exposed to finite bias voltages and show that our data acquired over a broad temperature range from T=4.2 K to room temperature is consistent with a phase change model exploiting extensive power dissipation released in the junction's volume.

Power dissipation in point contacts is concentrated in a small volume around the contact center, leading to an elevated temperature in the junction area. <sup>42</sup> Assuming that only electrons subject to a diffusive motion carry the heat and the  $L_t$ 

inelastic diffusion length exceeds the d contact diameter, i.e.  $l_e < d < L_i$  with  $l_e$  being the elastic mean free path, the junction's local temperature is given by

$$T_J^2 = T^2 + \frac{9e^2}{4\pi^3 k_R^2} \frac{d}{L_i} V_{\text{bias}}^2,$$
 (1)

where T is the equilibrium temperature of the leads  $^{43}$  as it was demonstrated experimentally in ferromagnetic contacts by the observation of a finite bias induced ferromagnetic phase transition. 44 A detailed derivation of Eq. 1 along with the discussion of the so-called thermal  $(d > L_i)$  and ballistic  $(d < l_e)$ regimes are given in the Appendix. Inserting our typical junction diameters<sup>39</sup> of 2-5 nm,  $L_i \sim 10$  nm and the observed switching threshold of a few 100 mV into Eq. 1 reveals that the  $T_J = T_C = 451 \text{ K}$  bulk structural phase transition temperature of Ag<sub>2</sub>S is easily reached even at an ambient temperature of T = 4.2 K. While the low temperature acanthite phase of Ag<sub>2</sub>S is a semiconductor with very low conductivity, its high temperature argentite phase is a superionic conductor exhibiting a highly enhanced ionic mobility. 45 It has also been demonstrated  $^{8,22}$  that the bulk  $T_C$  is considerably reduced in the presence of an applied electric field facilitating the initial growth of the metallic Ag nanofilaments in high OFF state resistance devices. The detailed microscopical picture of the electric field driven ionic motion is a subject of ongoing molecular dynamical simulations. However, the above numerical estimation implies that a Joule heating assisted local superionic phase transition of the Ag<sub>2</sub>S solid electrolyte may play a major role in the observed resistive switchings. Based on a recent study on the dynamics of nanoscale metallic inclusions in dielectrics<sup>35</sup> we anticipate a continuous, bulk filament growth in our Ag<sub>2</sub>S system characterized by high oxidation and reduction rates as well as by a high ion mobility. 1 It is to be added that another relevant, highly non-equilibrium contributions, e.g. surface atom diffusion and electron wind forces, may also arise from the strong, inhomogeneous electric field and high current density, respectively.

Based on the above considerations we interpret the observed switching cycle along with the schematic illustrations displayed in Fig. 3 as follows. We point out that in a steady state the junction's temperature is determined by the  $P=I\cdot V_{\rm bias}$  power dissipation resulting in the emergence of isothermal regions along the  $I\cdot V_{\rm bias}=$  constant lines in the I-V plane of the device as indicated by the dashed lines in Fig. 3(b). Note that the steady state is classified here by a time scale which is shorter than that of the resistance change at the actual bias voltage <sup>40</sup> but long enough for the establishment of a stable temperature profile around the contact volume. We emphasize that the  $I\cdot V_{\rm bias}=$  constant equation of the isothermal lines directly follows from Eq. 1 by assuming an orifice-shaped, diffusive nanojunction where  $G=1/R=\sigma d$  with  $\sigma$  being the electrical conductivity <sup>46</sup> and thus  $T_J^2-T^2$  is pro-

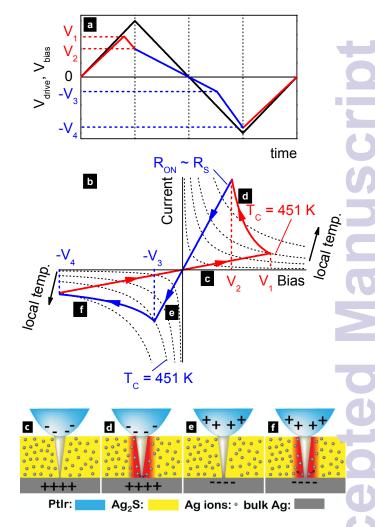


Fig. 3 (a) Schematic illustration of the recorded voltage signals.  $V_{\text{drive}}(t)$  (black) is the triangular voltage acting on  $R_S$  and the junction. The  $V_{\text{bias}}$  voltage drop is indicated by red (blue) in the OFF (ON) state. The four  $V_{\rm bias}$  values characterizing the resistive switching cycle are labeled accordingly. (b) Schematic illustration of the switching cycle at the I-V plane starting from the OFF state at zero bias in the framework of the thermally assisted phase change model. Along the dashed hyperbolae the  $I \cdot V_{\text{bias}}$  dissipated power along with the  $T_J$  local temperature of the junction are constant. Electrical conductance via the metallic filament in the OFF (c) and ON (e) states as well as during the OFF to ON (d) and ON to OFF (f) transitions are labeled on the I-V characteristics. (d) & (f) An enhanced filament growth/shrinkage is expected to take place when the local temperature of the biased junction reaches the  $T_C$  = 451 K critical temperature of the superionic phase transition of the Ag<sub>2</sub>S matrix in either field direction.

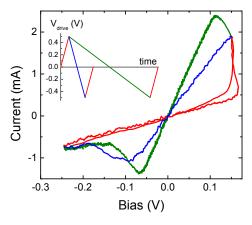
portional to  $G \cdot V_{\text{bias}}^2 = I \cdot V_{\text{bias}}$ . We believe that a narrowest cross-section dominating the electronic transport properties necessarily exists along the metallic filament and its shape

can be well approximated by an orifice-like profile. However, a nanowire-like, uniformly elongated constriction of the length l can also be taken into account here. In the latter case  $G = \sigma d^2/l$  applies, resulting in isothermal regions situated along the steeper,  $I \cdot V_{\rm bias}^3 =$  constant lines. In reality, these two scenarios can be considered as limiting cases for the isothermal lines corresponding to arbitrary filament geometries. The exact form of these lines, however, does not play a role in our argumentation.

Compared to the predictions of Eq. 1 the actual junction temperature may be reduced due to the fact that the filament is embedded in a semiconducting  $Ag_2S$  matrix exhibiting a finite heat conduction. However, based on its poor electrical conductivity we do not expect a considerable cooling power on the junction mediated by the acanthite phase  $Ag_2S$  in our non-planar arrangement.

While ionic motions do occur within the filament volume also at  $T_J < T_C$  leading to a slow reconfiguration of the conducting channel and thus to a small, systematic positive deviation from a linear I-V characteristics in the initial OFF state at a negatively charged inert electrode [Fig. 3(c)], the onset of an enhanced filament growth takes place when at  $V_{\text{bias}} =$  $V_1 = V_{\rm th}$  the local temperature around the contact reaches  $T_C$ and the surrounding Ag<sub>2</sub>S matrix enters its superionic phase [Fig. 3(d)]. Due to the the rapid filament growth taking place in the superionic argentite surrounding in the presence of strong electric fields during the OFF to ON switching,  $V_{\rm bias}$ can be decreasing while  $V_{\text{drive}}$  is still increasing. This is not only the consequence of the increasing fraction of  $V_{\text{drive}}$  dropping on the series resistance at higher current levels but is also in agreement with Eq. 1, i.e. at larger d the  $T_J \ge T_C$  condition can be fulfilled at lower  $V_{\rm bias}$ . At decreasing  $V_{\rm bias}$  during the transition the characteristic time scale of the resistance change is exponentially diverging as reported in Ref. 40. Consequently, a "final" ON state resistance is never strictly reached. However, any further resistance change would require either an unreasonably long time or unreasonably high  $V_{\rm drive}$ , as will be discussed below. Therefore the OFF to ON transition at a given voltage sweep rate is naturally terminated as the junction's resistance becomes comparable to  $R_S$ , in agreement with the data shown in Fig. 2(a).

At oppositely charged electrodes the direction of ionic motion is reversed and acts toward the (partial) destruction of the conducting filament [Fig. 3(e)]. In this field direction the  $T_J = T_C$  condition is fulfilled at a lower,  $V_3 < V_1$  bias in accordance with Eq. 1 as  $d_{\rm ON} > d_{\rm OFF}$ . Independently from the relation of  $V_1$  and  $V_2$ ,  $V_3 < V_2$  also holds because both points of the linear I-V trace belong to the same ON state exhibiting an identical resistance while they are subject to different driving voltages of  $V_{\rm drive}(2) > |V_{\rm drive}(3)|$ , as illustrated in Fig. 3(a) and (b). The  $V_4 > V_1$  relation relies on similar considerations. These arguments make it evident that the hys-

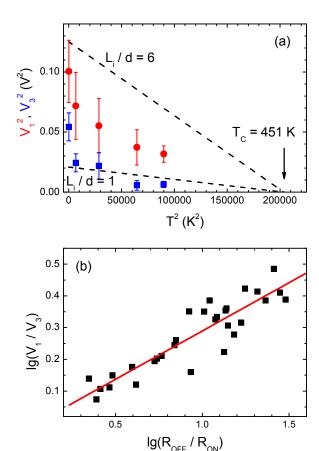


**Fig. 4** I-V traces of a single junction recorded at different voltage sweep rates after the OFF to ON transition. The inset illustrates the different driving schemes with -200 V/s (blue) and -2.5 V/s (green) sweep rates.  $V_{\rm drive}^0$ =0.5 V,  $R_{\rm OFF}$ =380 Ω,  $R_{\rm ON}$ =75 Ω (blue) and 45 Ω (green),  $R_{\rm S}$ =50 Ω.

teresis loops are necessarily asymmetric in  $V_{\text{bias}}$  exhibiting a longer and smoother transition from the ON to the OFF state than vice versa in full agreement with the representative traces shown in Fig. 1(a).

Another important consequence of the  $V_3 < V_1$  condition is  $T_I(2) > T_I(1)$ , i.e. the resistive switching is not an isothermal process. This implies that during a decreasing positive bia. further resistance change is expected to take place in the ON state as long as  $T_I > T_C$ . The competing time scales of this inherent resistance change and that of the driving signal are demonstrated in Fig. 4. A single device was identically biased to its OFF to ON transition within 2.5 ms by a triangular signal with an amplitude of  $V_{\text{drive}}^0$  = 0.5 V. This was followed by different voltage sweeps at rates of -200 V/s (blue trace) and -2.5 V/s (green trace). In the latter case the ongoing resistance change at higher biases corresponding to  $T_I > T_C$  resulted in a further, well visible decrease in  $R_{ON}$  and a rounded upper co ner of the hysteresis loop. On the contrary, the fast sweep rate in the former experiment outperformed the reduced rate of the resistance change and yielded to an apparent linear I-V trace and a sharp corner. The actual shape of the transition along with the achievable  $R_{\rm OFF}/R_{\rm ON}$  ratios are thus also largely determined by the frequency of the driving signal.<sup>40</sup>

At  $V_{\text{bias}} = V_3$  the Ag<sub>2</sub>S matrix becomes superionic again, fueling an accelerated filament destruction [Fig. 3(f)]. However, on the contrary to the one responsible for the OFF to ON switching, this process is inherently self-limiting as at a decreasing d the magnitude of  $V_{\text{bias}}$  necessary to keep the  $T_J = T_C$  condition satisfied is also increasing. Therefore, in order to achieve higher  $R_{\text{OFF}}$  values one has to supply an increased  $V_{\text{bias}}$ . The unambiguous identification of the terminating mechanism of the ON to OFF switching is not as straight-



**Fig. 5** (a)  $V_1^2 = V_{th}^2$  (red dots) and  $V_3^2$  (blue squares) as a function of  $T^2$ . The dots and the error bars correspond to the average and standard deviation as evaluated for  $\sim 10^3$  traces at each temperature, respectively. The dashed lines are calculated by Eq. 1 with  $T_J = T_C$ = 451 K and  $L_i/d$ = 6 (upper line) and 1 (lower line), the latter representing the thermal limit. (b) Logarithmic plot of  $V_1/V_3$  versus  $R_{\rm OFF}/R_{\rm ON}$  with a linear fit to the data.

forward as in the opposite case. However, the firm experimental finding that upon increasing the magnitude of the negative bias  $R_{OFF}$  always takes its initial value indicates that the Ag<sub>2</sub>S matrix exposed to the strong electric field in the vicinity of the filament has a limited capability to incorporate the dissolved Ag<sup>+</sup> ions and this saturation concentration is close to the stoichiometric value which is present at the beginning of the switching cycle. It is also to be added that in the Ag rich environment the argentite phase can survive even at room temperature. 22 Such residues may also contribute to the filament structure refining the simple picture of pure Ag channels depicted at Fig. 3.(c)-(f).

The relevance of the above scenario is further supported by re-plotting the  $V_1(T) = V_{th}(T)$  data of Fig. 1(b) along with the  $V_3(T)$  ON to OFF switching threshold voltages against Eq. 1 in a linearized fashion with  $T_J = T_C = 451$  K, as shown in Fig. 5(a). While the thermal limit with  $L_i/d = 1$  clearly remains unchallenged at the onset of the OFF to ON switching. even the low temperature enhancement in  $L_i$ , which presumably occurs due to suppressed phonon scattering, falls below an upper limit of  $L_i/d = 6$ . On the other hand, the ON to OFF switching takes place close to the thermal limit signalling that the relevant transport length scales,  $L_i$ , d and  $l_e$  fall close to each other within a few nanometers.

Figure 5(b) shows the relation of the ON and OFF switching threshold voltages to the corresponding  $R_{OFF}$  and  $R_{ON}$  values. As pointed out in the discussion of Eq. 1, the requirement that the onsets of both transitions must occur as  $T_J$  approaches the same  $T_C$  sets the condition of  $(V_1/V_3)^2 = (R_{\rm OFF}/R_{\rm ON})^{\alpha}$  with  $\alpha=1$  and  $\alpha=1/2$  for the two limiting junction geometries of an orifice and a uniform nanowire, respectively. Arbitrary junction geometries are manifested in the intermediate values of α. The satisfactory linear fit to the corresponding logarithmic plot displaying data acquired at all investigated temperatur and  $R_S$  values reveals  $\alpha = 0.61 \pm 0.06$  and thus provides 2 strong quantitative evidence to our picture.

In the intermediate regime situated on the verge of ballistic and diffusive conductance the  $d_{OFF}$  and  $d_{ON}$  average filament diameters are estimated based on the interpolating formula<sup>47</sup> relying on the Boltzmann equation for arbitrary ratio of  $d/l_e$ 

$$R = l_e/d \cdot \frac{16}{3\pi\sigma d} + \Gamma(l_e/d) \frac{1}{\sigma d},\tag{2}$$

where  $\Gamma(l_e/d)$  is a numerically determined monotonic function with  $\Gamma(0) = 1$  and  $\Gamma(\infty) = 0.694$ . Note that the first term is exactly the Sharvin resistance by putting the  $\sigma = l_e^2 n/\hbar k_F$ Drude conductivity into the formula, thus it is actually independent of  $l_e$ . The junction diameters are calculated by taking  $\lambda_F = 0.4$  nm being the Fermi wavelength in bulk Ag into account. This approximation results in the temperature independent values of  $d_{OFF}$ = 1.8±0.7 nm and  $d_{ON}$ = 4.8±1.2 nm confirming the range of validity of Eq. 1, i.e. the  $l_e \le d < 1$ assumption with  $l_e = 1.8$  nm being the elastic mean free path in argentite phase Ag<sub>2</sub>S. <sup>48</sup> These values are also in agreement with our recent study on the conducting channel distribution carried out by low temperature point contact Andreev reflection spectroscopy. <sup>39</sup>

In conclusion, we studied the resistive switching characteristics to metallic Ag<sub>2</sub>S nanojunctions. We propose that the dominating driving force of the resistance change in the highly non-equilibrium metallic regime is self-heating assisted electric field driven ionic transport giving rise to an intensive expansion/shrinkage of the metallic conduction channel as the bias dependent local temperature of the nanojunction approaches the superionic phase transition temperature of the surrounding Ag<sub>2</sub>S solid electrolyte. Based on the statistical analysis of  $\sim 10^4$  I-V traces acquired at different biasing conditions over a wide temperature range we found that the technologically most relevant parameters, the ON and OFF switching threshold voltages as well as  $R_{\rm ON}$  and  $R_{\rm OFF}$  are determined by the controllable means of sample preparation, the series resistance of the biasing circuit and the ambient temperature, in quantitative agreement with the proposed model. In spite of the self-assembling nature of filament formation/destruction, our results demonstrate the merits of engineering and large scale production of nanometer-scale  ${\rm Ag_2S}$  based memory cells exhibiting uniform behavior at technologically optimal device parameters.

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**Appendix.** In this appendix power dissipation and local overheating in nanometer-scale junctions are discussed. In biased point contacts the major part of the potential drops within a characteristic distance of d from the contact center thus the power dissipation is also concentrated in a small volume resulting in elevated junction temperatures under an applied voltage. Assuming that the heat is conducted just by the electrons, the equations of heat conduction can be solved for an arbitrary point contact geometry. <sup>49</sup> These calculations are valid in the so-called thermal regime, where the d contact diameter is larger than the  $L_i$  inelastic diffusive length. In this limit the  $T_J$  temperature of the contact center is determined by the bias voltage as

$$T_J^2 = T^2 + \frac{V_{\text{bias}}^2}{4L},$$
 (3)

where T is the temperature of the electrodes and  $\mathcal{L} = (\pi k_B)^2/3e^2$  is the Lorentz number. The power is dissipated inside the junction within a characteristic volume of  $\sim d^3$ . As the resistance of a diffusive contact is  $R = 1/\sigma d$  with  $\sigma$  being the electrical conductivity, <sup>46</sup> the dissipated power scales with the contact diameter as  $P = V_{\rm bias}^2 \sigma d$ . According to Eq. 3 these two factors give a contact temperature which is independent of d.

In smaller nanojunctions with  $d < L_i$  the potential also drops within a distance of d from the contact center. <sup>46</sup> However, in this regime the electrons must travel a distance of  $L_i$  to dissipate the energy gained from the potential drop. Therefore the power  $P = V^2 \sigma d$  is dissipated in a volume of  $\sim L_i^3$ , regardless of the contact diameter. As the magnitude of power dissipation scales with d whereas its corresponding volume is constant,  $T_J$  is expected to decrease with decreasing contact size. These considerations can be quantified by the following calculation.

We consider an orifice-like contact and assume that the power dissipation takes place within a sphere with radius b

around the contact whereas the  $\mathcal{P}$  power density is constant in this volume. The continuity equation for the  $\vec{j}_t$  thermal current density is given as

$$\oint_{A} \vec{j}_{t} d\vec{A} = \int_{V} \mathcal{P} dV. \tag{4}$$

The equation for the heat conduction is  $\vec{j}_t = -\kappa \vec{\nabla} T$ . If the heat is conducted solely by the electrons, the Wiedemann-Franz relation between the  $\kappa$  heat conductivity and the  $\sigma$  electrical conductivity is applied as  $\kappa = \mathcal{L}T \cdot \sigma$  thus  $\vec{j}_t$  can be written as  $\vec{j}_t = -\mathcal{L}\sigma T \vec{\nabla} T = -(\mathcal{L}\sigma \vec{\nabla} T^2)/2$ . Assuming that in the steady state the temperature depends only on the r distance from the contact center the continuity equation can be integrated as

$$2\pi r^2 \mathcal{L}\sigma \frac{d}{dr} T^2 = -\frac{4}{3}\pi b^3 \mathcal{P}, \text{ if } r > b$$
 (5)

$$2\pi r^2 \mathcal{L}\sigma \frac{d}{dr}T^2 = -\frac{4}{3}\pi r^3 \mathcal{P}, \text{ if } r < b, \tag{6}$$

with the boundary condition of  $T(r) \to T$  at  $r \to \infty$ .

In a voltage biased diffusive contact  $\mathcal{P} = (V_b^2/R)/(4\pi b^3/J_a)$  and  $R = 1/\sigma d$ , so the temperature of the junction at r = 0 is

$$T_J^2 = T^2 + \frac{3}{4\pi} \frac{V_{\text{bias}}^2}{f_c} \frac{d}{h}.$$
 (7)

In the thermal regime the power is dissipated in a characteristic distance of d from the contact center, thus b = d should be substituted into Eq. 7 in agreement, apart from a small deviation in the numerical coefficient, with Eq. 3.

As this simple calculation successfully reproduces the known results in the thermal limit, it can also be employed for smaller contacts with  $d < L_i$ . In this case  $b = L_i$  is to be inserted into Eq. 7 with the proper coefficient adopted from Eq. 3 as

$$T_J^2 = T^2 + \frac{V_{\text{bias}}^2}{4\mathcal{L}} \frac{d}{L_i}.$$
 (8)

Equation. 8 shows that  $T_J$  is reduced in smaller contacts and the magnitude of this reduction is determined by  $d/L_i$ .

In even smaller contacts with  $d < l_e$  the electrons perform a ballistic motion and the resistance is determined by the Sharvin formula,  $R = 16l_e/3\pi d^2\sigma$  thereby the temperature of the junction is written as

$$T_J^2 = T^2 + \frac{9}{64} \frac{V_b^2}{\mathcal{L}} \frac{d^2}{L_i l_e}.$$
 (9)

It must be noted that the validity of these calculations ir the  $d < l_e$  regime is limited. As the electrons can only thermalize within a characteristic distance of  $L_i$ , the equations of heat conduction are not strictly applicable at shorter length scales. However, while the major part of the temperature increase takes place at a longer length-scale of  $r > L_i$ , the above

formulae still provide a good estimation for the contact temperature within an error of  $\sim 33\%$ . These calculations are also overestimating  $T_J$  when not only the distant electrodes are cooled but the whole contact surface, for instance, in measurements performed at ambient conditions.

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