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Sodium-Ion Battery Cathodes Na₂FeP₂O₇ and Na₂MnP₂O₇: Diffusion Behaviour for High Rate Performance

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The Na-ion battery is currently the focus of much research interest due to its cost advantages and the relative abundance of sodium compared to lithium. Recently, the pyrophosphate family of cathodes has attracted considerable attention, particularly $\text{Li}_2\text{FeP}_2\text{O}_7$ due to its high operating voltage and enhanced safety properties; in addition the sodium-based compounds $\text{Na}_2\text{FeP}_2\text{O}_7$ and $\text{Na}_2\text{MnP}_2\text{O}_7$ are also generating interest. Herein, we present defect chemistry and ion migration results, determined via atomistic simulation techniques, for $\text{Na}_2MP_2\text{O}_7$ (where M = Fe, Mn) as well as findings for $\text{Li}_2\text{FeP}_2\text{O}_7$ for direct comparison. Within the pyrophosphate framework the most favourable intrinsic defect type is found to be the cation anti-site defect, in which alkali-cations (Na/Li) and M ions exchange positions. Low activation energies are found for long-range diffusion in all crystallographic directions in $\text{Na}_2MP_2\text{O}_7$ suggesting three-dimensional (3D) Na-diffusion. In contrast $\text{Li}_2\text{FeP}_2\text{O}_7$ supports 2D Lidiffusion. The 2D or 3D nature of the alkali-ion migration pathways within these pyrophosphate materials means that antisite defects are much less likely to impede their transport properties, important for high rate performance.

1. Introduction

The portable energy storage market has been dominated by Liion batteries in the past two decades¹⁻⁷ due to their lightweight, high energy density and high power, which all depend critically on fast Li-ion mobility. Despite the wide-spread use of Li-ion cells, batteries based on alternative carrier ions such as sodium ions could be more suitable for large-scale energy storage systems. Whilst the higher gravimetric capacity afforded by Liion cells is critical for portable applications, the relative abundance and low cost associated with Na-ion batteries now make them an attractive alternative for grid storage.^{8,9}

Substantial effort has been expended in previous decades to prepare electrode materials that can easily intercalate and transport Na-ions at suitable potentials. Among positive electrode materials, a variety of layered oxides (e.g. NaxCO₂, NaCrO₂, NaVO₂, Nax[Fe_{0.5}Mn_{0.5}]O₂) and polyanionic compounds (e.g. NaFePO₄, Na₃V₂(PO₄)₃, Na₂FePO₄F, NaFeSO₄F) have been reported¹⁰⁻¹⁷.

Recently lithium pyrophosphate-based materials including $\text{Li}_2\text{FeP}_2\text{O}_7$ and $\text{Li}_2\text{Fe}_x\text{Mn}_{1-x}\text{P}_2\text{O}_7$ ($0 \le x \le 1$) have been examined,¹⁸⁻²⁰ which show good electrochemical and thermal properties. It was found that $\text{Li}_2\text{FeP}_2\text{O}_7$ exhibited a redoxpotential of 3.5 V vs Li/Li⁺ while showing a reversible capacity of ~105 mAhg⁻¹,¹⁸ whilst for the mixed-metal pyrophosphate it was found that the partial substitution with Mn was observed to

increase the Fe³⁺/Fe²⁺ redox potential.¹⁹ This pyrophosphate structure can offer partial upshift of Fe³⁺/Fe²⁺ redox potential approaching 4 V (vs Li/Li⁺) independent of cationic size and redox activity of 3d metal substituants.²¹ A universal Fe-redox upshifting near 4 V, the highest reported value matching the triplite LiFeSO₄F cathode, can be registered in this (PO₄)³⁻oxyanionic system without using more electronegative and hygroscopic (SO₄)²⁻ and/or F⁻ anions.²² In addition to this high-voltage redox tunability, it is expected that the framework provided by the pyrophosphate anion will give rise to cathode materials with enhanced thermal stabilities.²³

Motivated by the significance of Na-ion batteries for largescale storage systems in addition to the promising properties of Li₂FeP₂O₇, attempts were made to synthesise a sodium version of the Fe-based pyrophosphate (Na₂FeP₂O₇),²⁴⁻²⁶ as well as other Na-analogues with different transition-metal active redox species such as a new Mn-based polymorph, β -Na₂MnP₂O₇.^{27,28} Yamada *et al.*²⁴ were able to prepare Na₂FeP₂O₇ via a conventional one-step solid-state synthesis, and found it to be electrochemically active, delivering a re-versible capacity of 82 mAhg⁻¹ with an operating voltage around 3 V (vs Na/Na⁺). The combination of low cost materials, moderate theoretical capacity (~100 mAhg-1), high rate kinetics and good thermal stability makes Na₂FeP₂O₇ a highly promising Na-ion battery material. From a crystal structure view-point, the change of alkali ions from Li to Na results in different crystal

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frameworks: while $Li_2FeP_2O_7$ adopts the monoclinic ($P2_1/c$) structure¹⁸, Na₂FeP₂O₇ adopts the triclinic (P-1) structure²⁵.

Recently β -Na₂MnP₂O₇²⁷ has also been proposed as a new pyrophosphate cathode for sodium-ion batteries, and found to offer similar (if not slightly superior) electrochemical performance to Na₂FeP₂O₇. Na₂MnP₂O₇ displayed a discharge capacity close to 80 mAhg⁻¹ (at 25 °C) with a voltage of 3.6 V, the highest Mn³⁺/Mn²⁺ redox potential amongst all Mn-based cathodes. The electrochemical activity of the Mn-containing cathode material is noteworthy, when compared to the Li counterpart (Li₂MnP₂O₇), which is almost inactive at room temperature owing to its sluggish kinetics.²⁸ The β -Na₂MnP₂O₇ polymorph crystallise in the triclinic (*P*1) space group²⁷, isostructural to rose-polymorph of Na₂COP₂O₇.²⁹

The present study uses advanced simulation techniques to investigate important issues related to point defects and alkali (Na/Li) ion migration in Na₂*M*P₂O₇ (M = Fe, Mn, Co) and Li₂FeP₂O₇. The present work extends our previous simulation studies of lithium battery electrodes³⁰⁻³⁹ such as Li*M*PO₄ (M = Mn, Fe, Co, Ni),³¹⁻³⁴ and our investigations of sodium-based cathodes such as NaFeSO₄F³⁶ and Na₂FePO₄F.⁴⁰ Herein, we present a systematic investigation of the defect chemistry, Naion migration paths and volume changes in Na₂*M*P₂O₇ (where M = Fe, Mn) with direct comparison with Li₂FeP₂O₇.

2. Simulation Methods

This investigation uses well established simulation techniques based on the Born model of solids. As these techniques are described in detail elsewhere^{41,42}, only a general outline will be given here. All systems were treated as crystalline solids, with interactions between ions consisting of a long-range coulombic component and a short-range component representing electronelectron repulsion and van der Waals interactions. The shortrange interactions were modelled using the Buckingham potential,⁴¹ and the well-known shell model⁴³ was employed to account for the polarizability effects. As argued previously, interatomic potential methods are assessed primarily by their ability to reproduce observed crystal properties. Indeed, they are found to work well, even for phosphate and silicate cathodes^{31-36,39} where there is undoubtedly a degree of covalency. The Fe-O, Mn-O, P-O and O-O interatomic potentials were taken directly from the study of the related $Li_2FeP_2O_7^{39}$ (to which we compare our defect and migration results), whilst the Na–O potential was taken from the recent study of the $Na_2FePO_4F^{40}$ cathode material. The resulting potential parameters are listed in Table S1 (supporting information).

The lattice relaxation about defects (such as Na vacancies) and migrating ions was calculated by an implementation of the Mott-Littleton scheme incorporated in the GULP code⁴⁴, which partitions the crystal lattice into two separate regions, where ions in the inner region immediately surrounding the defect (~1000 ions) are relaxed explicitly. In contrast, the remainder of the crystal (~3000 ions), where the defect forces are relatively weak, is treated by more approximate quasi-continuum methods. It is worth noting that explicit relaxation of such a large number of lattice ions around defect species is not easily treated by electronic structure methods.

3. Results and Discussion

3.1 Structural Modelling



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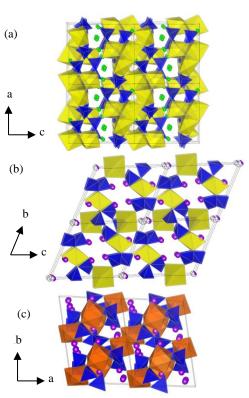


Fig. 1 Crystal structure of Li₂FeP₂O₇ and Na₂*M*P₂O₇ (M = Fe, Mn). a.) Li₂FeP₂O₇ ($P2_1/c$; *c*-axis view), b.) Na₂FeP₂O₇ (P-1; *a*-axis view), c.) Na₂MnP₂O₇ (P1; *c*-axis view); showing Li ions (green) Na ions (purple), FeO₆ octahedra (yellow), MnO₆ octahedra (orange) and P₂O₇ pyrophosphate (blue).

The starting point of the study was to reproduce the experimentally observed crystal structures (Figure 1). The structure exhibited by Na₂FeP₂O₇ is triclinic (*P*-1),²⁵ comprised of corner-sharing FeO₆ octahedra creating Fe₂O₁₁ dimers, which are interconnected by both corner-sharing and edge-sharing with P_2O_7 pyrophosphate groups. The FeO₆ octahedra and PO₄ tetrahedra are connected in a staggered fashion thus creating large tunnels along the [011] direction within which the Na atoms are present. The Na ions occupy six distinct crystallographic sites; three of which are fully occupied (Na1, Na2, Na3), whilst the other three adopt sites that are partially occupied (Na4, Na5, Na6). Due to the partial occupancy it was necessary to use a $3 \times 1 \times 1$ supercell approach considering different cation ordering schemes as used in previous simulations.^{33,36,39} The energetics of the different cation configurations were investigated by performing a series of geometry optimizations in P1 symmetry. We note that the lattice energy differences were found to be very small (< 15 meV), sug-gesting that the ordering of the Na4, Na5 and Na6 sites may not be significant.

The structure exhibited by $Na_2MnP_2O_7^{27}$ consists of distorted MnO_6 octahedral and tetrahedral building blocks which are connected in a staggered manner thus creating tunnels along the [001] direction. The structures have cornersharing isolated Mn_2O_{11} dimers, which are in turn connected by the P_2O_7 units by a mixed edge and corner-sharing fashion. The constituent Na atoms are located in eight inequivalent crystallographic sites. It has been postulated that the complex nature of this triclinic (*P*1) structure may allow for multidimensional Na⁺ diffusion.²⁴ Comparisons between the

calculated and experimental crystal structures are given in Table 1.

Table 1 Calculated and Experimental Structural Parameters of Na₂MP₂O₇ (M = Fe, Mn) and $Li_2FeP_2O_7$.

$\begin{array}{c c c c c c c } & & & & & & & & & & & & & & & & & & &$	β(°)	γ(°)							
$\begin{array}{ccccccc} \exp t.^{25} & 6.433 & 9.458 & 11.143 & 65.16 \\ \Delta \left(\pm \right) & 0.016 & 0.025 & 0.150 & 0.31 \\ & & & & & \\ & & & & & \\ & & & & & \\ \end{tabular} \\ \begin{tabular}{lllllllllllllllllllllllllllllllllll$	Param $a(\text{\AA})$ $b(\text{\AA})$ $c(\text{\AA})$ $a(^{\circ})$ $\beta(^{\circ})$ $\gamma(^{\circ})$ Na ₂ FeP ₂ O ₇								
$\begin{array}{c cccc} \Delta \left(\pm\right) & 0.016 & 0.025 & 0.150 & 0.31 \\ & & & & \\ \hline & & & & \\ rac{2}MnP_2O_7 \\ \hline calc. & 9.917 & 11.169 & 12.489 & 148.77 \\ expt.^{27} & 9.922 & 11.084 & 12.473 & 148.39 \\ \Delta \left(\pm\right) & 0.005 & 0.0854 & 0.0167 & 0.38 \\ \hline & & & \\ Li_2FeP_2O_7^{39} \\ \hline \end{array}$	86.24	73.13							
$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	85.49	73.49							
calc. 9.917 11.169 12.489 148.77 expt. ²⁷ 9.922 11.084 12.473 148.39 Δ (±) 0.005 0.0854 0.0167 0.38 Li ₂ FeP ₂ O ₇ ³⁹	0.75	0.36							
$\begin{array}{cccccccc} expt.^{27} & 9.922 & 11.084 & 12.473 & 148.39 \\ \underline{\Delta} (\pm) & 0.005 & 0.0854 & 0.0167 & 0.38 \\ & & & \\ & & $	Na ₂ MnP ₂ O ₇								
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	121.26	69.00							
Li ₂ FeP ₂ O ₇ ³⁹	121.95	68.42							
	0.68	0.58							
	$Li_2FeP_2O_7^{39}$								
calc. 11.017 9.754 9.805 90.00	101.54	90.00							
expt. 11.200 9.715 9.791 90.00	102.85	90.00							
$\Delta(\pm) 0.183 0.039 0.014 0.00$	1.31	0.00							

For all pyrophosphate systems, the calculated unit cell parameters deviate from experiment by at most 0.18 Å, and in most cases much less; the same is found for the individual bond lengths. The excellent reproduction of the complex low symmetry monoclinic (Li₂FeP₂O₇) and triclinic (Na₂MP₂O₇) crystal structures gives us confidence that the interatomic potential models can be used reliably in subsequent defect and migration calculations.

3.2 Intrinsic Atomic Defects

Insights into the defect properties of cathode materials is crucial to the full understanding of their electrochemical behavior especially the possibility of "blocking" anti-site defects in structures showing 1D ion conduction. A series of isolated point defect (vacancy and interstitial) energies were calculated for both $Li_2FeP_2O_7$ and $Na_2MP_2O_7$ (M = Fe, Mn). By combining these energies, the relative energies of formation of Frenkel and Schottky-type defects were determined. These take the following general forms (using Kröger-Vink notation and where A = Li, Na):

A Frenkel:
$$A_A^X \to V_A' + A_i^{\bullet}$$
 (1)

 $M_M^X \rightarrow V_M^{\prime\prime} + M_i^{\bullet \bullet}$ M Frenkel (2)

O Frenkel
$$O_0^X \to V_0^{\bullet\bullet} + O_i^{\prime\prime}$$
 (3)
Full Schottky $2A_A^X + M_M^X + 2P_B^X + 7O_0^X \to$

Full Schottky

$$2V'_{A} + V''_{M} + 2V''''_{P} + 7V'^{*}_{0} + A_{2}MP_{2}O_{7}$$
(4)

We also examined the A/M "anti-site" pair defect, which involves the exchange of an A^+ ion (Li⁺ radius 0.76 Å, Na⁺ radius 1.02 Å) with an M^{2+} ion (Fe²⁺ radius 0.78 Å and Mn² radius $(0.83 \text{ Å})^{45}$, according to:

M/A Antisite
$$M_M^X + A_A^X \to A'_M + M_A^{\bullet}$$
 (5)

This type of defect is worth investigating since anti-site or cation exchange effects have been observed in other examples of polyanionic systems including $LiMPO_4$ (M = Mn, Fe, Co, Ni)³¹⁻³³ and Li₂MnSiO₄³⁷.

Examination of the resulting defect energies listed in Table 2 reveals three main points. First, the magnitude of the energies

suggests that formation of M Frenkel, O Frenkel and Schottky defects is unfavorable. In particular, O² vacancies and interstitials are highly unfavorable, and unlikely to occur in any significant concentration in the undoped materials, confirming the structural stability of the pyrophosphate framework in accord with thermal stability experiments²⁵

Table 2 Energies of Intrinsic Atomic Defect Processes in Na₂MP₂O₇ (M = Fe, Mn) and $Li_2FeP_2O_7$.

			Energy (eV)	
Disorder Type	eq.	Na ₂ FeP ₂ O ₇	Na ₂ MnP ₂ O ₇	Li ₂ FeP ₂ O ₇ ³⁹
A Frenkel	(1)	1.14	1.34	1.21
M Frenkel	(2)	3.52	2.93	3.39
O Frenkel	(3)	3.53	3.92	3.99
Full Schottky	(4)	33.03	38.62	32.42
A/M anti-site	(5)	0.89	0.80	0.22

Second, the most favorable type of intrinsic defect for the $Na_2MP_2O_7$ material is found to be the Na/M anti-site pair as was predicted for the Li/Fe anti-site pair in the analogous study of the Li-analogue $(\text{Li}_2\text{FeP}_2\text{O}_7)^{39}$. The formation energy for the Na/M antisite within the $Na_2MP_2O_7$ materials is of greater magnitude, suggesting lower but still significant concentrations of antisite defects within Na₂MP₂O₇. The concentration of antisite disorder would be temperature dependent and hence sensitive to experimental synthesis conditions. Since Na⁺ (radius 1.02 Å) is significantly larger than Li⁺ (radius 0.76 Å), Fe^{2+} (radius 0.78 Å) and Mn^{2+} (radius 0.83 Å)⁴⁵, it is interesting to analyse the local structure of the anti-site defects revealed by the calculations.

Lastly, the second lowest energies for the Na₂MP₂O₇ cathode materials are found for the Na Frenkel defect (Table 2). This result is in accordance with the value calculated for the Li Frenkel defect within Li₂FeP₂O₇³⁹. This suggests that a very minor population of such Li/Na vacancy and interstitial defects could be present at high temperatures. In the context of ion diffusion, the antisite defects bare more significance in the case of olivine materials as their presence blocks the only available 1D channel for alkali ion migration.^{31,40}

3.3 Na Ion Migration

Examination of the Na⁺ mobility and pathways in Na₂MP₂O₇ is of vital importance when considering their respective charge/discharge rates and any differences with Li⁺ mobility. However, obtaining such insights for complex polyhedral structures is far from straightforward. Simulation methods can greatly enhance our understanding of the migration pathways and diffusion dimensionality at the atomic level.

Na-diffusion pathways were considered between all neighbouring Na positions within the $Na_2MP_2O_7$ (M = Fe, Mn) materials along each of the three principal axes via conventional vacancy hopping, as used in the study of Li-diffusion in Li₂FeP₂O₇³⁹. Energy profiles for Na migration along each of the pathways considered can be mapped out, and the migration energies derived; such an approach has been used in numerous previous studies on oxide ion and cation migration in complex oxides.31,32,46 The resulting lowest migration energies for Na diffusion along the three principal axes of the Na₂MP₂O₇ materials are reported in Table 3 with the corresponding lowest migration energies for Li diffusion within Li₂FeP₂O₇ reported for comparison³⁹.

 $\begin{array}{l} \textbf{Table 3} Calculated Migration Energies for Most Favourable Paths of Alkali- ion Diffusion: Na-ion Migration in Na_2FeP_2O_7 and Na_2MnP_2O_7 and Li-ion Migration in Li_2FeP_2O_7. \end{array}$

Net Diffusion	Migration Energies (eV)				
Direction	Na ₂ FeP ₂ O ₇	$Na_2MnP_2O_7$	Li ₂ FeP ₂ O ₇ ³⁹		
<i>a</i> -axis	0.33	0.58	0.73		
<i>b</i> -axis	0.42	0.58	0.40		
c-axis	0.49	0.58	0.40		

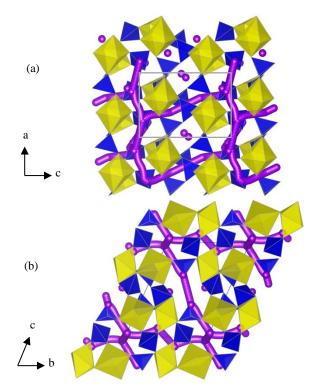


Fig. 2 Calculated paths for long-range Na⁺ migration within Na₂FeP₂O₇ along the *a*-axis, *b*-axis and *c*-axis directions with activation energies ≤ 0.49 eV; a) view of the *ac*-plane; b) view of the *bc*-plane.

From the results presented in Table 3, it would appear that that both Na₂MP₂O₇ structures support quasi-three dimensional (3D) Na⁺ diffusion with activation energies of 0.49 eV and 0.58 eV for Na₂FeP₂O₇, and Na₂MnP₂O₇ respectively. The final calculated paths for long-range Na⁺ diffusion are shown in Figures 2 and 3. We note that in recent theoretical studies of a different Na₂FeP₂O₇ polymorph (triclinic, P1) Na⁺ diffusion was found to be 2D with migration barriers of ~0.54 eV. The Li₂FeP₂O₇ compound shows 2D Li⁺ diffusion in the *bc*-plane with activation energies of 0.40 eV.³⁹ Therefore in all cases the pyrophosphate framework appears to show high alkali-ion (Na⁺/Li⁺) mobility. Although there are no Li⁺/Na⁺ conductivity data for direct comparison, our calculated values for alkali-ion migration are consistent with experimental activation energies for Li/Na ion conductivity in other framework-structured phosphate materials.⁴⁷⁻⁴⁹ The 2D and 3D transport behaviour in the pyrophosphates contrasts with that in olivine LiFePO₄ and NaFePO₄ which only allow Li⁺/Na⁺ migration along 1D channels parallel to the *b*-axis^{31,40}. In addition, ion blocking by anti-site defects is much less likely to make a significant difference to the alkali (Na/Li) ion migration in these pyrophosphate materials. Electrochemical studies indicate that Na₂FeP₂O₇ has excellent rate kinetics, superior to that of

 $Li_2FeP_2O_7^{39}$; this may be related to the high dimensionality (3D) and low migration energy for Na-ion diffusion in Na₂FeP₂O₇.

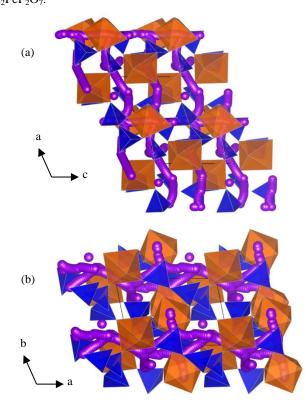


Fig. 3 Calculated paths for long-range Na⁺ migration within Na₂MnP₂O₇ along the *a*-axis, *b*-axis and *c*-axis directions with activation energies ≤ 0.58 eV; a) view of the *ac*-plane; b) view of the *ab*-plane.

Our simulations also reveal curved paths between adjacent Na/Li sites within each of the pyrophosphate materials studied (Figures 2 and 3), which produces "wavelike" trajectories for long-range migration. It is worth noting that analogous, curved Li^+ migration paths were first predicted from atomistic simulation³¹ of LiFePO₄, which were subsequently confirmed by neutron diffraction maximum entropy method (MEM) analysis.⁵⁰

There has been recent debate about the volume difference between the reduced and oxidized phases as a significant factor in determining electrochemical performance of cathode materials.^{40,51,52} For two-phase processes, a phase boundary between oxidized and reduced phases is formed during charge/discharge. Electrochemical performance could be affected by the amount of strain generated in this phase boundary, as well as by the activation energy barrier for Li-ion or Na-ion transport.

The difference in the unit cell volume (ΔV) of the oxidized and reduced phases is only ~3.26 % for Na₂FeP₂O₇, but > 15 % for NaFePO₄ and NaFeSO₄F. We note that while the majority of the compounds undergo volume contraction on Li/Na extraction, Li₂FeP₂O₇ shows a small volume expansion, although de(lithiation) has been found to be via a solid-solution mechanism in this pyrophosphate⁵². Although the interplay of all factors is still under investigation, materials with a large volume difference between the end member phases could lead to poor rate capability as discussed by Tripathi et al⁴⁰. In contrast, promising electrochemical properties can be anticipated for Na-based cathode materials with low volume change on cycling (e.g. <7%) and low ion migration activation barriers (e.g. <0.5 eV) as in the case of $Na_2FeP_2O_7$ and $Na_2FePO_4F.$

4. Conclusions

We have investigated Fe- and Mn-based pyrophosphate materials which offer promising high rate cathodes that are potentially low cost and thermally stable for sodium-ion batteries. This systematic survey of $Na_2MP_2O_7$ (M = Fe, Mn) with comparison to $Li_2FeP_2O_7$ used atomistic simulation techniques to provide insights into their defect and ion migration properties. The main results can be summarized as follows:

(1) The atomistic simulations show good reproduction of the observed complex structures of $Na_2FeP_2O_7$ and $Na_2MnP_2O_7$. The defect calculations indicate the stability of the pyro-phosphate framework towards oxygen evolution, which is important for operational safety. The most favourable intrinsic defect type is the Na/M and Li/Fe antisite, with the relative energies suggesting greater Li/Fe disorder in the $Li_2FeP_2O_7$ material as observed.

(2) Both Na₂FeP₂O₇ and Na₂MnP₂O₇ are predicted to exhibit curved diffusion pathways parallel to the *a*-, *b*- and *c*axes with low migration energies (~0.50 eV). Hence, the pyrophosphate framework appears to support 3D Na⁺ diffusion in Na₂MP₂O₇, (and 2D Li⁺ diffusion in Li₂FeP₂O₇), which is consistent with the high rate kinetics observed for Na₂FeP₂O₇.

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[†] Electronic Supplementary Information (ESI) available: [details of any supplementary information available should be included here]. See DOI: 10.1039/b000000x/

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