A phenomenological model of the solvent-assisted lipid bilayer formation method

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The recently introduced solvent-assisted lipid bilayer (SALB) formation method allows one to efficiently fabricate planar, lipid bilayers on solid supports and can be used for various applications. It involves the introduction of an aqueous buffer into a mixture of lipid and alcohol, which is incubated on a solid support. The associated phase changes in the ternary bulk system are accompanied by the formation of a lipid bilayer at the solid–liquid interface. While the phase behavior of the ternary bulk system is well understood, the mechanism of bilayer assembly at the solid–liquid interface remains to be elucidated, including whether the adsorption process is limited by diffusion of the lipid in the bulk or by lipid binding kinetics onto the surface. Such factors strongly influence the success of bilayer formation as they pertain to operating conditions, such as lipid concentration, solvent exchange rate and chamber dimensions, and are hence of critical importance for SALB fabrication strategies. Herein, we extend an earlier proposed phenomenological kinetic model of the SALB formation process, based on a volume-averaged treatment of the solvent mixing process. By comparing the model to quartz crystal microbalance with dissipation monitoring (QCM-D) experimental data, we conclude that SALB formation is limited by diffusion of suspended lipid aggregates, with a hydrodynamic radius, that is consistent with aggregate size measurements in the literature. This agreement validates the proposed model to serve as the basis for optimizing conditions for SALB formation.

Introduction

Supported lipid bilayers (SLBs) are membrane-mimetic platforms, which preserve the fundamental features of highly complex biomembranes, such as bilayer thickness, lateral lipid mobility and the ability to host membrane associated biomolecules. SLBs enable membrane-related processes to be studied by highly sensitive, surface-based analytical tools. For instance, total internal reflection microscopy, atomic force microscopy, impedance spectroscopy and quartz crystal microbalance with dissipation (QCM-D) have successfully been applied to SLBs for biosensor development, drug discovery and protein assembly.

Several approaches have been developed for fabrication of SLBs, including air bubble collapse and dip-pen nanolithography for submicron-sized membrane patches and spin-coating for membrane stacks. For a continuous coverage of a substrate with a single, planar bilayer, Langmuir–Blodgett and vesicle fusion (VF) can be used. In particular, the VF method, which involves adsorption, spontaneous rupture and spreading of small unilamellar vesicles on a solid support, has become a standard method for bilayer formation.

Since the VF method requires a relatively large adhesion force between the vesicles and the substrate, such that the vesicles rupture and spread spontaneously upon adsorption, the VF method is limited to a sub-set of surfaces, mainly silica-based materials, such as glass and mica, while the other important surfaces, such as Au, TiO$_2$ and Al$_2$O$_3$ or nanostructured ones are intractable to vesicle fusion, as well as certain biologically relevant membrane compositions, with a high fraction of cholesterol for instance. In some cases, it is possible to overcome these limitations by altering the environmental factors, such as ionic strength, pH, temperature, osmotic imbalance and the addition of divalent cations. Alternatively, other self-assembly routes which bypass vesicle rupture can be used.

The solvent-assisted lipid bilayer (SALB) formation method is an alternative technique to form supported lipid bilayers, which does not require preparation of vesicles. The method involves introduction of an aqueous buffer into a mixture of lipids and water-miscible alcohol (e.g. isopropanol). This ternary system flows through a fluidic chamber contacting a solid support. This principle has also been used to form liposomes. It is known that, with increasing water content, this ternary system undergoes phase transitions in the bulk, where the lipid structures change from inverted micelles to individual molecules, then to micelles,
and subsequently to vesicles.\textsuperscript{36} Simultaneously, as the water content is increased, lipids form an adsorbed phase at the solid–liquid interface. For small water fractions, the adsorbed lipid phase, which is in the form of small mono-layered patches, is in dynamic equilibrium with the dissolved lipid phase in the bulk,\textsuperscript{38} while at sufficiently large water fractions, the adsorbed lipid phase constitutes a complete supported lipid bilayer. Hohner \textit{et al.} correlated the equilibrium adsorbed bilayer mass at various water fractions to the lipid aggregate size distribution in the bulk, and concluded that, with increasing water fraction, the supported bilayer forms just before the micelle to vesicle phase transition occurs in the bulk.\textsuperscript{36}

The SALB formation method has been applied to surfaces which are intractable to the VP method, such as Al\textsubscript{2}O\textsubscript{3}, Cr, SnO\textsubscript{2}, and Au.\textsuperscript{35,39,40} The method also extends the range of possible compositions of artificial membranes, allowing for instance the formation of bilayers with a high cholesterol content.\textsuperscript{41,42}

Although the formation of bilayers \textit{via} the SALB method has been demonstrated to be correlated with the micelle to vesicle phase transition in the bulk, the exact formation mechanism is not known. For instance, it is unclear, whether the formation rate is determined by the binding kinetics onto the surface or by the lipid diffusivity in the bulk. These aspects determine the extent of bilayer formation as a function of the operating conditions and are of crucial importance for optimizing the SALB formation process.

In this work, we address the aforementioned question, by extending an earlier proposed, phenomenological kinetic model for SALB formation, based on a volume averaged treatment of the solvent mixing.\textsuperscript{35} The model in ref. 35 assumes that bilayers are formed by adsorbing micelles and it incorporates micelle attachment to the support \textit{via} a rate constant \( k_a \) and predicts that SALB formation is complete for a sufficiently large lipid concentration in the bulk \( c_0 \) and for a sufficiently small solvent exchange rate \( \gamma [s^{-1}] \) and it is incomplete for small \( c_0 \) or large \( \gamma \). Here we refine this model with an explicit expression for \( k_a \) based on the diffusion flux in laminar flow, which depends on chamber geometry, flow speed and the hydrodynamic radius of the lipid (aggregates). We fit the extended model to quartz crystal microbalance with dissipation monitoring (QCM-D) experimental data of the mass of the adsorbed lipid phase. Using this approach, we deduce the details of the adsorption kinetics leading to SALB formation.

**SALB formation model**

The dynamics of SALB formation depends on the mixing characteristics of the aqueous buffer with the lipid–alcohol mixture, which in turn depend on the geometrical details of the fluidic chamber.\textsuperscript{43} In the present experiments however, as will be shown below, the mixing may vary considerably upon repeating the experiment under identical conditions. Therefore, we do not attempt to model the detailed, space-dependent flow and mixing in the fluidic chamber, but restrict the modeling to volume-averaged quantities, and restrict the comparison between model and experiment to the equilibrated bilayer mass after full solvent exchange, for which, as will be shown below, experimental variations are modest.

We consider a mixture of lipids and water-miscible alcohol that is contained in a cylindrical chamber with diameter \( L \) and height \( H \). The geometry is sketched in Fig. 1. The lipid concentration is \( c_0 \). At \( t = 0 \) aqueous buffer is fed into the chamber with volume rate \( Q \), where it mixes with the lipid–alcohol mixture. The mixture is assumed to be homogeneous, except for a thin boundary layer at the bottom surface, with a thickness: \( \delta \ll H \).

The bilayer formation model is an extension of a model presented earlier,\textsuperscript{35} and it is based on the assumption that lipids adsorb onto the surface in the form of micelles. Micelles form in the bulk when the water fraction \( \Phi \) exceeds a certain critical value \( \Phi_c \).\textsuperscript{35,36} Accordingly, the bilayer areal mass density \( \rho \) increases due to a deposition mass flux \( J \), which is zero, when \( \Phi < \Phi_c \), and it is zero also when the bilayer mass density reaches its fully developed value \( \rho_{LB} \):\textsuperscript{44}

\[
\frac{d\rho}{dt} = \begin{cases} 
0 & \text{if } \Phi \leq \Phi_c \\
J & \text{if } \Phi > \Phi_c \\
0 & \text{if } \rho = \rho_{LB}
\end{cases}.
\]

As a result of lipid adsorption onto the surface, the concentration of the dissolved lipids is depleted in a region close to the surface. The thickness of this concentration boundary layer is denoted as \( \delta \). In the present model, we assume and verify below, that the SALB formation is diffusion limited, \textit{i.e.} \( D/k\delta \ll 1 \), where \( D \) is the diffusion coefficient of the dissolved lipid and \( k \) is the lipid adsorption rate constant. Under this condition the mass flux reads:\textsuperscript{44}

\[
J = \frac{c_b D}{\delta}.
\]

where \( c_b \) is the time dependent, volume averaged lipid concentration in the chamber. It is noted that, as a consequence of \( D/k\delta \ll 1 \), the deposition mass flux \( J \) in eqn (2) is independent of the lipid adsorption rate constant \( k \). Under laminar flow conditions, \( \delta \) is the following function of the downstream position \( x \):\textsuperscript{44,45}

\[
\delta = \left( \frac{DxH}{U} \right)^{1/3},
\]

where \( U \) is the fluid velocity. In eqn (3) we have omitted a numerical factor of 0.97.\textsuperscript{44} Furthermore, in the present work we employ eqn (3) as an effective (surface averaged) model, where we
estimate the effective fluid velocity by \( U = Q/(LH) \), and the effective downstream position by \( x = L \). It is noted that using \( x = L/2 \) instead of \( x = L \) would result in a correction factor of \((L/2)^{3/2} \approx 0.8\), which is irrelevant in the present level of approximation. For the same reason, we omit the factor \((4\pi)^{3/2} \approx 1.1\) in the definition for the cylinder diameter \( L = (V/H)^{2/3} \) in terms of the volume \( V \) and the height \( H \).

The diffusivity \( D \) depends on the form in which the lipids diffuse towards the surface, where single lipid molecules diffuse faster than large aggregates, such as micelles or vesicles. In the model we treat the lipid size \( R \) as an unknown parameter, which will be determined by matching the model to the experimental data, as seen below. The relation between the diffusivity and the particle size is given by the Stokes–Einstein relation:

\[
D = \frac{k_B T}{6\pi \eta R}
\]  

(4)

where \( \eta \) is the solvent viscosity and \( k_B T \) is the Boltzmann energy.

Assuming perfectly mixed conditions in the QCM-D chamber (except for the boundary layer), the bulk lipid concentration \( c_b \) and the water volume fraction \( \Phi \) in the chamber evolve as follows:46

\[
c_b = c_0 \exp(-tQ/V),
\]

(5)

and:

\[
\Phi = 1 - \exp(-tQ/V).
\]

(6)

As mentioned above, the lipid flux onto the surface is nonzero only when the water volume fraction \( \Phi \) exceeds the critical value \( \Phi_c \), i.e. when \( t > t_c \), where the critical time \( t_c \) is found by inserting \( \Phi = \Phi_c \) into eqn (6):

\[
\Phi_c = 1 - \exp(-t_cQ/V).
\]

(7)

By combining eqn (1), (2) and (5), we obtain the following differential equation for the bilayer areal mass density \( \rho \) as a function of time:

\[
\frac{d\rho}{dt} = \begin{cases} 
0 & \text{if } t < t_c \\
\frac{Dc_0}{\delta} \exp(-tQ/V) & \text{if } t_c < t < t_c \\
0 & \text{if } t > t_c
\end{cases}
\]

(8)

Here \( t_c \) is the moment where the bilayer reaches its fully developed mass, i.e. \( \rho(t_c) = \rho_{LB} \). The solution to eqn (8) reads:

\[
\rho = \begin{cases} 
0 & \text{if } t < t_c \\
VDc_0(1 - \Phi_c - \exp(-tQ/V)) & \text{if } t_c < t < t_c \\
\rho_{LB} & \text{if } t > t_c
\end{cases}
\]

(9)

By inserting \( \rho = \rho_{LB} \) into eqn (9), we find that a complete bilayer is formed when:

\[
1 - \Phi_c = \frac{\rho_{LB}Q}{VDc_0} \exp(-t_cQ/V),
\]

(10)

and by inserting \( t \to \infty \) into eqn (9), we find for the final adsorbed lipid mass density \( \rho_{LB} \):

\[
\rho_{LB} = \begin{cases} 
c_0 & \text{if } c_0 < 1 \\
1 & \text{if } c_0 > 1
\end{cases}
\]

(11)

where \( c_{min} \) is the minimum lipid concentration, required to form a complete bilayer, which is given by:

\[
c_{min} = \frac{\rho\Phi_{LB}Q}{(1 - \Phi_c)DV}.
\]

(12)

Combining eqn (12) with the expression for the boundary layer thickness \( \delta \) [eqn (3)], we find:

\[
c_{min} = \frac{\rho_{LB}Q}{(1 - \Phi_c)V} \left(\frac{LHQ}{D}\right)^{2/3}.
\]

(13)

Instead of a relation between bilayer mass and lipid concentration, eqn (11) and (13) can also be recast into a relation between bilayer mass and flow rate:

\[
\rho_{LB} = \begin{cases} 
\left(\frac{Q_{max}}{Q}\right)^{2/3} & \text{if } Q > Q_{max} \\
1 & \text{if } Q < Q_{max}
\end{cases}
\]

(14)

where the maximum flow rate to form a complete bilayer is given by:

\[
Q_{max} = \left(\frac{(1 - \Phi_c)c_0V}{\rho_{LB}}\right)^{3/2} D^{1/2} / LH.
\]

(15)

Materials and methods

Lipid preparation

Zwitterionic 1,2-dioleoyl-sn-glycero-3-phosphocholine (DOPC) lipid was purchased from Avanti Polar Lipids (Alabaster, AL). A stock solution was prepared by dissolving the lipid powder in isopropanol (IPA) at a concentration of 5 \( \mu \)g mm\(^{-2}\). Prior to the experiments, the stock solution was further diluted with IPA to the desired lipid concentration. In the SALB formation experiment, the DOPC–IPA mixture was exchanged with an aqueous buffer solution with 150 mM NaCl, 10 mM Tris and a pH of 7.5.

Quartz crystal microbalance-dissipation (QCM-D)

A Q-Sense E4 (Q-Sense AB, Gothenburg, Sweden) setup was used to measure the adsorbed bilayer mass, employing an AT-cut, 5 MHz, piezoelectric quartz crystal, coated with an atomically flat silicon dioxide film, with an active area of 97 mm\(^2\), mounted in a cylindrical fluidic chamber, with height \( H = 0.6 \) mm, diameter 11.1 mm and volume \( V = 58 \) mm\(^3\). Prior to use, the substrate was cleaned by immersion in 1% sodium dodecyl sulfate (SDS), rinsed with Milli-Q water (Millipore), dried with a stream of nitrogen gas and treated with oxygen plasma at 180 W for 30 s (March Plasmod Plasma Etcher, March Instruments, California). The frequency shifts \( \Delta f \) and dissipation shifts \( \Delta D \) were recorded at the 3rd, 5th, 7th, 9th
and 11th overtones under flow-through conditions, using a peristaltic pump (Ismatec Reglo Digital M2-2/12). The temperature of the flow cell was fixed at 24.0 ± 0.5 °C. Experiments were conducted for various lipid concentrations $c_0$ between 0.01 and 0.5 µg mm$^{-3}$ and for various flow rates $Q$ between 0.83 and 10 mm$^3$ s$^{-1}$, respectively. Further details of QCM-D principles and operation can be found elsewhere.$^{47}$

**Results**

We have used QCM-D to measure the extent of SALB formation at various lipid concentrations ($c_0 = 0.01 − 0.5\ \mu g\ mm^{-3}$) and flow rates ($Q = 0.83 − 10\ mm^3\ s^{-1}$).$^{35,38}$ Fig. 2A shows, for $c_0 = 0.5\ \mu g\ mm^{-3}$ and $Q = 0.83\ mm^3\ s^{-1}$, the recorded negative frequency shift $-\Delta f_n/n$, which itself is a positive quantity, for the third overtone, i.e. $n = 3$, as a function of time. At $t = 0$, pure buffer is injected into the QCM-D flow chamber, which defines the zero (baseline) frequency and dissipation shifts, i.e. $\Delta f_n = 0$ and $\Delta D_n = 0$. It is noted that $t = 0$ in the experiments (buffer injection) does not correspond to $t = 0$ in the model (organic to aqueous solvent exchange). At $t = 6$ min pure IPA is injected, inducing a gradual exchange in the chamber from buffer to IPA. Due to the non-monotonic viscosity of the buffer−IPA mixture$^{48}$ (Fig. 2B), $\Delta f_n$ first increases and then it decreases during the solvent exchange. After full exchange, at $t = 20$ min and $-\Delta f_3/3 = 134$ Hz, the lipid−IPA solution ($c_0 = 0.5\ \mu g\ mm^{-3}$) is injected, resulting in $-\Delta f_3/3$ increasing slightly, from 134 Hz to 139 Hz. This increase does not correspond to bilayer formation but to the formation of lipid monolayer patches on the support, which are in dynamic equilibrium with the bulk lipid.$^{49}$ After equilibration ($t = 36$ min), the flow is switched back to buffer solution, where again due to the non-monotonic viscosity (Fig. 2B), the $-\Delta f_3/3$ first increases and then it decreases. The signal does not return back to zero (baseline), but instead reaches: $-\Delta f_3/3 = 26$ Hz, which corresponds to an adsorbed mass of $\rho_{AD} = -C\Delta f_3/3 = 4.4\ ng\ mm^{-2}$, which is in the correct range for lipid bilayers.$^{49}$ Here $C = 0.17\ ng\ s\ mm^{-2}$ is the Sauerbrey constant of the sensor.$^{30}$

Fig. 2C shows the final scaled frequency shift $-\Delta f_n/f_0$ and dissipation shift $\Delta D_n/\pi$ as functions of the overtone number $n$, where $f_n = n f_0$ is the overtone resonance frequency and $f_0 = 5\ MHz$ is the QCM-D fundamental frequency. These quantities correspond to the forces on the quartz (scaled with the quartz inertia) due to the adsorption of the lipids, where $-\Delta f_n/f_0$ is the inertial force, which is in phase with the quartz acceleration and $\Delta D_n/\pi$ is the friction force, which is in phase with the quartz velocity.$^{31}$ The data show that $-\Delta f_n/f_0$ is overtone independent and that $\Delta D_n/\pi \ll -\Delta f_n/f_0$. Both these observations indicate that the lipid adsorbs into a homogeneous film, which oscillates rigidly and in phase with the oscillating quartz, which is consistent with the formation of a lipid bilayer.

Upon repetition of the experiment under identical conditions, the time evolution of $-\Delta f_3/3$ during the solvent exchange is...
observed to vary from experiment to experiment (Fig. 2D). These variations are due to variations in the mixing process in the QCM-D chamber. Variations in the final bilayer mass however are modest (±10%), as can be seen in Table 1. Therefore, we do not analyze the transient mixing details, but focus the analysis on the final bilayer mass.

Fig. 3A and Table 1 show the final bilayer mass as a function of the lipid concentration \( c_0 \), at a fixed flow rate of \( Q = 0.83 \text{ mm}^3 \text{ s}^{-1} \). Fitting eqn (11) to the data in Fig. 3A gives the minimum lipid concentration required to form a full bilayer of \( c_{\text{min}} = 0.13 \mu \text{g mm}^{-3} \). Inserting this value into eqn (13) provides the diffusivity of the lipid that is transported towards the bilayer. Eqn (13) also contains the critical water fraction \( \Phi_c \). Since the value for \( \Phi_c \) is not known for the water–IPA–DOPC system, we assume \( \Phi_c = \frac{1}{2} \), which is consistent with the measured \( \Phi_c \) in the range (0.4–0.8), using 1,2-dimyristoyl-sn-glycero-3-phosphocholin (DMPC) and 1,2-dimyristoyl-sn-glycero-3-trimethylammoniumpropane (DMTAP) dissolved in water and IPA.2626 In the Discussion and conclusion section, we will discuss the sensitivity of the outcome of the model to the exact value of \( \Phi_c \). Inserting \( c_{\text{min}} = 0.13 \mu \text{g mm}^{-3} \) together with \( \Phi_c = \frac{1}{2} \) and \( Q = 0.83 \text{ mm}^3 \text{ s}^{-1} \) into eqn (13) gives a diffusivity of \( D = 139 \mu \text{m}^2 \text{ s}^{-1} \), and inserting this diffusivity value into eqn (4) gives a radius of \( R = 0.6 \text{ nm} \), where we have used a solvent viscosity of \( \eta = 2.5 \text{ g m}^{-1} \text{ s}^{-1} \), which corresponds to a 50% water fraction (Fig. 2B), which is consistent with the assumption \( \Phi_c = \frac{1}{2} \) above.

**Table 1** Mean and standard deviation (over repeated measurements) of QCM-D frequency shift after full solvent exchange, at various lipid concentrations \( c_0 \) and flow rates \( Q \). The experiment was repeated \( N \) times.

<table>
<thead>
<tr>
<th>( c_0 ) [mg mL(^{-1})]</th>
<th>( Q ) [mm(^3) s(^{-1})]</th>
<th>(-\Delta f/3) [Hz] mean</th>
<th>(-\Delta f/3) [Hz] standard deviation</th>
<th>( N )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.01</td>
<td>0.83</td>
<td>10</td>
<td>1.6</td>
<td>4</td>
</tr>
<tr>
<td>0.05</td>
<td>0.83</td>
<td>7.7</td>
<td>3.9</td>
<td>4</td>
</tr>
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<td>0.1</td>
<td>0.83</td>
<td>21.4</td>
<td>1.6</td>
<td>4</td>
</tr>
<tr>
<td>0.25</td>
<td>0.83</td>
<td>26.3</td>
<td>1.8</td>
<td>4</td>
</tr>
<tr>
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<td>0.83</td>
<td>25.3</td>
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<td>4</td>
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<td>0.83</td>
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<td>1</td>
</tr>
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<td>2</td>
</tr>
<tr>
<td>0.1</td>
<td>10</td>
<td>4.7</td>
<td>—</td>
<td>1</td>
</tr>
</tbody>
</table>

Fig. 3B and Table 1 show the final bilayer mass as a function of the solvent exchange rate \( Q \), at a fixed lipid concentration \( c_0 = 0.1 \mu \text{g mm}^{-3} \). Increasing \( Q \) reduces the contact time between the lipid solution and the target surface, inhibiting bilayer formation. Fitting eqn (14) to the data in Fig. 3B gives a maximum flow rate to ensure a full bilayer formation of \( Q_{\text{max}} = 0.8 \text{ mm}^3 \text{ s}^{-1} \). Inserting this value together with \( c_0 = 0.1 \mu \text{g mm}^{-3} \) into eqn (15) gives a diffusivity of \( D = 237 \mu \text{m}^2 \text{ s}^{-1} \), and inserting this diffusivity value into eqn (4) gives a radius of \( R = 0.2 \text{ nm} \). Furthermore, as seen in Fig. 3B, the model (eqn (4) law) correctly predicts that upon increasing \( Q \) to 10-fold, i.e. from 1 to 10 mm\(^3\) s\(^{-1}\), the bilayer mass reduces five-fold, i.e. from 25 Hz to 5 Hz.

**Discussion and conclusion**

We have extended an earlier proposed phenomenological model for the solvent-assisted lipid bilayer (SALB) formation, by assuming that the lipid adsorption process is limited by diffusion. In the model the diffusivity acts as a free parameter, which we have obtained by fitting the model to experimentally measured bilayer mass, either as a function of the lipid concentration or as a function of the flow rate. The diffusivities from both procedures are in the same range, i.e. \( D = 139 \mu \text{m}^2 \text{ s}^{-1} \) and \( 237 \mu \text{m}^2 \text{ s}^{-1} \), which supports that the model correctly predicts the flow rate and concentration dependencies of the SALB formation process and that it can be used as a design tool for optimizing the SALB formation in different experimental configurations.

Furthermore, we have used the Stokes–Einstein relation to determine the hydrodynamic radius of the adsorbing lipid: \( R = 0.4 \pm 0.2 \text{ nm} \). It is noted that for objects with a radius smaller than ~0.5 nm, the diffusivity can be somewhat larger, than the value predicted by the Stokes–Einstein model.26 Applying these corrections to the present analysis may give a somewhat larger value for \( R \).

Let us now verify the assumption that the adsorption process is limited by diffusion, i.e. that \( k \delta / D \gg 1 \). To this end, we consider the consequences of assuming that \( k \delta / D = 1 \), by imagining that we decrease \( k \) from a value that is very large...
to a value that is very small compared to $D_i\delta$, while keeping all the other parameters constant. Reducing $k$ at a constant $D$ reduces the adsorption rate and therefore results in a lower bilayer mass. In order to match the experimentally measured bilayer mass would therefore require a larger diffusivity, which corresponds to a smaller particle size, according to the Stokes–Einstein relation [eqn (4)]. Above, we estimated that matching the experimental data with a diffusion-limited model ($k_0/D \gg 1$) requires a particle of nano-meter size. Therefore matching the experimental data, assuming $k_0/D \ll 1$, would require the adsorbing particles to be (order(s) of magnitude) smaller than a nano-meter. This hypothetical violation of physical constraints suggests that the process is indeed limited by diffusion, or that the diffusion velocity $D_i\delta$ is at most of the same order of magnitude as the adsorption rate constant $k$.

Another crucial assumption in our model is the value for the critical water fraction, which is unknown in the present system, and which was arbitrarily chosen as $\Phi_c = \frac{1}{2}$. To see the influence of this parameter on the results, we re-calculate the diffusivities and the corresponding hydrodynamic radii $R$, by inserting $c_{\min} = 0.13 \mu g \text{ mm}^{-2}$ and $Q_{\max} = 0.8 \text{ mm}^3 \text{ s}^{-1}$ into eqn (13) and (15), respectively, for the limiting case of $\Phi_c \rightarrow 1$, which results in $R = 1.1 \pm 0.6$ nm.

Considering the above mentioned factors, we conclude that in the present experiments, lipids diffuse towards the surface in a form that has a hydrodynamic radius of $R \sim 1$ nm. Given the adsorbing molecules, the bulk system is in quasi-equilibrium, and can therefore be compared to experiments under equilibrium conditions. The quasi-equilibrium bulk phase condition follows from the time scale for micelle formation $t_c \sim 10^{-5}$ s, estimated from Smoluchowski theory: $t_c \sim (4\pi D c c_0)^{-1}$ and measured experimentally, which is orders of magnitude smaller than that of bilayer formation $t_{LB} \sim \delta_0 D_{LB_D}(Dc_0) \sim 10^2$ s. Here $R \sim 10^{-9}$ m is the micelle radius, $c = c_0 R_\text{m} \sim 10^{-3} \text{ m}^{-3}$ is the number density of individual lipid molecules, $M_\text{r} \sim 10^{-2} \text{ kg}$ is the mass of one lipid molecule, $D \sim 10^{-10} \text{ m}^2 \text{ s}^{-1}$ is the lipid diffusivity and $\delta \sim 10^{-6}$ m is the boundary layer thickness.

In summary, our results are consistent with the literature findings and the proposed phenomenological model may serve as a design tool to find the optimal operating conditions for SALB formation, such as lipid concentration, flow rate and chamber dimensions.

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References