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Determining the 3D orientation of optically trapped upconverting nanorods by in situ single-particle polarized spectroscopy†

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An approach to unequivocally determine the three-dimensional orientation of optically manipulated NaYF₄:Er³⁺,Yb³⁺ upconverting nanorods (UCNRs) is demonstrated. Long-term immobilization of individual UCNRs inside single and multiple resonant optical traps allow for stable single UCNR spectroscopy studies. Based on the strong polarization dependent upconverted luminescence of UCNRs it is possible to unequivocally determine, in real time, their three-dimensional orientation when optically trapped. In single-beam traps, polarized single particle spectroscopy has concluded that UCNRs orientate parallel to the propagation axis of the trapping beam. On the other hand, when multiple-beam optical tweezers are used, single particle polarization spectroscopy demonstrated how full spatial control over UCNR orientation can be achieved by changing the trap-to-trap distance as well as the relative orientation between optical traps. All these results show the possibility of real time three-dimensional manipulation and tracking of anisotropic nanoparticles with wide potential application in modern nanobiophotonics.

Introduction

Rare earth doped Upconverting Nanoparticles (hereafter UCNPs) have emerged during the last few years as useful fundamental building blocks in modern photonics. UCNPs are being extensively used in a large variety of research fields including solar energy, nanomedicine and bioimaging, among many others. ¹-⁸ UCNPs show the unique capability of producing visible (VIS) luminescence under near-infrared (NIR) optical excitation by a multiphoton excitation process known as upconversion.⁶,⁹ When compared to other nanomaterials also capable of NIR-to-VIS optical conversion (such as metallic nanoparticles and semiconductor nanocrystals), UCNPs present several remarkable advantages including long-term photochemical stability, narrow emission lines, long luminescence lifetimes, and size-independent spectral shape of their luminescence bands.¹⁰-¹⁴ Recent studies have also pointed out that, since in UCNPs the multiphoton excitation is assisted by real electronic states, large NIR-to-VIS efficiencies could be achieved upon cw excitation without requiring the use of expensive, ultrafast, high power laser sources (as is the case when using gold nanoparticles or semiconductor nanocrystals).⁹ This fact boosted the use of UCNPs for optical conversion in solar cells as well as in the development of cost-effective bioimaging equipment.¹⁵-¹⁷ In the particular field of fluorescence bioimaging, UCNPs are nowadays considered as one of the most promising in vitro luminescence probes because of the low autofluorescence generated by continuous wave NIR optical excitation.¹⁸ Moreover, recent studies have demonstrated that some UCNPs are not only capable of in vitro imaging but, in addition, they can also be used as intracellular thermal and chemical sensing units.¹⁹-²² In addition, intracellular studies based on single UCNP are nowadays a real possibility as the synthesis of ultra-small (<10 nm in diameter) UCNPs showing large NIR-to-VIS optical conversion efficiencies has been recently demonstrated.²³ As a consequence, UCNPs are also being considered as promising...
optical probes for experiments at single-cell and single-particle levels.

As a result of the intensive research carried out on UCNPs during the last few years, a wide range of UCNPs consisting of different host lattices and dopants have appeared onto the scene.\textsuperscript{4,24,25} Modifying the different synthesis parameters could achieve among all of them, erbium and ytterbium doped NaYF\textsubscript{4} UCNPs are considered as the reference combination of dopants and host materials.\textsuperscript{3,23} In particular, the recently demonstrated possibility of synthesizing NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} upconverting nanorods (hereafter NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNRs) appears to be especially interesting as they constitute a unique system that could be used in a wide range of applications including security inking, cell tracking, cell manipulation, and bottom-up fabrication of nanofluidic and optical devices.\textsuperscript{14,26,29,30}

However, the full exploration of the potential applications of NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNRs would require remote three-dimensional control of their spatial arrangement. Such control becomes mandatory for, as an example, the construction of NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNR assemblies (interesting for security inking and nanofluidic applications) as well as for controlled incorporation of single NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNRs into living cells. At present, several techniques have been demonstrated to be capable of remote manipulation and assembly of different nanorods. These include the application of electric and magnetic fields as well as the use of laminar flows in microfluidic channels.\textsuperscript{31–33} Despite the good results obtained so far by these techniques, they lack the ability to provide real time three-dimensional spatial control. Optical tweezers are an appealing tool for real time three-dimensional manipulation of nanosized objects in aqueous environments.\textsuperscript{34,35} First demonstrated by Ashkin and co-workers, Optical Trapping (OT) of sub-micrometric structures is based on the gradient force created in the surroundings of a tightly focused laser beam.\textsuperscript{36,37} When a nanoparticle is randomly moving close to the laser focus, the optical electric field polarizes the nanoparticle so that it behaves as an electric dipole in a non-homogeneous electric field. As a consequence, the polarized nanoparticle is pushed towards the beam focus. OT and remote manipulation of a great variety of different nanostructures (including metallic nanoparticles, semiconductor nanowires, semiconductor quantum dots (QDs) and, more recently, UCNPs) have been already demonstrated.\textsuperscript{37–43} In previous experiments, the characterization of the dynamics of trapped nanostructures has been limited to accurate measurements of both the trapping force and particle incorporation rates. Nevertheless, practical applications require a deep understanding of the exact orientation of the optically trapped nanoparticles inside the optical trap. This is a challenging task since conventional approaches cannot be used: the trapped particle size is well below the resolution provided by optical microscopy. Thus, the design and development of non-direct strategies for nanoparticle tracking inside optical traps becomes necessary. As an example, Jauffred et al. determined the position distribution curve of optically trapped QDs by accurate tracking of their two-photon excited emission.\textsuperscript{37} In the case of highly asymmetric nanoparticles (such as nanorods) not only the position inside the trap is relevant but also their intra-trap orientation needs to be known. Such knowledge has been achieved in the case of optically trapped Gold Nanorods (GNRs) and niobate nanowires by the real time analysis of luminescence and by polarized Second Harmonic Generation, respectively. These pioneering experiments have demonstrated that orientation of asymmetric nanoparticles inside optical traps is far from easy to predict.\textsuperscript{39,44} Niobate nanowires were found to align along the trapping beam axis whereas GNRs oriented parallel to the polarization vector of the trapping laser beam. It is also worth mentioning that, apart from the particle material, the characteristics of the trapped particle, such as its length in the case of nanorods, deeply affect the way it is trapped.\textsuperscript{45} Despite the interest from both fundamental and applied point of view neither optical trapping of UCNRs nor their intra-trap orientation has been demonstrated so far.

In this work, a single-beam OT setup has been used to demonstrate stable optical trapping of NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNRs, with a highly anisotropic morphology. Resonant optical tweezers, in which the laser trapping radiation is partially absorbed by the optically trapped particle, allowed for real-time detection of the sequential incorporation of NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNRs into the optical trap by luminescence microscopy. Single NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNR spectroscopy in a dry environment was used to reveal the strong polarization dependence of the VIS luminescence generated by NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNRs. This property has been further used, through the analysis of the polarization state of intra-trap luminescence, to unequivocally elucidate the equilibrium orientation of optically trapped NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNRs with respect to the laser trapping beam.

**Experimental**

**Synthesis of NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} upconverting nanorods**

For the synthesis of NaYF\textsubscript{4}:2%Er\textsuperscript{3+},18%Yb\textsuperscript{3+} UCNRs we used a recently published protocol.\textsuperscript{46} The hydrothermal processing using microwave radiation (MAGNUM II ERTEC MV 02-02 reactor) was used to first prepare the lanthanide nitrate precursor salt (1.2 mM), which was further mixed with 14 mL of deionized water, 0.7 g (17.5 mM) of NaOH, 7.1 g (22.6 mM) of oleic acid (90 wt%), 10.0 g (21.7 mM) of ethanol and 0.3 g (7.2 mM) of NaF to obtain a milky homogeneous solution. After 30 min of stirring at room temperature, the solution was transferred into a Teflon vessel, sealed and then placed in a microwave reactor, followed by 8.5 h of hydrothermal processing at 250 °C, under average pressure lower than 25 atm, the solution of NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNRs was obtained. The synthesized NaYF\textsubscript{4}:Er\textsuperscript{3+},Yb\textsuperscript{3+} UCNRs were collected by centrifugation at 12 000 rpm for 15 min, and washed twice with ethanol. The as-synthesized NaYF\textsubscript{4}:2%Er\textsuperscript{3+},18%Yb\textsuperscript{3+} UCNRs
were dispersed in cyclohexane with a concentration of ca. 20 mg mL\(^{-1}\). In order to perform optical trapping experiments it was necessary to transfer NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNRs to a distilled water solution, for which we used the ligand removal procedure reported by Bogdan et al.\(^{22}\) Briefly, 1 mL of NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNRs in cyclohexane was mixed with 10 mL of deionized water for 2 h, while the pH of the solution was set at 4 with 0.1 M hydrochloric acid. After the reaction the aqueous solution was extracted with excess of cyclohexane to remove oleic acid molecules, further collected by centrifugation at 12 000 rpm for 15 min, washed and finally dispersed in distilled water with concentration of ca. 7 mg mL\(^{-1}\). Taking into account the mean size of a single NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNR and the density of the bulk NaYF\(_4\) matrix the concentration of the solution was recalculated to be \(\sim 10^{11}\) NRs per cm\(^{3}\). Distilled water was used as a trapping solution since NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNRs present a good colloidal character when dispersed in it without any evidence of agglomeration between the particles (see DLS measurements in Fig. S1†). Moreover, the low density of distilled water facilitates NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNR manipulation when trapped since no strong optical forces are needed in order to overtake the drag force. At this point, we should note that distilled water shows a non-negligible absorption coefficient at the trapping wavelength (980 nm). This could lead to the appearance of thermal effects in the surroundings of the trap. According to previous studies, under our experimental conditions, we had estimated that the temperature increment induced by the focused laser radiation is lower than 5 °C. We state that such reduced heating does not affect the optical trapping experiments.\(^{47}\)

### Optical trapping experimental setup

A single-beam optical tweezers setup is depicted in Fig. 1a. The 980 nm laser radiation coming from a single-mode fiber-coupled laser diode is collimated by a mounted Rochester aspheric lens (Thorlabs, A230TM-B) and then expanded by a 2× beam expander (Thorlabs, BE02M). This laser radiation is used for both optical trapping and to excite NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNR luminescence. All the experiments were performed by using the maximum laser power provided by the laser (60 mW). For multiple-beam optical trapping experiments, the single-beam optical trapping setup was modified as schematically illustrated in Fig. S2.† We experimentally observed that the total laser power provided by the 980 nm laser diode was insufficient to form two highly stable optical traps by itself. A second 1064 nm laser beam (Nd:YAG laser, Ventus, Laser Quantum, Photonic Solutions) was used to create two additional traps perfectly overlapping with the 980 nm ones. The 1064 nm beam was made collinear with the 980 nm beam using a beamsplitter (Thorlabs, BS020) to combine the two beams (as seen in Fig. S2†). Then, the collinear laser beams were both split into two by using a second beamsplitter, and then reflected off plane mirrors to recombine them as shown in Fig. S2.† By slightly changing the alignment of either of the plane mirrors it was possible to create a slight angular difference in the propagating beams, resulting in two separate optical traps when focused through a high numerical aperture microscope objective. The laser power at any of these two traps (80 mW) is the sum of the over-lapping 980 and 1064 nm laser powers. The extra contribution of the 1064 nm laser beam led to two stable optical traps. In summary, in this configuration, each optical trap is composed of the 1064 nm beam and the 980 nm laser beam; the more powerful laser operating at 1064 nm is used to provide the power for stable optical trapping, while the 980 nm radiation is needed for exciting NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNR luminescence (1064 nm absorption does not provide the sufficient emission from the trapped UCNR to perform accurate luminescence analysis). A 100× 1.25 NA oil-immersed microscope objective was used for single NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNR experiments while a 10× 0.10 NA microscope objective was used for spectral analysis of the NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNRs suspension in order to ensure the analysis of multiple NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNRs. For single NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNR polarized emission experiments, a drop of the colloidal suspension of NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNRs (~10\(^{11}\) NRs per cm\(^{3}\)) was dried on a microscope slide and covered by a cover glass to prevent oil from coming into contact with the sample. For optical trapping experiments, a diluted colloidal suspension of NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNRs (~5 × 10\(^{9}\) NRs per cm\(^{3}\)) placed inside a 100 μm height microchannel (Ibidi Inc., μ-Slide I 80106). For the analysis of the colloidal suspension of NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNRs (~10\(^{11}\) NRs per cm\(^{3}\)), it was placed inside a spectrometer cuvette (2 mm × 10 mm). For optical imaging a CMOS camera was used. Luminescence analysis was performed by optically coupling to the OT setup a high sensitivity Si CCD camera (Synapse, Horiba) attached to a monochromator (iH320, Horiba). At the entrance of the spectrometer a linear polarizer (Thorlabs, LPNI050-MP2) mounted on a graduated wheel was placed for the selection of the polarized emission collected from the sample.

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**Fig. 1** (a). Schematic representation of the experimental setup. (b) Time evolution of the recovered luminescence at the trap position during multiple-particle trapping experiment. Sequential steps denote the incorporation of a single NaYF\(_4\):Er\(^{3+}\),Yb\(^{3+}\) UCNR to the optical trap. Luminescence images show the change in the recovered intensity.
Results and discussion

Fig. 2a shows a Transmission Electron Microscopy (TEM) image of the NaYF$_4$:Er$^{3+}$,Yb$^{3+}$ UCNRs used all along this work. Statistical analysis of the TEM images provided the size histograms included in Fig. 2b from which the NaYF$_4$:Er$^{3+}$,Yb$^{3+}$ UCNR diameter and length were determined to be 140 ± 20 nm and 1100 ± 200 nm, respectively. Details of the synthesis method and sample preparation can be found in the Experimental section. Additionally, the crystal structure and detailed spectroscopic characterization of the studied NaYF$_4$:Er$^{3+}$,Yb$^{3+}$ UCNRs are published elsewhere. Fig. 2c shows an optical image of an aqueous suspension of NaYF$_4$:Er$^{3+}$,Yb$^{3+}$ UCNRs (0.7 wt%) revealing the excellent colloidal character of our NaYF$_4$:Er$^{3+}$,Yb$^{3+}$ UCNRs without any evident signs of precipitation during ensuing days. Fig. 2c also includes the optical image of the same cuvette containing the non-colored solution when optically excited by a 980 nm laser beam obtained by using a 600 nm long-pass filter. A clear red emission is observed that, according to the schematic energy level diagram shown in Fig. 2d, can be attributed to the $^4$F$_{9/2} \rightarrow ^4$I$_{15/2}$ transition of Er$^{3+}$ ions, optically excited by an Yb$^{3+}$ → Er$^{3+}$ non-radiative energy transfer process.

Dried sample experiments

It is possible to find in the literature numerous examples revealing that highly anisotropic nanoparticles could generate a highly polarized luminescence. This was firstly demonstrated in non-spherical QDs that show well differentiated polarization states in their luminescence when their aspect ratios exceed 2. Later, a strong polarization anisotropy was discovered in codoped Tm$^{3+}$ and Er$^{3+}$ UCNRs. The transition of the emission levels of interest corresponds to polarization states parallel and perpendicular to the NaYF$_4$:Er$^{3+}$,Yb$^{3+}$ UCNR axis, giving the two distinct spectra. Two dimensional map represents the emission intensities as a function of the emission polarization angle. Red dashed circle delimits ratio values above and under 1.

Fig. 3 (a) Emission spectra from a single NaYF$_4$:Er$^{3+}$,Yb$^{3+}$ UCNR immobilized on a surface for two perpendicular emission polarization angles. Purple (blue) line represents the recovered emission parallel (perpendicular) to the optical axis of the NaYF$_4$:Er$^{3+}$,Yb$^{3+}$ UCNR. Inset represents these two different polarizations of the electric field that gives the two distinct spectra. Two dimensional map represents the emission intensity of red band as a function of the emission polarization angle. Polar plot of the ratio ($R_{652/660}$) between 652 and 660 peak intensities as a function of the emission polarization angle. Red dashed circle delimits ratio values above and under 1.
the NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNR axis (see inset in Fig. 3a). As can be observed, the luminescence intensities of the two main peaks (652 and 660 nm) appear to be strongly polarization dependent. This is further evidenced in the two-dimensional map shown in Fig. 3a that includes the dependence of the emitted intensity as a function of the emission polarization angle (with respect to the NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNR axis). As can be seen, intensity peaks at 652 nm and 660 nm change with the polarization angle in a cyclic way. Fig. 3b reveals that the intensity ratio between 652 and 660 nm peaks \(R_{652/660}\) is hypersensitive to the polarization state. Values under and above 1 (inside and outside the red dashed circle) denote two polarization states, one dominated by the 652 nm peak intensity and a second one characterized by reaching the maximum intensity at 660 nm. Note that the \(R_{652/660}\) coefficient varies from 2.5 down to 0.5 when the polarization state is driven from being parallel to perpendicular to the NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNR axis. At this point we would like to mention that similar results were obtained when the \(\text{H}_2\text{I}_{1/2}\to\text{I}_{1/2}\) green emission was analyzed (see Fig. S4 in the ESI†). The large induced polarization variation (five-fold) in the intensity ratio reveals the \(R_{652/660}\) coefficient as a reliable and precise parameter to determine the relative orientation of NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs by polarized single-particle spectroscopy.

A tentative explanation of the polarized luminescence of NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs can be given based on the recently published work of Ping Chen et al.\(^{51}\) In this work, the authors demonstrated that the polarized luminescence of Erbium doped NaF \(_4\) nanodisks is due to the deterministic orientation of the crystallographic optical axis inside the nanoparticle. They claim that the optical axis in their nanostructures is perpendicular to the hexagonal (largest) face, so that the luminescence recorded along this direction does not show any polarization dependence. On the contrary, when measuring perpendicular to this direction, due to the existence of an anisotropic crystal field, the luminescence becomes strongly polarization dependent due to the appearance of polarization induced forbidden and allowed transitions.\(^{52}\) We state at this point that, very likely, the optical axis of our NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs lies parallel to their longest dimensions \(i.e.\) optical axis coincides with the geometrical axis of the UCNRs. This would lead to a non-polarized luminescence when measured along the longest dimension (as it is observed later in the Optical trapping experiments section) and to a strongly polarized luminescence when spectra are recorded perpendicular to the longest dimension of the UCN (see Fig. 3).

**Optical trapping experiments**

**Single-beam resonant optical trapping.** The experimental setup used for simultaneous luminescence tracking and OT of a single Er\(^{3+}/\)Yb\(^{3+}\) codoped UCN is schematically depicted in Fig. 1a. A detailed description of all the optical components can be found in the Experimental section. Briefly, a 980 nm laser beam was focused into a 100 µm height microchannel, which contains a diluted colloidal suspension of NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\), Yb\(^{3+}\) UCNRs, by using a 1.25 NA microscope objective. The 980 nm laser beam, partially absorbed by Yb\(^{3+}\) ions inside the NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs, was used to both trap the NaF \(_2\)Er\(^{3+}\), Yb\(^{3+}\) UCNR and, simultaneously, to excite its luminescence when incorporated into the trap. The luminescence generated by the optically trapped NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNR was collected with the same objective used for focusing the 980 nm excitation laser beam, and it was spectrally analyzed by optically coupling the OT setup to the a high resolution spectrometer. Simultaneously, the luminescence image of the optical trap was recorded with a CMOS camera. A 700 nm short-pass filter was used to prevent the 980 nm radiation from reaching either the CMOS camera or the spectrometer. The sequential incorporation of individual NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs into the trap could be monitored in real time by recording the time evolution of the trap luminescence intensity by using the CMOS camera. A typical intensity profile is shown in Fig. 1b. From this intensity profile, it is possible to identify three sharp intensity steps at 0.6, 1 and 1.6 min after switching on the 980 nm laser beam. Each intensity step accounts for a single trapped NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNR whose luminescence is added to that generated by a previously trapped NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNR. The luminescence images obtained after the incorporation of each single NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNR are shown as the inset in Fig. 1b. At this point it should be noted that the time interval between consecutive incorporation of NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs has been found to be strongly dependent on the concentration of NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs in the suspension and by the 980 nm laser power, as it was already demonstrated to occur for spherical shaped Er\(^{3+}/\)Yb\(^{3+}\) codoped UCNPs.\(^{53}\) The optical force acting on NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs was measured by applying the so-called hydrodynamic-drag method that is explained in detail in the ESL†. Fig. S5† includes the optical trapping force acting on a single NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNR as obtained at different 980 nm laser powers. The minimum laser power required for OT of a single NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNR under our experimental conditions was found to be 10 mW. This value is 5 times lower than the corresponding one previously reported by us for spherical Er\(^{3+}/\)Yb\(^{3+}\) codoped UCNP.\(^{54}\) Fig. S5† clearly reveals that the optical force increases linearly with the 980 nm laser power as it was, indeed, expected. From the linear fit of experimental data we have obtained an optical trapping constant close to \(k_{\text{trap}} \approx 2 \text{ pN W}^{-1} \text{ µm}^{-1}\), which can be compared to that previously found for other UCNP.\(^{54}\)

Finally, it should be also mentioned that, although fluctuations in the position of NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs could be taking place, the optically trapped NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs remained stable inside the trap. This is evidenced by the intensity profile shown in Fig. 1b in which sharp intensity drops down to the zero level (indicating that the NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs have escaped from the trap and no luminescence is recorded) are not observed. This is in contrast to the results recently published by Jauffret et al. who evidenced the escape of QDs from an optical trap by the observation of intensity drops in the intensity time profiles.\(^{37}\) We state at this point that the larger size of our NaF \(_2\)Er\(^{3+}\),Yb\(^{3+}\) UCNRs led to a
reduced mobility as well as to a larger optical force in such a way that the optically trapped NaYF₄:Er³⁺,Yb³⁺ UCNRs remain stable in the optical trap.

Once stable OT of UCNRs was experimentally achieved, the orientation of NaYF₄:Er³⁺,Yb³⁺ UCNRs inside the trap was elucidated. This has been accomplished by performing polarized spectroscopy on a single optically trapped NaYF₄:Er³⁺,Yb³⁺ UCNR. The emission spectra generated by an optically trapped NaYF₄:Er³⁺,Yb³⁺ UCNR were systematically analyzed for different polarization states. At variance with the experimental results shown in Fig. 3, we observed that the luminescence spectra generated along the trapping direction was only slightly polarization dependent. This is evidenced in Fig. 4a that includes the emission spectra generated by a single optically trapped NaYF₄:Er³⁺,Yb³⁺ UCNR as obtained for two arbitrary orthogonal polarizations. Within experimental error, they have been found to be virtually the same. In the emission spectra shown in Fig. 4a, the 660 nm line clearly dominates over the 652 nm peak, this being behavior independent of the polarization state as shown in the two-dimensional map where the emission intensity of the red band is represented as a function of the emission polarization angle. According to the data shown in Fig. 3, this fact suggests that the collected luminescence is polarized orthogonally to the axis of the trapped NaYF₄:Er³⁺,Yb³⁺ UCNR. This unequivocally implies that the NaYF₄:Er³⁺,Yb³⁺ UCNR axis is parallel to the k vector of the trapping laser beam, i.e. the NaYF₄:Er³⁺,Yb³⁺ UCNR is aligned parallel to the propagating direction of the trapping beam (see Fig. 4b). Fig. 4c shows the polar plot of the R₆₅₂/₆₆₀ ratio with the emission polarization angle. When analyzing in detail the polar plot obtained for R₆₅₂/₆₆₀, we observed that a nearly circular plot is obtained. This reveals that, when the luminescence is collected along the direction of the trapping beam, an isotropic scenario is obtained. This also concludes that the NaYF₄:Er³⁺,Yb³⁺ UCNR aligns parallel to the propagation direction of the trapping laser beam.

At this point it should be noted that near circular plot diagrams of the R₆₅₂/₆₆₀ intensity ratio would be achieved if the NaYF₄:Er³⁺,Yb³⁺ UCNR was orientated perpendicular to the trapping beam while rotating inside the trap with a rotation period much smaller than the acquisition time of luminescence spectra. In this scenario, the collected luminescence spectra result from a combination of the spectra obtained for the two polarization states shown in Fig. 3a, as it does occur when polarized spectroscopy is performed on a colloidal suspension of randomly oriented NaYF₄:Er³⁺,Yb³⁺ UCNRs (see Fig. S3b in the ESI†). Nevertheless, the emission spectra generated by an optically trapped NaYF₄:Er³⁺,Yb³⁺ UCNR does not show any relevant contribution of parallel polarized emission. Thus, the rotation of NaYF₄:Er³⁺,Yb³⁺ UCNR in a plane perpendicular to the laser trapping beam can be disregarded.

**Multiple-beam optical trapping.** The potential application of single particle polarized spectroscopy for three-dimensional monitoring of optically trapped UCNRs has been further explored by using a multiple-beam optical trap. A two beam optical tweezer setup was used to three dimensionally manipulate a single optically trapped NaYF₄:Er³⁺,Yb³⁺ UCNR. For this purpose a modification of the optical tweezers setup depicted in Fig. 1a was used (for more details see the Experimental section and Fig. S2†). Such a setup allowed for an accurate control over the distance and relative position between the two optical traps. Two different situations were found to take place. When optical traps are separated by a distance longer than one micron (approximately), they behave as two independent single-beam optical traps. When a single NaYF₄:Er³⁺,Yb³⁺ UCNR is optically trapped within one of the traps it aligns and remains parallel to the propagation axis of the beam (see Fig. 5a-c where a single UCNR is trapped in the bottom trap). Orientation of the UCNR is again evidenced by the luminescence spectrum in which the 652 nm and 660 nm emission peaks are of similar intensity, independent of the polarization angle. This is exactly the same result obtained in single-beam optical trap experiments. When the traps are close enough (distance between traps close to 1 μm), the trapped NaYF₄:Er³⁺,Yb³⁺ UCNR is subjected to the force field resulting from the superposition of both traps. Under these conditions, the force field becomes anisotropic and, as a consequence, the NaYF₄:Er³⁺,Yb³⁺ UCNR flips and orientates parallel to the line connecting both the traps. Thus, the proximity of both traps orients the NaYF₄:Er³⁺,Yb³⁺ UCNR in the plane perpendicular to the trap beam propagation direction. This is evidenced in the fluorescence image shown in Fig. 5d as well as in the associated single-particle luminescence spectrum acquired.
with the selection polarized parallel to the inter-trap connection line (see white arrows in Fig. 5a–d that indicate the analyzed polarization angle). Under these conditions, the emission spectrum is dominated by the 652 nm emission line indicating that the NaYF₄:Er³⁺,Yb³⁺ UCNR is aligned parallel to the polarizer direction, i.e. the NaYF₄:Er³⁺,Yb³⁺ UCNR is aligned parallel to the inter-trap connection line. The relative orientation of the UCNR and the two traps is schematically shown in Fig. 5e and f.

Further manipulation of the two trap positions by keeping this inter-trap distance close to 1 µm allows, in principle, for full control/rotation of the NaYF₄:Er³⁺,Yb³⁺ UCNR within the plane perpendicular to the laser beams’ direction. This possibility has been demonstrated by rotating one trap around the other by 90° and keeping the inter-trap distance fixed at 1 µm (see schematic drawings in the right column of Fig. 6). Rotation of the optically trapped UCNR is shown by the fluorescence images in the central column of Fig. 6. This in-plane rotation is further evidenced by the changes observed in the spectral shape of the polarized upconversion spectrum obtained by keeping the measured polarization angle fixed as indicated by arrows shown in Fig. 6. Rotation of the optical traps causes a shift from an emission spectrum dominated by the 652 nm emission line to an emission spectrum in which both 652 and 660 nm emission lines are of comparable intensity. This unequivocally reveals a complete 90° in-plane rotation of the NaYF₄:Er³⁺,Yb³⁺ UCNR. Note that the data shown in Fig. 5 and 6 do not only reveal the possibility of accurate three-dimensional optical manipulation of single UCNRS but also the continuous monitoring of their three-dimensional orientation by single particle spectroscopy.

**Conclusions**

In summary, resonant stable optical trapping of NaYF₄:Er³⁺, Yb³⁺ upconverting nanorods has been demonstrated. The efficient excitation of the Er³⁺ visible luminescence by the partially absorbed 980 nm trapping radiation of the Yb³⁺ ions, allowed for real time tracking of the optically trapped NaYF₄:Er³⁺,Yb³⁺ upconverting nanorods by simple luminescence imaging microscopy. The time evolution of the luminescence images from the optical trap evidenced the sequential incorporation of single NaYF₄:Er³⁺,Yb³⁺ upconverting nanorods as well as their stable localization inside the trap. Single-particle polarized spectroscopy experiments performed on immobilized NaYF₄:Er³⁺,Yb³⁺ upconverting nanorods revealed that their two-photon excited luminescence is strongly polarized, evidence for the existence of two well-defined polarization states corresponding to the polarization of luminescence perpendicular and parallel to the axis of NaYF₄:Er³⁺,Yb³⁺ upconverting nanorods. This strong polarization dependence of luminescence has been used to unequivocally determine the orientation of optically trapped NaYF₄:Er³⁺,Yb³⁺ upconverting nanorods inside single and double beam optical traps. It has been concluded that, under our experimental conditions, NaYF₄:Er³⁺,Yb³⁺ upconverting nanorods oriented parallel to the propagation direction of the trapping laser beam in a single-beam optical tweezers setup. Two beam optical trapping allowed for controlled three-dimensional manipulation of single NaYF₄:Er³⁺,Yb³⁺ upconverting nanorod whose three-dimensional orientation was unequivocally determined by the
analysis of the polarization state of their single particle luminescence.

The possibility, demonstrated here, of applying simple experimental approaches to achieve three-dimensional manipulation of the upconverting nanorods, whilst knowing their exact position and orientation, opens up a new avenue into their use in numerous applications ranging from biology to nanofluidics.

Authors contribution
The manuscript was written through contributions of all the authors. All the authors have given approval to the final version of the manuscript.

Conflict of interest
The authors declare no competing financial interest.

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Notes and references
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