Exploration of minimum energy conical intersection structures of small polycyclic aromatic hydrocarbons: toward an understanding of the size dependence of fluorescence quantum yields†

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Minimum energy conical intersection (MECI) geometries were searched for polycyclic aromatic hydrocarbons (PAHs) consisting of up to 26 atoms. The energy barriers to the obtained MECIs showed a correlation with their fluorescence quantum yields. This provides a theoretical rationale for the size dependence of the fluorescence quantum yields seen in these PAHs.

Introduction

The importance of the conical intersection (CI) in photochemical reactions has been noted in a number of studies.1−6 With particular regard to the ultrafast photo-decay process, several observations have been made of dynamics of species undergoing a nonadiabatic transition near the CI region.7−10 If a stable CI region that a molecule can access easily from the Franck–Condon (FC) region is present, an ultrafast non-radiative decay occurs dominantly upon photo-absorption. In this case, ab initio molecular dynamics (AIMD) simulations are ideally suited to an examination of the non-statistical dynamics of the ultrafast photoreaction. Such short-timescale (sub-10−100 picoseconds) AIMD simulations have been made possible by increases in computing power.

The CI region also plays a role in non-ultrafast photoreactions. For example, fluorescent molecules stay on the electronic excited-state potential energy surface (PES) on sub-nano- to micro-second timescales. In this case, radiative and non-radiative decays compete with each other, and their competition determines the fluorescence quantum yield. When the energy barriers to reach CI regions are sufficiently high, and are thus difficult to access from the FC region, the fluorescence process is dominant. However, AIMD simulations of the electronic excited-state PES on sub-nano- to micro-second timescales remain highly demanding, even for small molecules. Thus, in this study, we tackled the problem by directly finding minimum energy conical intersections (MECIs).

The MECI is the lowest energy point within a CI hyperspace, and MECI geometries have been optimized as a critical point, or a representative geometry, of the nonadiabatic transition.11−18 However, preparing initial geometries for MECI optimizations is not trivial, because MECI geometries are generally distant from the stable geometries in the ground state. Motivated by this, the seam model function (SMF) approach was proposed to find the all-important MECIs.19 In the SMF, automated stable structure search methods are initially applied to a model function on which approximate MECI structures can be obtained as local minima. These approximate structures are then optimized using a standard MECI optimization technique. This approach has been used extensively in the studies of the photodissociation mechanisms of small molecules.20 Recently, its applicability has been improved dramatically by the use of the spin–flip time dependent density functional theory (SF-TDDFT)21−23 in the electronic structure calculations and the use of the single-component artificial force induced reaction (SC-AFIR)24 method in the automated stable structure search.25,26

In the present study, MECI geometries for the lowest two singlet electronic states (denoted S1/S0-MECI) were systematically searched using the SMF/SC-AFIR/SF-TDDFT approach. These searches were applied to the five polycyclic aromatic hydrocarbons (PAHs) shown in Fig. 1 and initiated from their FC points. Transition state (TS) geometries between the FC region and the obtained MECIs were also determined. Based on the energies of the obtained MECI and TS structures, the size dependence of the fluorescence quantum yields seen in these PAHs is discussed.

Target system

In this study, the five smallest PAHs (listed in Fig. 1) were considered. The ground state electronic structures27−31 and

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† Electronic supplementary information (ESI) available: All of the MECI geometries and the relative energies are shown. See DOI: 10.1039/c5cp02103k
vertical excitation energies of these molecules have been studied extensively.\textsuperscript{32,33} The larger of these five PAHs exhibit larger fluorescence quantum yields, as summarized in Fig. 1.\textsuperscript{34} There are two possible reasons for this: (1) the radiative decay is faster in the larger PAHs, and/or (2) the non-radiative decay is slower in the larger PAHs. To discuss the latter, it is necessary to identify important non-radiative decay channels. In particular, the energy barrier to reach one of the S\textsubscript{1}/S\textsubscript{0}-MECIs indicates how often the molecule can reach a region with a small S\textsubscript{1}/S\textsubscript{0} energy gap. Thus, locating all of the stable S\textsubscript{1}/S\textsubscript{0}-MECIs provides a reasonable starting point for a discussion of the efficiency of the non-radiative decay.

The S\textsubscript{1}/S\textsubscript{0}-CI regions and the S\textsubscript{1}/S\textsubscript{0}-MECI structures of benzene have been studied thoroughly by Robb and co-workers.\textsuperscript{35–37} However, the S\textsubscript{1}/S\textsubscript{0}-MECIs for the larger PAHs have not been studied in detail. In this study, we therefore systematically explored the MECIs of the larger PAHs using the SMF/SC-AFIR/SF-TDDFT approach, and we discuss here the efficiency of the non-radiative decay.

Results and discussion

From the SMF/SC-AFIR/SF-TDDFT searches, 6, 12, 26, 14, and 17 independent MECI structures were found for benzene, naphthalene, phenanthrene, anthracene, and pyrene, respectively. Because of the lower symmetry in phenanthrene, the number of independent structures in phenanthrene was larger than that in the larger PAH, pyrene. The local minimum structures on the S\textsubscript{1} surface near the FC region (S\textsubscript{1,MIN}) were also optimized from each FC point, and the TS geometries between the S\textsubscript{1,MIN} and the MECIs were then optimized. The connection of the S\textsubscript{1,MIN} and the MECIs through the TSs was finally confirmed by the intrinsic reaction coordinate (IRC) calculations. The S\textsubscript{1,MIN} geometries, the TS geometries, the MECI geometries, and their relative energies are shown in the ESI.\textsuperscript{†}

The S\textsubscript{1,MIN}, the three most stable MECIs, and the related TSs for each PAH are summarized in Fig. 2. A low-energy MECI with a CH bond dissociation for pyrene was excluded, because a high-energy TS providing a route to the CI region was found. The most stable MECI geometry for benzene (shown in Fig. 2) was consistent with that determined in previous studies.\textsuperscript{35–37} The FC point and the three most stable MECIs for benzene were further optimized using the CASPT2/cc-pVDZ method. The S\textsubscript{1} energies determined using the CASPT2 method for the optimized FC, MECI\textsubscript{1}, MECI\textsubscript{2} and MECI\textsubscript{3} geometries of benzene were 4.84 eV, 4.97 eV, 5.07 eV, and 5.17 eV, respectively, relative to the ground state benzene. The geometries and the order of the relative energies were consistent with the SF-BHHLYP results shown in Fig. 2 (see the ESI for the geometries).

As shown in Fig. 2, the S\textsubscript{1,MIN} geometries were planar for all of the PAHs. In Fig. 2, the label “N/A” for the S\textsubscript{1,MIN} of phenanthrene indicates that the corresponding local minimum was not found. That is, the optimizers implemented in both GRRM and GAMESS showed oscillating behavior, and ultimately failed to reach a converged geometry. This oscillation was caused by the instability of the SF-TDDFT calculations for geometries in which the reference triplet state was nearly degenerate with the other triplet state. Although most of the MECIs were accessed from the S\textsubscript{1,MIN} in one step via a single TS, there were two cases showing two barriers, and one case in which there was no barrier. The MECI\textsubscript{2} of benzene and the MECI\textsubscript{3} of naphthalene fell into the two-barrier classification; for these two, only the higher TS is shown in Fig. 2. In the two-step path to the MECI\textsubscript{2} of benzene, MECI\textsubscript{3} was the intermediate, and MECI\textsubscript{2} and MECI\textsubscript{3} were connected by a small barrier. Among the two TSs along this path, the first TS between S\textsubscript{1,MIN} and MECI\textsubscript{3} was higher than the second TS between MECI\textsubscript{3} and MECI\textsubscript{2}. Thus, in Fig. 2, the first TS, which was identical to TS\textsubscript{2}, is presented as TS\textsubscript{3}. Similarly, for the MECI\textsubscript{3} of naphthalene, S\textsubscript{1,MIN} and MECI\textsubscript{3} were connected by two steps via the fourth stable MECI (see MECI\textsubscript{4} in the ESI). The TS connecting S\textsubscript{1,MIN} and MECI\textsubscript{4} was higher than that between MECI\textsubscript{4} and MECI\textsubscript{3}, and the former TS is shown as TS\textsubscript{3} in Fig. 2. The MECI\textsubscript{3} of anthracene corresponded to the case with no barrier; the corresponding TS\textsubscript{3} is indicated by “N/A” in Fig. 2. This was confirmed by the meta-IRC (the mass-weighted steepest descent path) determined from the MECI\textsubscript{3} of anthracene; the meta-IRC led directly to S\textsubscript{1,MIN}.

From the extensive list of MECI structures shown here, it was found that the stable MECI geometries for the PAHs could be categorized into three types characterized by the three stable MECI structures determined for benzene. In other words, the structural deformations in the stable MECIs were localized on a single ring in these small PAHs. Consequently, the relative energies for the most stable MECIs fell within a narrow range of 4.94–5.57 eV, as shown in Fig. 2.

Here, we discuss the magnitude of the fluorescence quantum yields based on the shape of potential energy surfaces. Fig. 3A and B show schematic illustrations of two different potential profiles: one illustrates the case in which the non-radiative decay is dominant (Fig. 3A), and the other illustrates the case in which the radiative decay with fluorescence is dominant (Fig. 3B). Fig. 3A shows an MECI in a lower energy region, relative to the FC point; in this case a non-radiative, ultrafast decay via the related CI region can take place. In the case of Fig. 3B, the lowest energy MECI is much higher in energy than the FC point. Hence, the access frequency of a molecule to the CI region is low, and the non-radiative decay should thus be slow. In other words, the relative importance of the radiative decay is high. In this manner, one can discuss the relative importance of the radiative...
decay by comparing the energy difference between the most stable MECI and the FC point, i.e., $E_{\text{Lowest-MECI}} - E_{\text{FC}}$. For a more quantitative prediction, the $S_1\text{MIN}$ and the TS connecting the $S_1\text{MIN}$ and the CI region are required, as illustrated in Fig. 3B. Based on the transition state theory, the Gibbs free energy gap between the $S_1\text{MIN}$ and the TS, i.e. $G_{S_1\text{TS}} - G_{S_1\text{MIN}}$, can be compared directly with the access frequency of a molecule to the CI region. In this study, the $E_{\text{Lowest-MECI}} - E_{\text{FC}}$ and $G_{S_1\text{TS}} - G_{S_1\text{MIN}}$ gaps were compared with the experimental fluorescence quantum yields, where $G_{S_1\text{TS}} - G_{S_1\text{MIN}}$ corresponds to the Gibbs free-energy gap at 298.15 K and 1 atm.

With this information in mind, the experimental fluorescence quantum yields were plotted against the two calculated energy differences, i.e., $E_{\text{Lowest-MECI}} - E_{\text{FC}}$ and $G_{S_1\text{TS}} - G_{S_1\text{MIN}}$, for the five PAHs, as shown in Fig. 4. The $G_{S_1\text{TS}} - G_{S_1\text{MIN}}$ gap for phenanthrene was excluded from Fig. 4, because the $S_1\text{MIN}$ geometry was not found at the SF-BHHLYP level, as noted above. As expected, the $G_{S_1\text{TS}} - G_{S_1\text{MIN}}$ gap showed a clear correlation with the experimental fluorescence quantum yields. For these PAHs, the $E_{\text{Lowest-MECI}} - E_{\text{FC}}$ gap also correlated well with the fluorescence quantum yields. This was because the TSs were close to the MECIs, and the $S_1\text{MIN}$ were also close to the FC point. Thus, in the following, the origin of the size dependence of fluorescence quantum yields is discussed based on the nature of the FC point and the MECIs.
an interesting correlation between the fluorescence quantum yields and the energy barrier to the CI region was discovered for these five small PAHs. This suggested that two processes—specifically, radiative decay with the emission of fluorescence and nonradiative decay near the conical intersection—were in competition. This correlation provided a theoretical explanation for the observed experimental trend that the larger PAHs showed stronger fluorescence. Further applications of the present approach to other fluorescent systems are in progress to investigate the generality of this correlation.

**Conclusion**

In the present study, S$_0$/S$_1$-MECIs were searched systematically using our own automated MECI search method, SMF/SC-AFIR/SF-TDDFT. The search was applied to five PAHs—benzene, naphthalene, phenanthrene, anthracene, and pyrene—and a total of 6, 12, 26, 14, and 17 independent S$_0$/S$_1$-MECI geometries were obtained, respectively. It was found that structural deformations in the stable MECIs were localized on a single ring, and that all of the stable MECIs could be classified into three types that were reported previously for benzene. Because of the localized nature of the stable MECIs, their relative energy did not depend strongly on the PAH size. In contrast, the vertical excitation energy decreases with increase in the PAH size. As a consequence, the energy barrier between the FC point and the lowest CI point increased with increase in the PAH size.

Based on the extensive MECI structural database determined here, an interesting correlation between the fluorescence quantum yields and the energy barrier to the CI region was discovered for these five small PAHs. This suggested that two processes—specifically, radiative decay with the emission of fluorescence and nonradiative decay near the conical intersection—were in competition. This correlation provided a theoretical explanation for the observed experimental trend that the larger PAHs showed stronger fluorescence. Further applications of the present approach to other fluorescent systems are in progress to investigate the generality of this correlation.

**Computational details**

The S$_0$/S$_1$-MECI geometries of five PAHs, benzene, naphthalene, phenanthrene, anthracene, and pyrene, were searched using the SMF/SC-AFIR/SF-TDDFT method, starting from the ground state equilibrium structure of each molecule. The BHLYP functional and the 6-31G* basis set were employed in the SF-TDDFT calculations (indicated by SF-BHLYP). The reference triplet ground state was calculated based on the spin-restricted open-shell framework. To apply the SMF/SC-AFIR/SF-TDDFT method to relatively large systems, coarse DFT/TDDFT grids were adopted in the initial automated structural search; all obtained MECI structures were then re-optimized using the default DFT/TDDFT parameters in the GAMESS program package. The collision energy parameter for the SC-AFIR method was set to 100 kJ mol$^{-1}$, a value that was confirmed as appropriate in our previous study. The S$_1$-minimum geometry near the FC-point was optimized from the FC-point. The TS geometries between S$_1$ and the MECIs were optimized for each PAH. For the S$_1$-MIN and TS geometries, the Gibbs free energies in the gas phase were computed at 298.15 K and 1.0 atm. For comparison, the three most stable MECIs of benzene were further optimized using MS-CASPT2/cc-pVQZ calculations for the lowest two singlet states, where the six electrons in six orbitals active space was adopted (see the ESI†). All of the SF-TDDFT calculations were performed using the GAMESS program, and the CASPT2 calculations were performed using the Molpro2012 program. The structural deformations and optimizations under the SMF/SC-AFIR approach were performed using a developmental version of the GRRM program.

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**Notes and references**